

Super-Kamiokande

Y.Totsuka
Kamioka

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Super-Kamiokande collaboration

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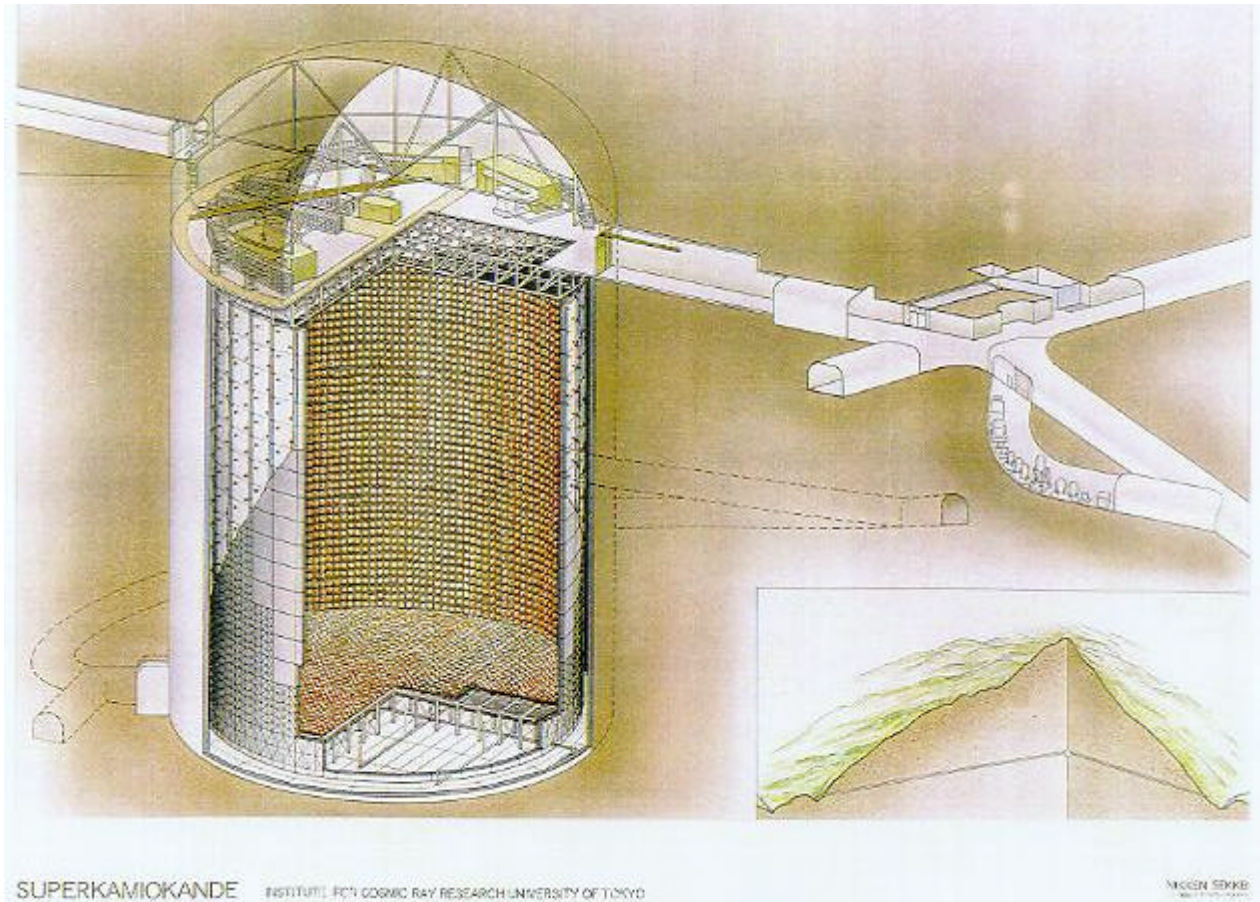
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Super-Kamiokande detector



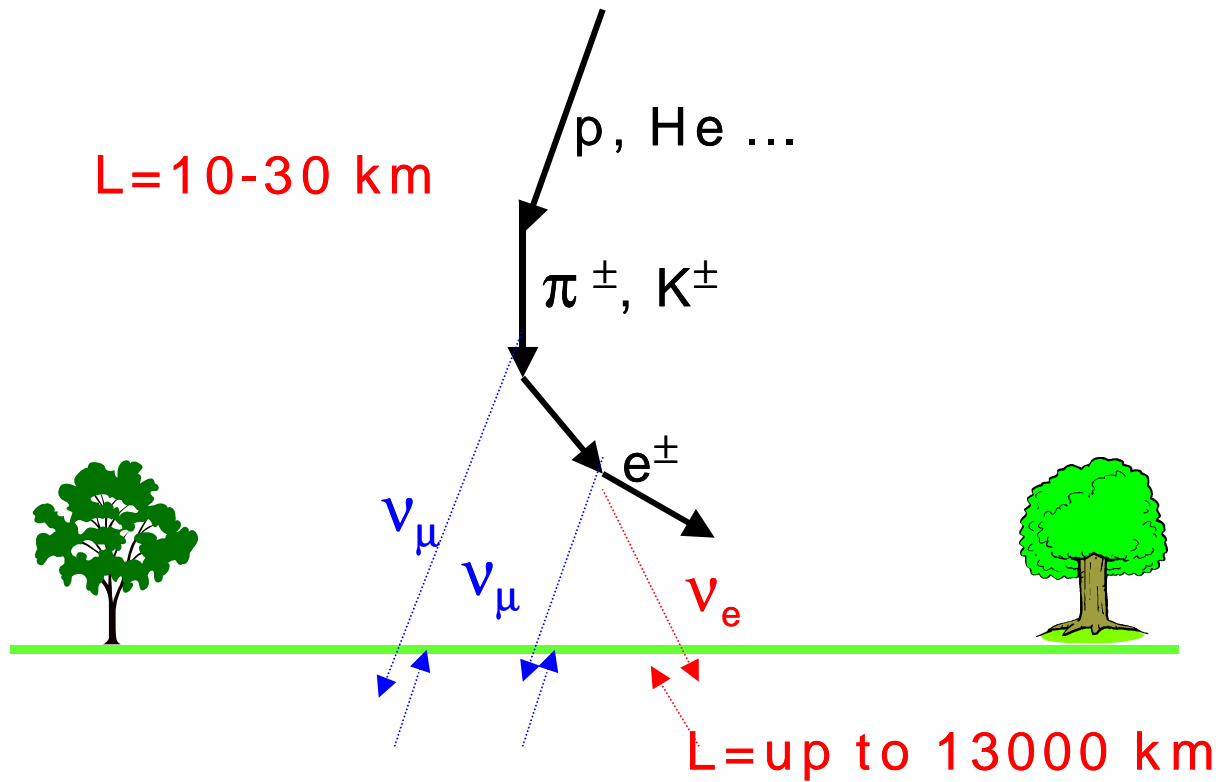
50,000 ton water Cherenkov detector
(22.5 kton fiducial volume)

1000m underground (2700 m.w.e.)

11,146 20-inch PMTs for inner detector

1,885 8-inch PMTs for outer detector

Atmospheric neutrinos



$$\frac{\overline{\nu_{\mu} + \nu_{\mu}}}{\overline{\nu_e + \nu_e}} = \sim 2 \quad \text{@ low energy } (E_{\nu} < 1 \text{ GeV})$$

$$\frac{\overline{\nu_{\mu} + \nu_{\mu}}}{\overline{\nu_e + \nu_e}} \quad \nearrow \quad \text{@ high energy}$$

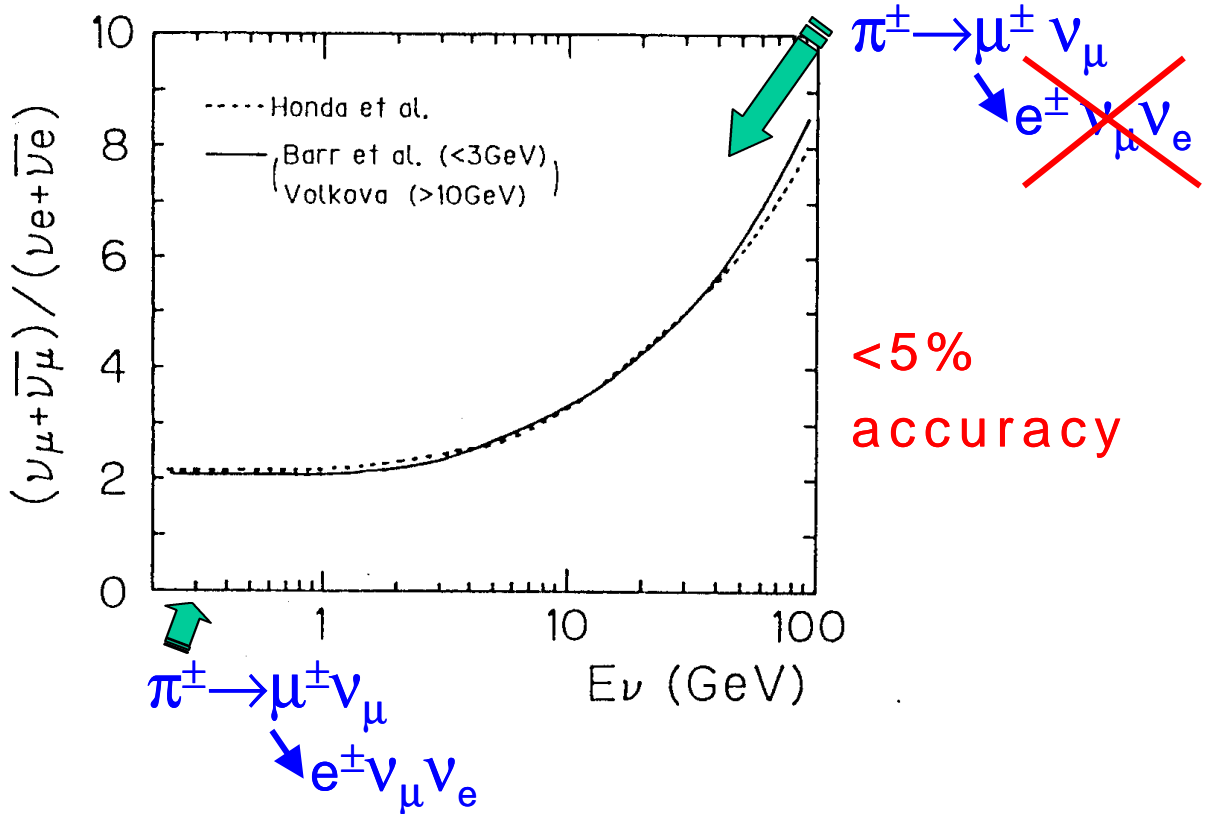
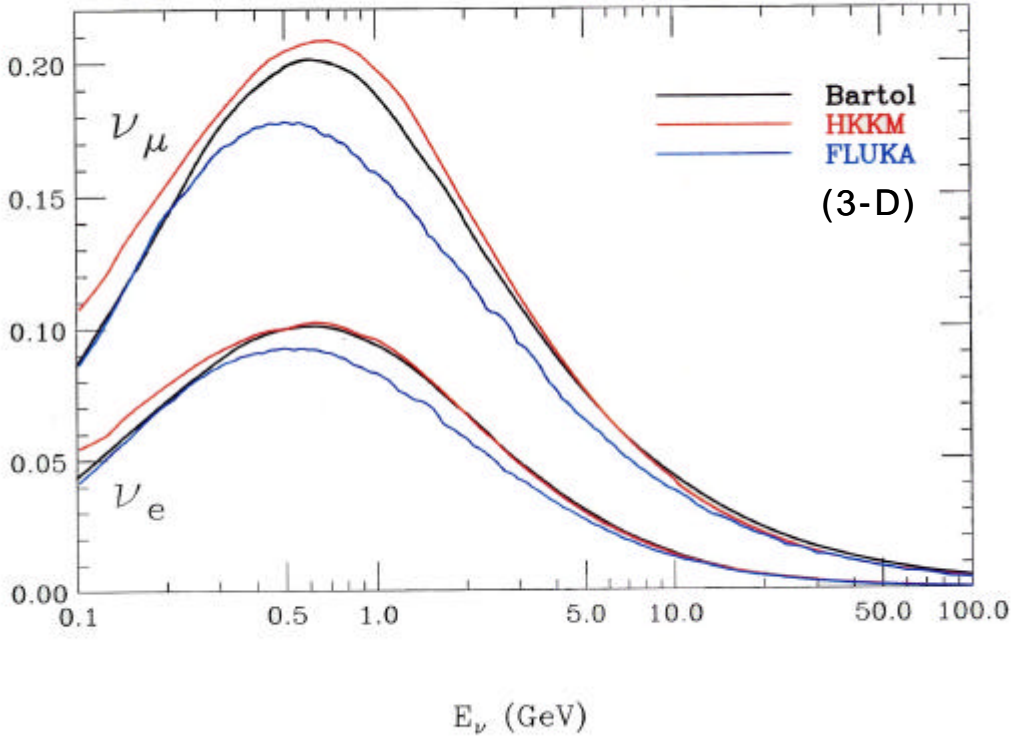
Error in absolute flux ~20%, but ν_μ/ν_e ratio ~5%

Neutrino oscillations :

$$\rightarrow \left(\frac{\overline{\nu_{\mu} + \nu_{\mu}}}{\overline{\nu_e + \nu_e}} \right)_{data} / \left(\frac{\overline{\nu_{\mu} + \nu_{\mu}}}{\overline{\nu_e + \nu_e}} \right)_{MC} \neq 1$$

Atmospheric neutrino spectrum

MODEL dependence of ENERGY spectrum (P.Lipari)



Primary cosmic ray flux

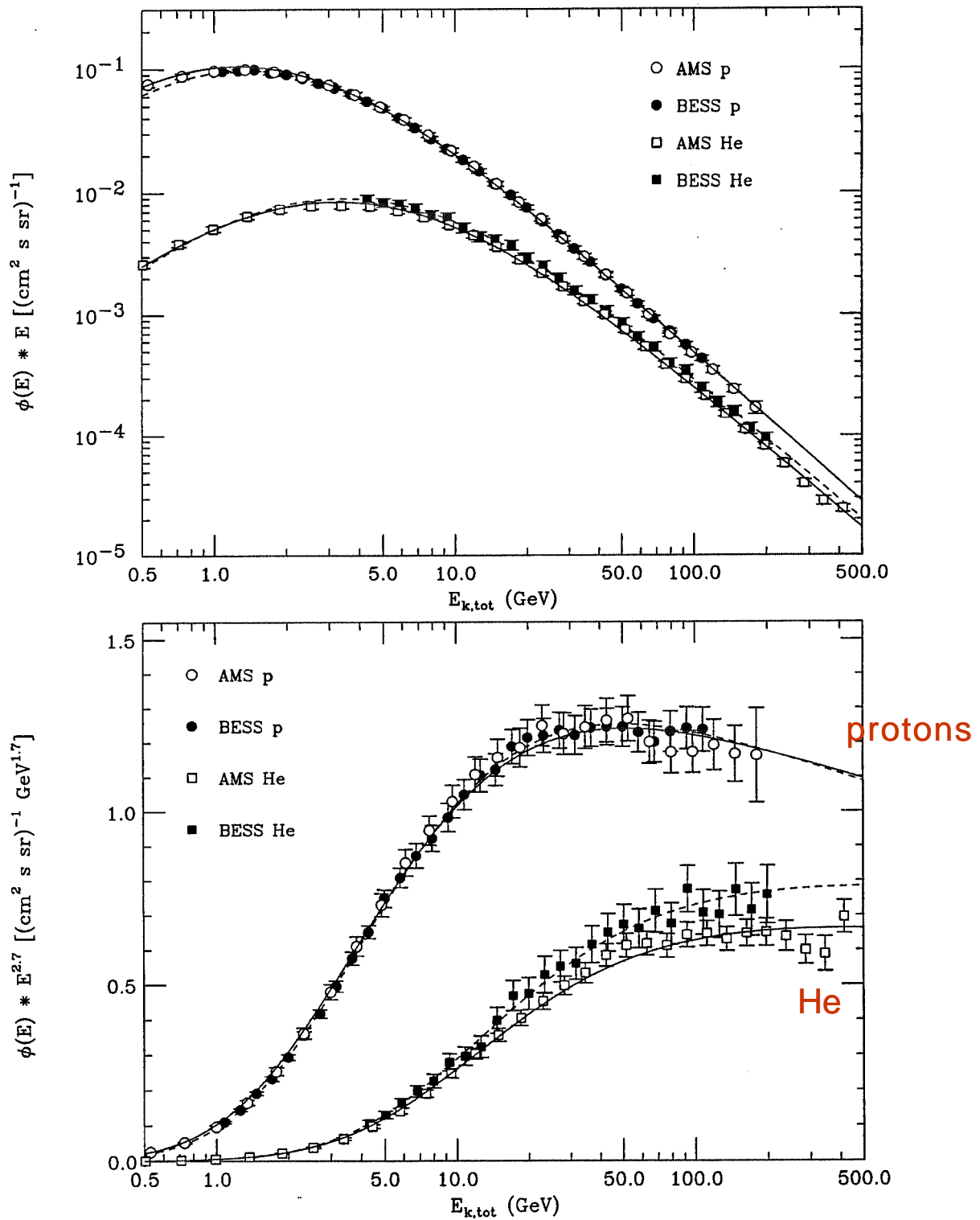
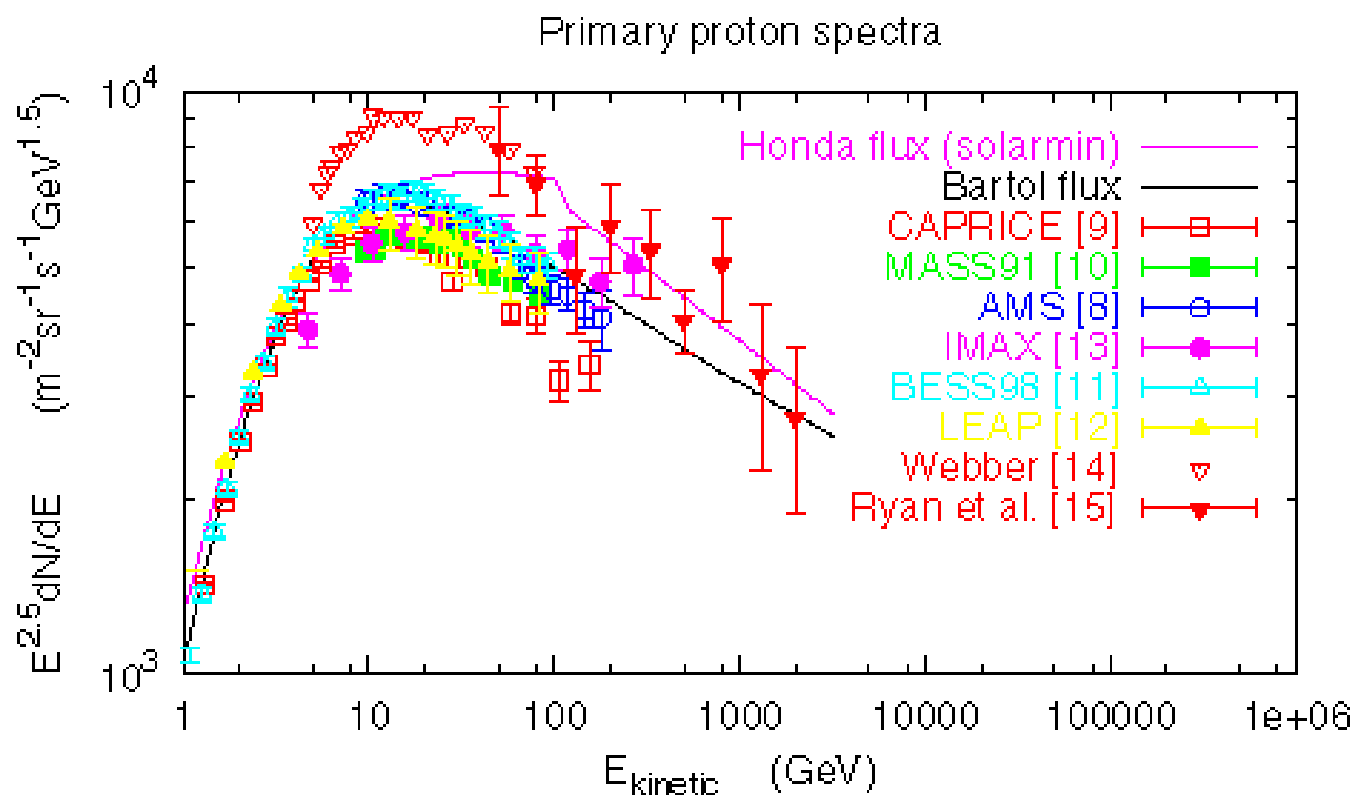
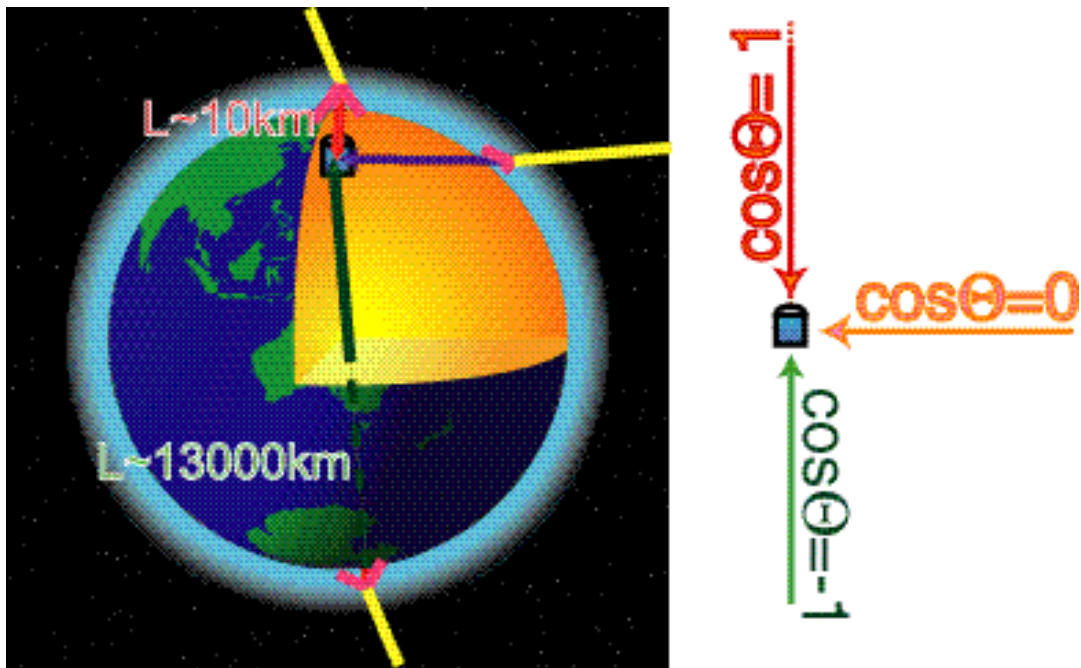


Figure 2: Fits to the AMS and BESS data (Energy per particle)

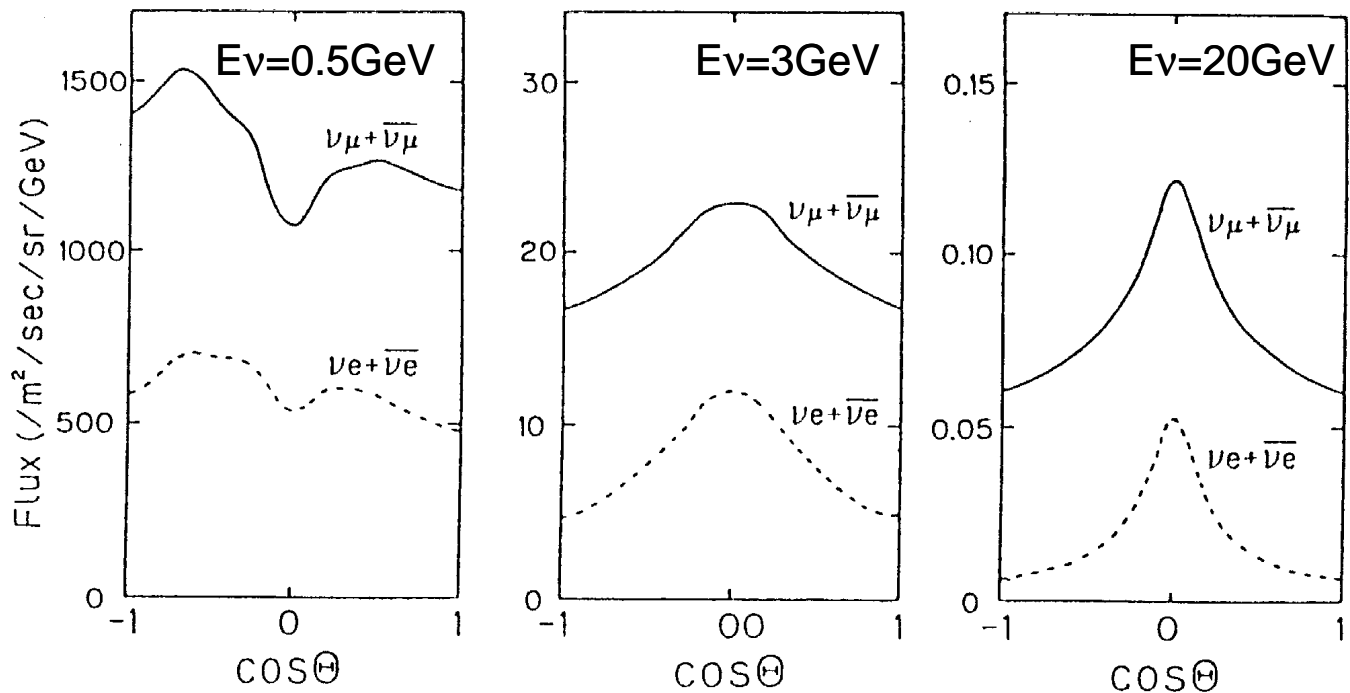
Bartol and Honda fluxes



Zenith angle distribution(1D)



Calculated zenith angle distribution

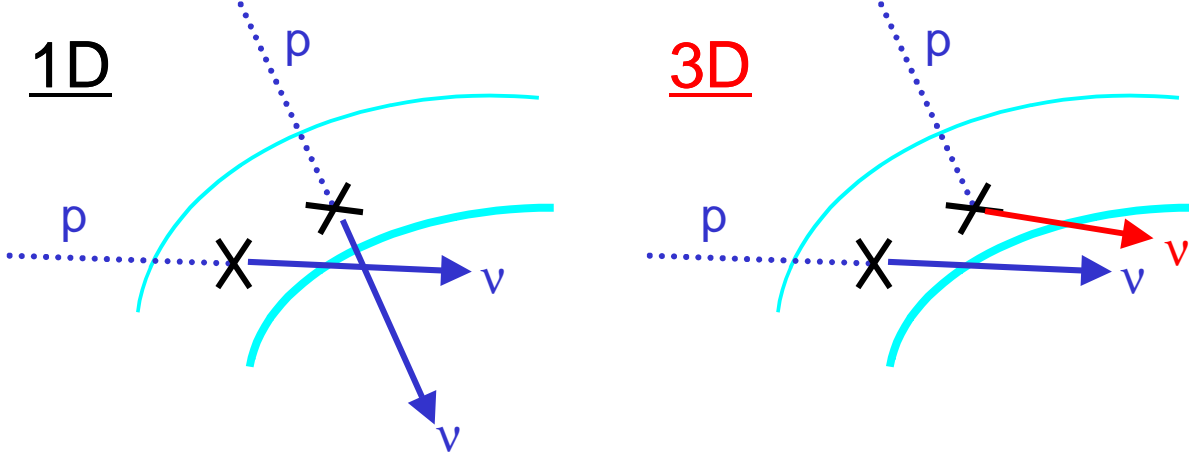


For $E_\nu > \text{a few GeV}$,
Upward / downward = 1 (within a few %)



Up/Down asymmetry for neutrino oscillations

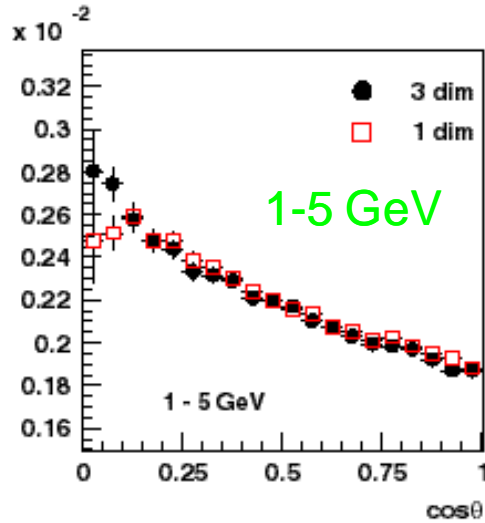
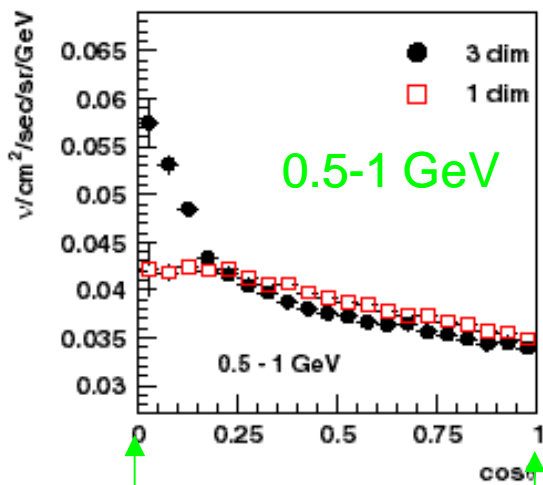
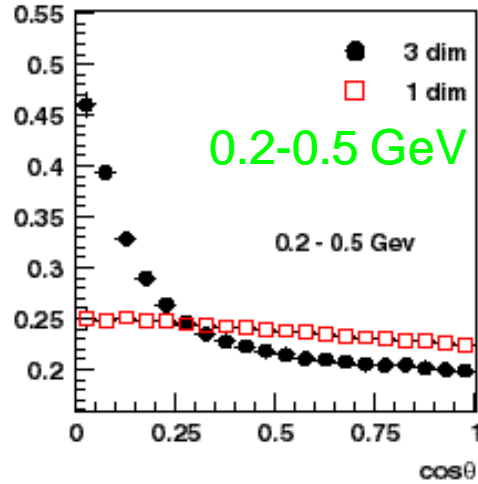
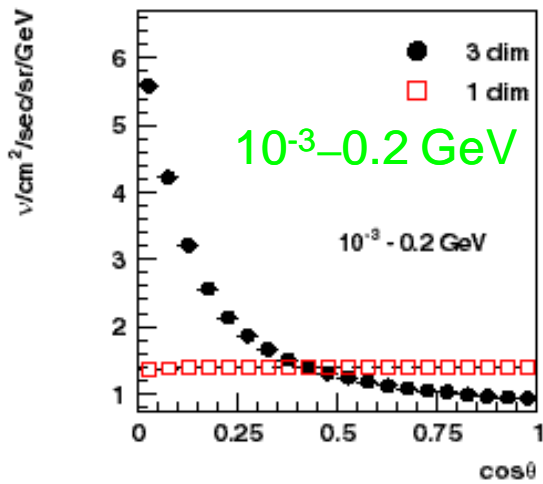
3D neutrino flux calculation



3D calculation by G. Battistoni et al.

(hep-ph/9907408)

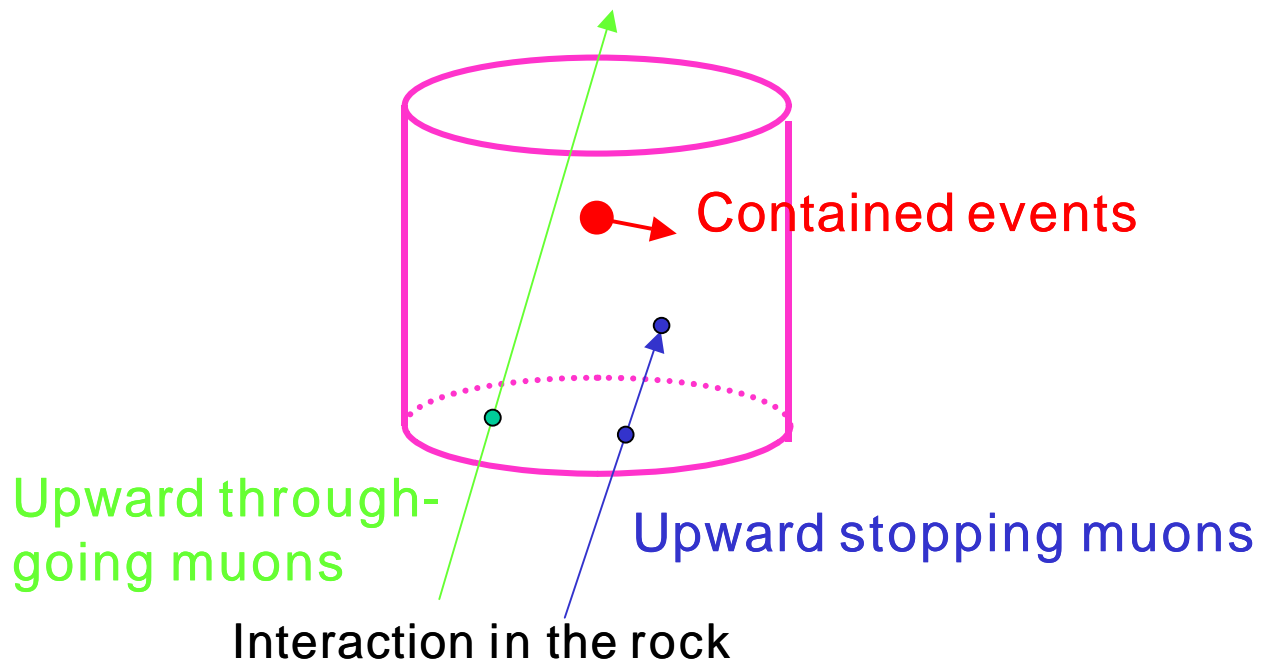
ν_μ



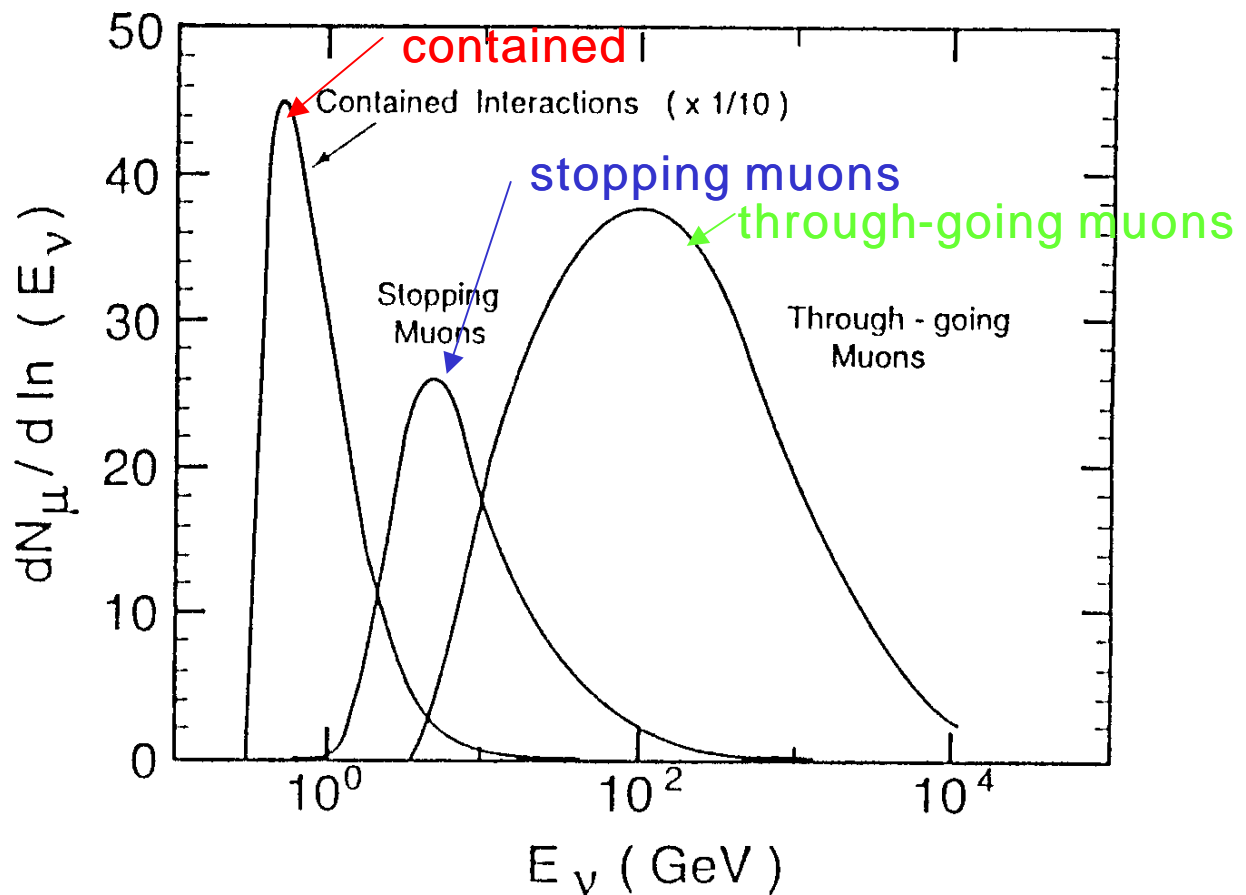
horizontal

vertical

How to detect atmospheric neutrinos



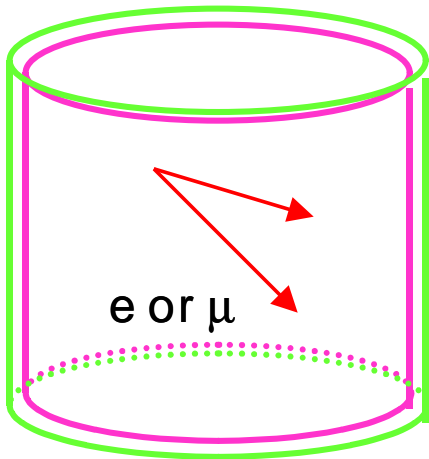
Initial neutrino energy spectrum



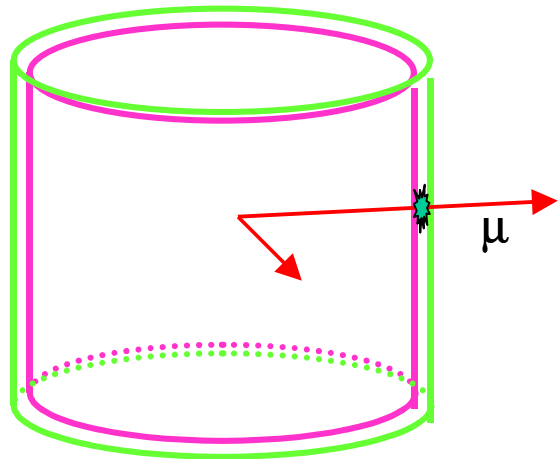
Contained event analysis

Fully Contained (FC)

Partially Contained (PC)



No hit in Outer Detector



One cluster in Outer Detector

Reduction

Automatic ring fitter
Particle ID
Energy reconstruction

Fiducial volume (>2m from wall, 22 ktons)
 $E_{vis} > 30 \text{ MeV}$ (FC), $> 3000 \text{ p.e.}$ ($\sim 350 \text{ MeV}$) (PC)

Final sample:

FC: 8.2 ev./day, PC: 0.58 ev./day

$E_{vis} < 1.33 \text{ GeV}$: Sub-GeV

$E_{vis} > 1.33 \text{ GeV}$: Multi-GeV

Fully contained event summary

(1289.4 d (79.3 kt . y))

Sub-GeV (Fully Contained)

$E_{\text{vis}} < 1.33 \text{ GeV}, P_e > 100 \text{ MeV}, P_\mu > 200 \text{ MeV}$

	Data	MC(Honda flux)
1ring e-like	2864	2667.6
μ-like	2788	4072.8
Multi ring	2159	2585.1
Total	7811	9325.5

$$\frac{(\mu/e)_{\text{Data}}}{(\mu/e)_{\text{MC}}} = 0.638 \pm 0.017 \pm 0.050$$

Multi-GeV

Fully Contained ($E_{\text{vis}} > 1.33 \text{ GeV}$)

	Data	MC(Honda flux)
1ring e-like	626	612.8
μ-like	558	838.3
Multi ring	1318	1648.1
Total	2502	3099.1

Partially Contained (assigned as μ-like)

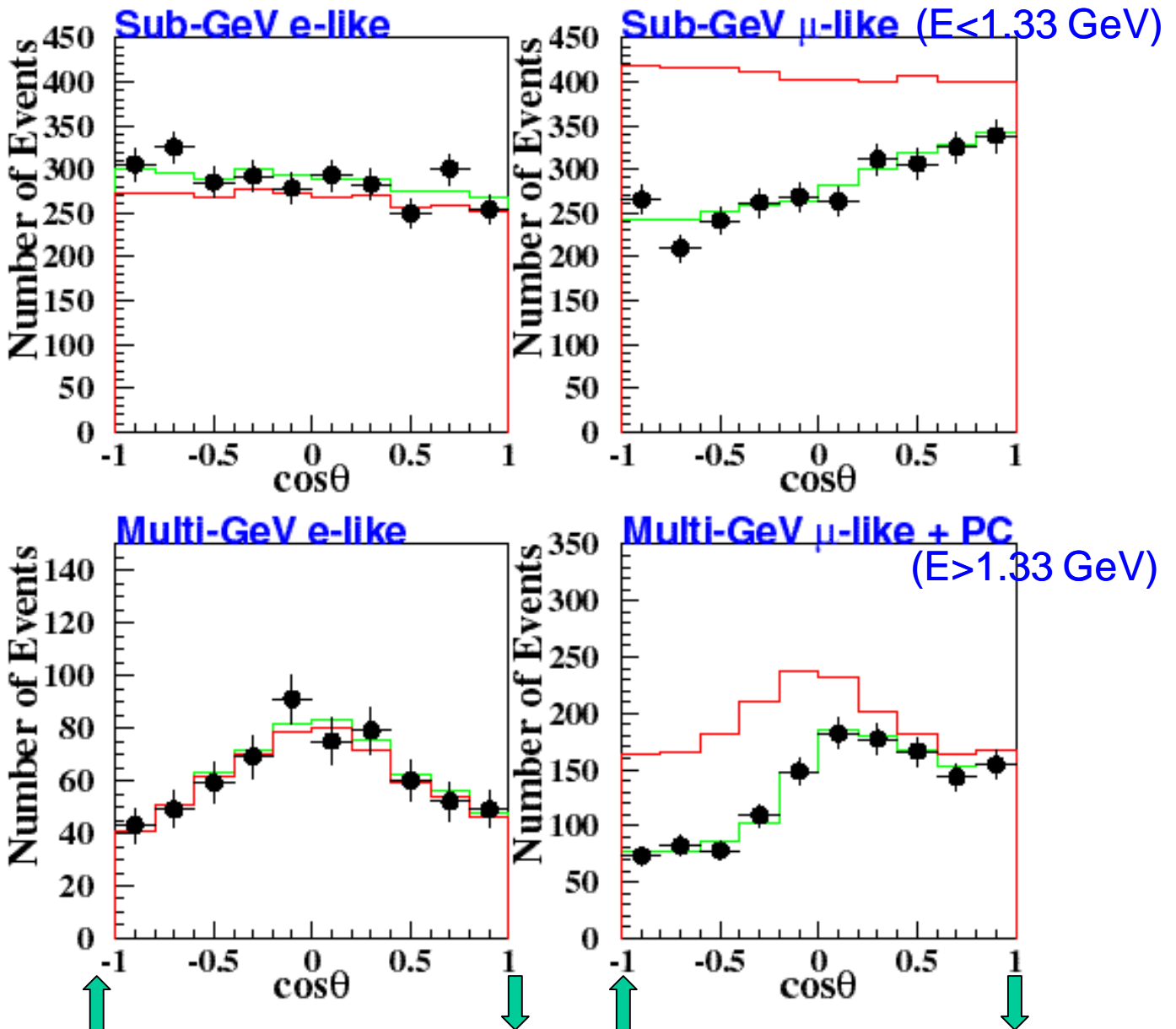
Total	754	1065.0
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$$\frac{(\mu/e)_{\text{Data}}}{(\mu/e)_{\text{MC}}} = 0.675 \begin{matrix} +0.034 \\ -0.032 \end{matrix} \pm 0.080$$

Zenith angle distribution

1289 days (79.3 kt . yrs)

- No oscillation
- Best fit ($\Delta m^2=2.4 \times 10^{-3} \text{eV}^2$, $\sin^2 2\theta=1.00$)



$\chi^2(\text{best fit}) = 132.4/137 \text{ d.o.f.}$

$\chi^2(\text{no osc.}) = 299.3/139 \text{ d.o.f.}$

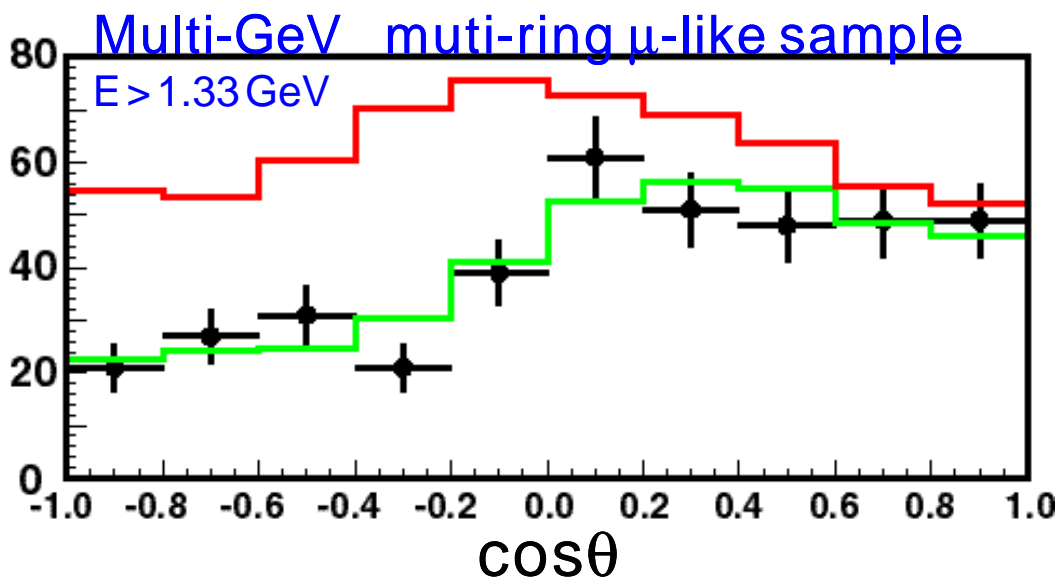
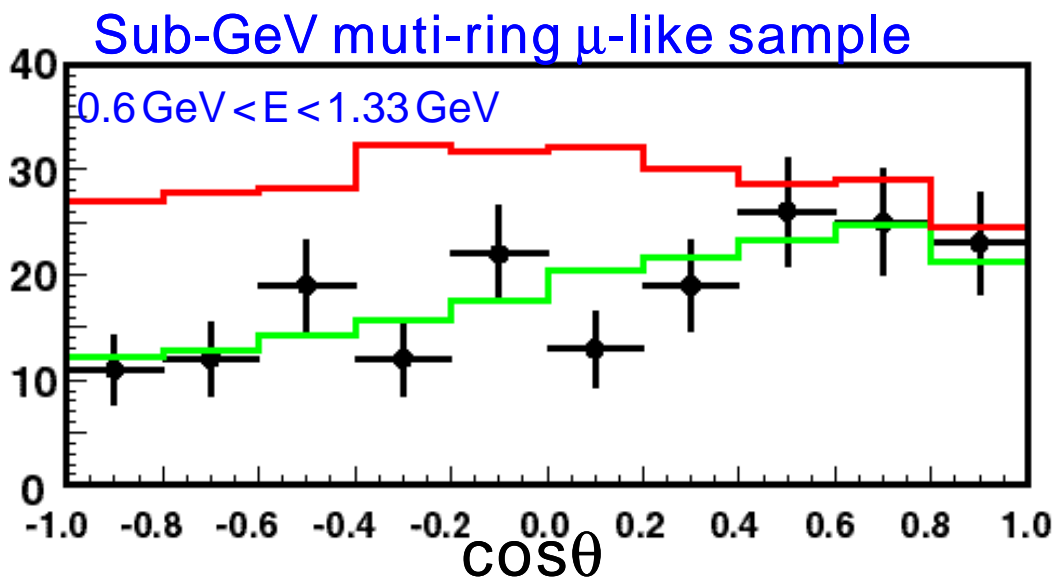
$\Delta\chi^2 = 167$

Multi-ring event analysis

1289 days (79.3 kt . yrs)

Zenith angle distributions preliminary

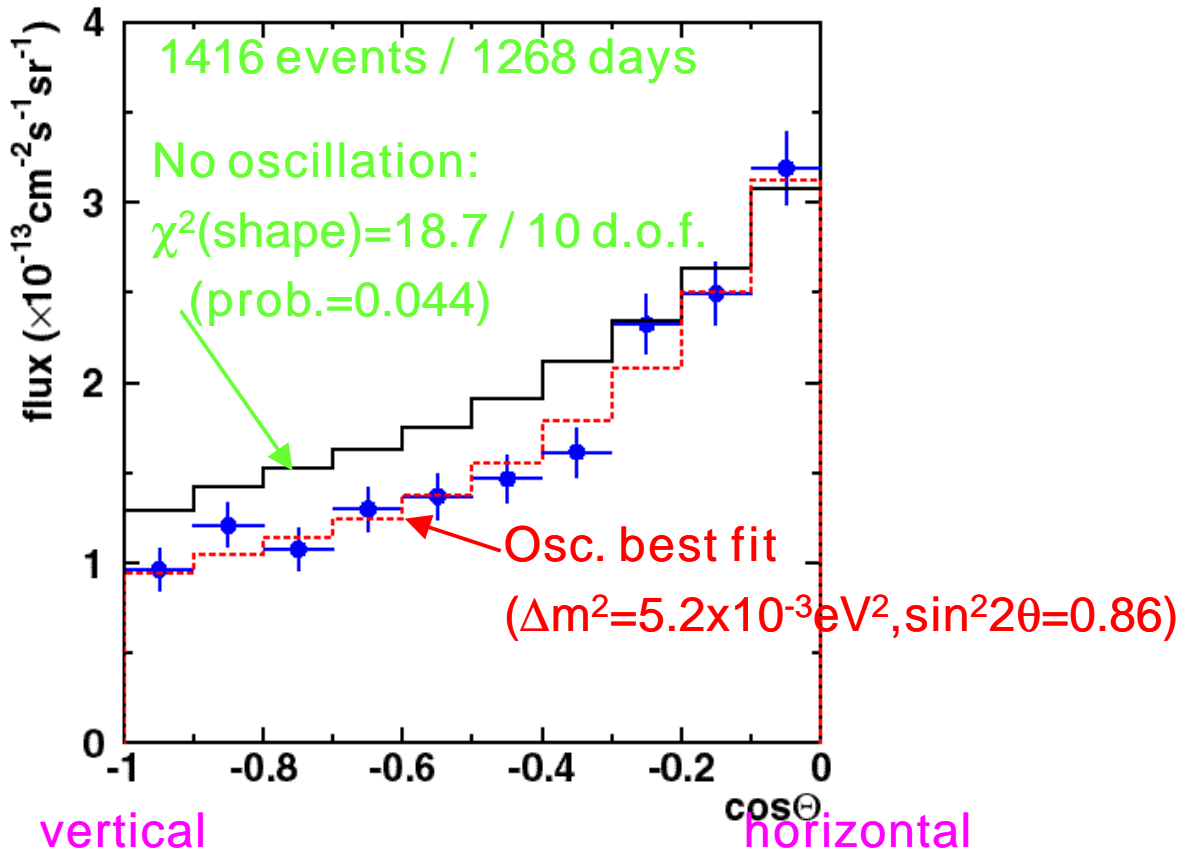
- No oscillation
- Best fit ($\Delta m^2=2.0 \times 10^{-3} \text{eV}^2$, $\sin^2 2\theta=1.00$)



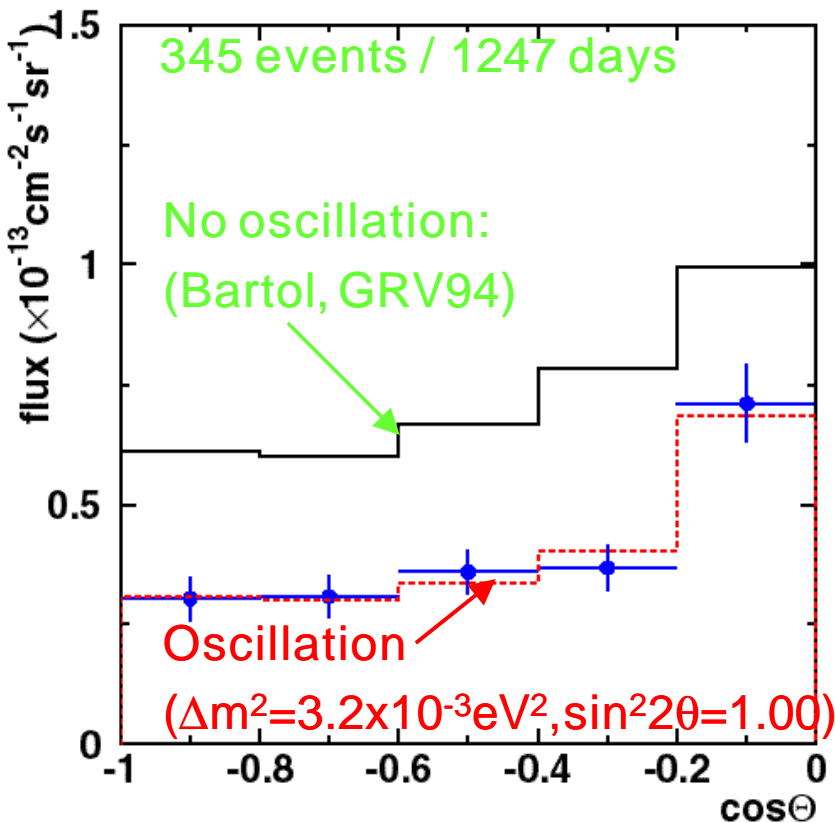
The zenith angle distortion is consistent with single-ring analysis.

Zenith angle distributions of upward-going muons

Upward through-going muons

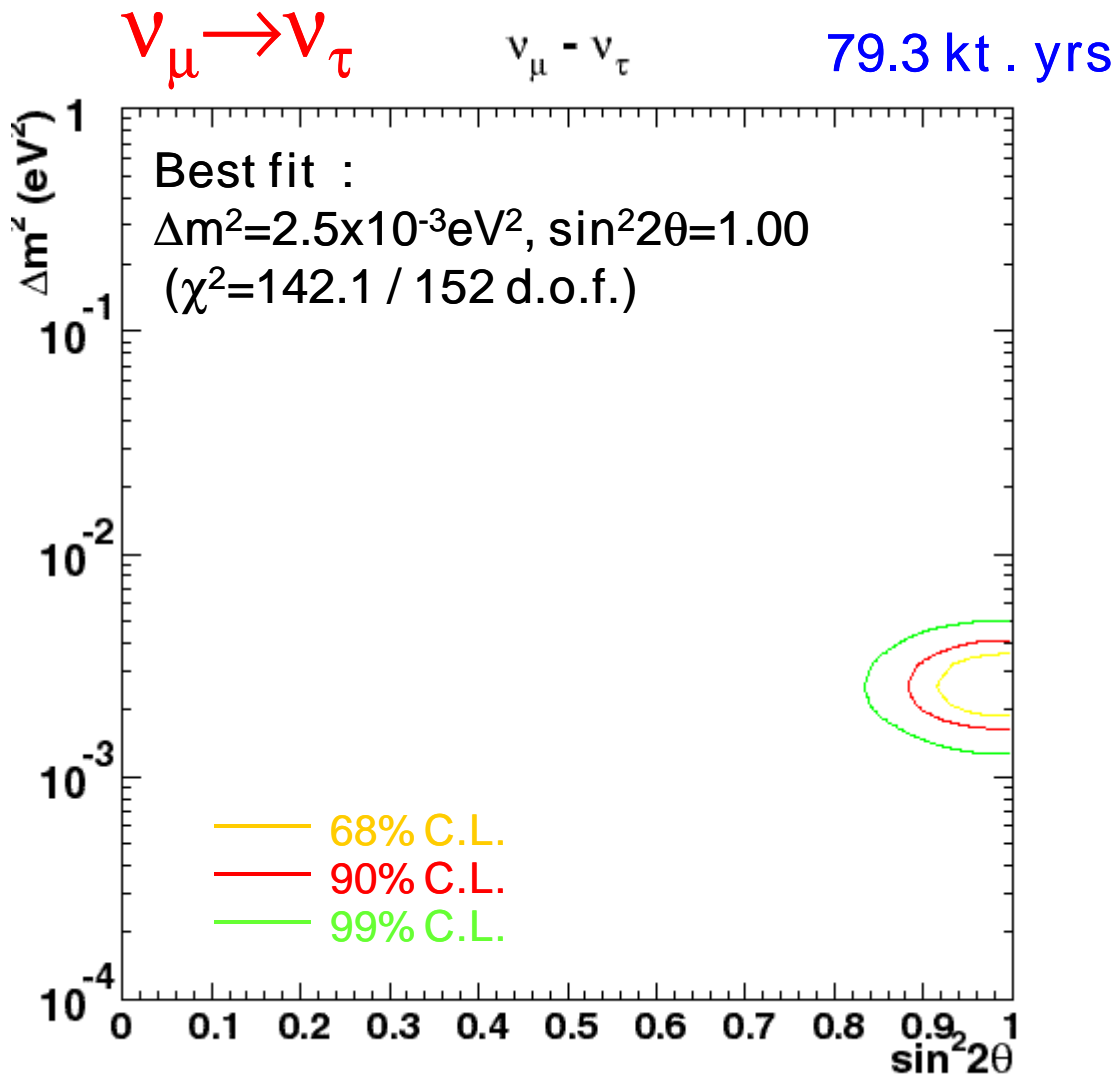


Upward stopping muons



$$\begin{aligned}
 & \frac{\left(\begin{array}{c} \uparrow \text{stopping } \mu \\ \uparrow \text{through } \mu \end{array} \right)_{\text{Data}}}{\left(\begin{array}{c} \uparrow \text{stopping } \mu \\ \uparrow \text{through } \mu \end{array} \right)_{\text{MC}}} \\
 &= \frac{0.241 \pm 0.016 \quad \begin{array}{c} +0.013 \\ -0.011 \end{array}}{0.368 \quad \begin{array}{c} +0.049 \\ -0.044 \end{array}} \\
 &= 0.65 \pm 0.04 \pm 0.09 \\
 &<< 1
 \end{aligned}$$

Allowed region
(FC + PC + UP-thru + UP-stop)

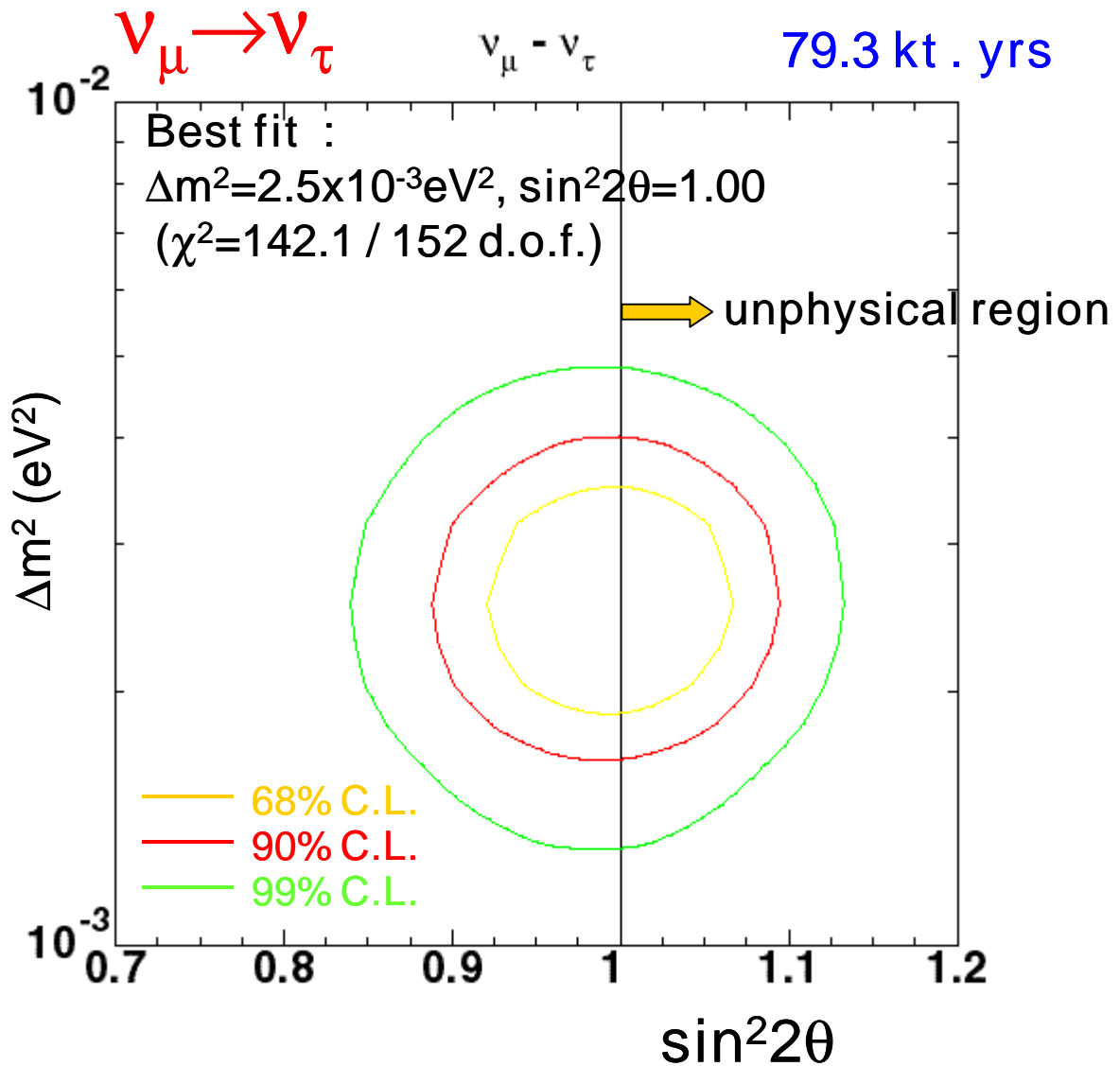


SK combined result

$$\Delta m^2 = (1.7 \sim 4) \times 10^{-3} \text{eV}^2$$

$$\sin^2 2\theta > 0.89 \quad (90\% \text{ C.L.})$$

Allowed region - II
(FC + PC + UP-thru + UP-stop)



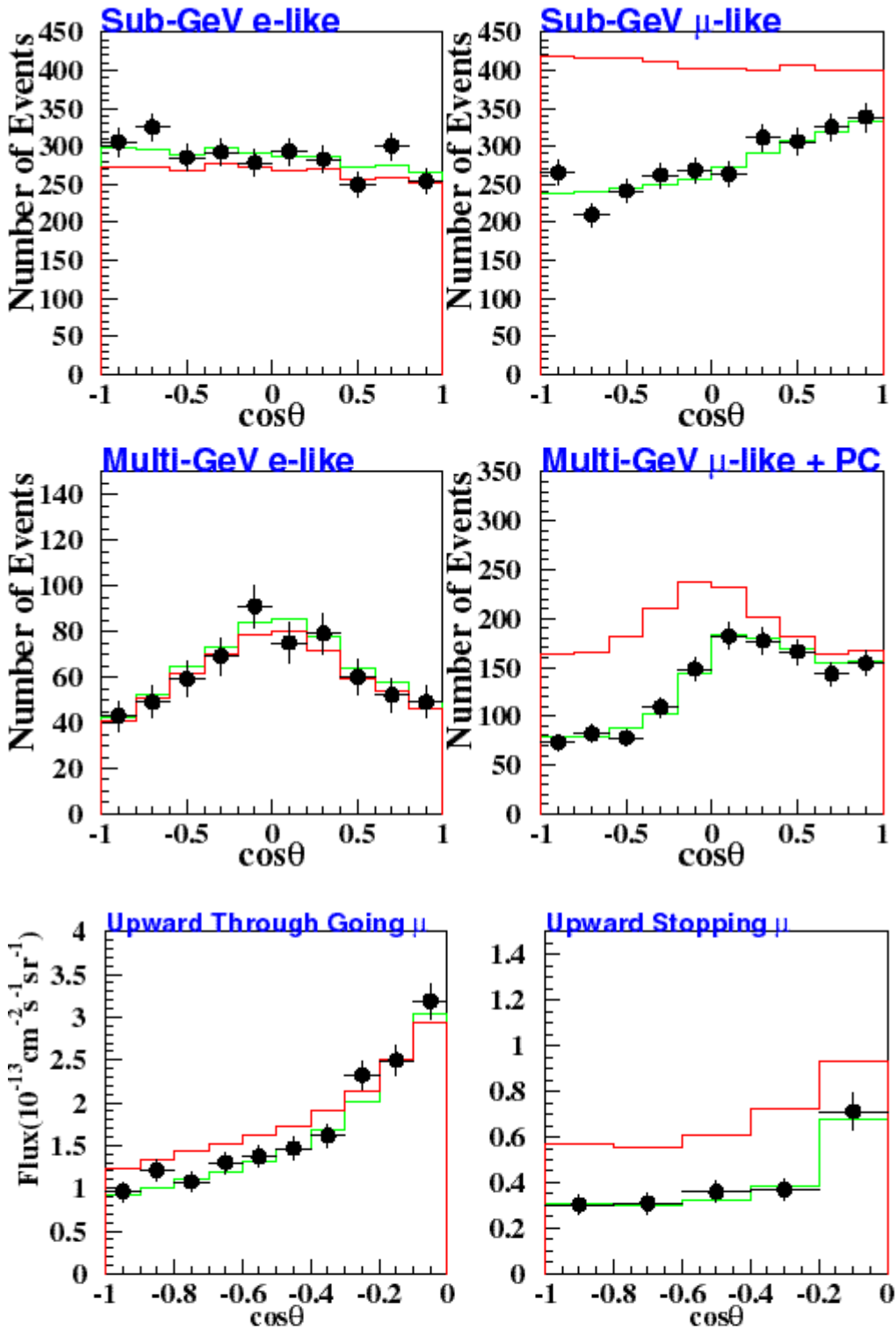
SK combined result

$$\Delta m^2 = (1.7 \sim 4) \times 10^{-3} \text{eV}^2$$

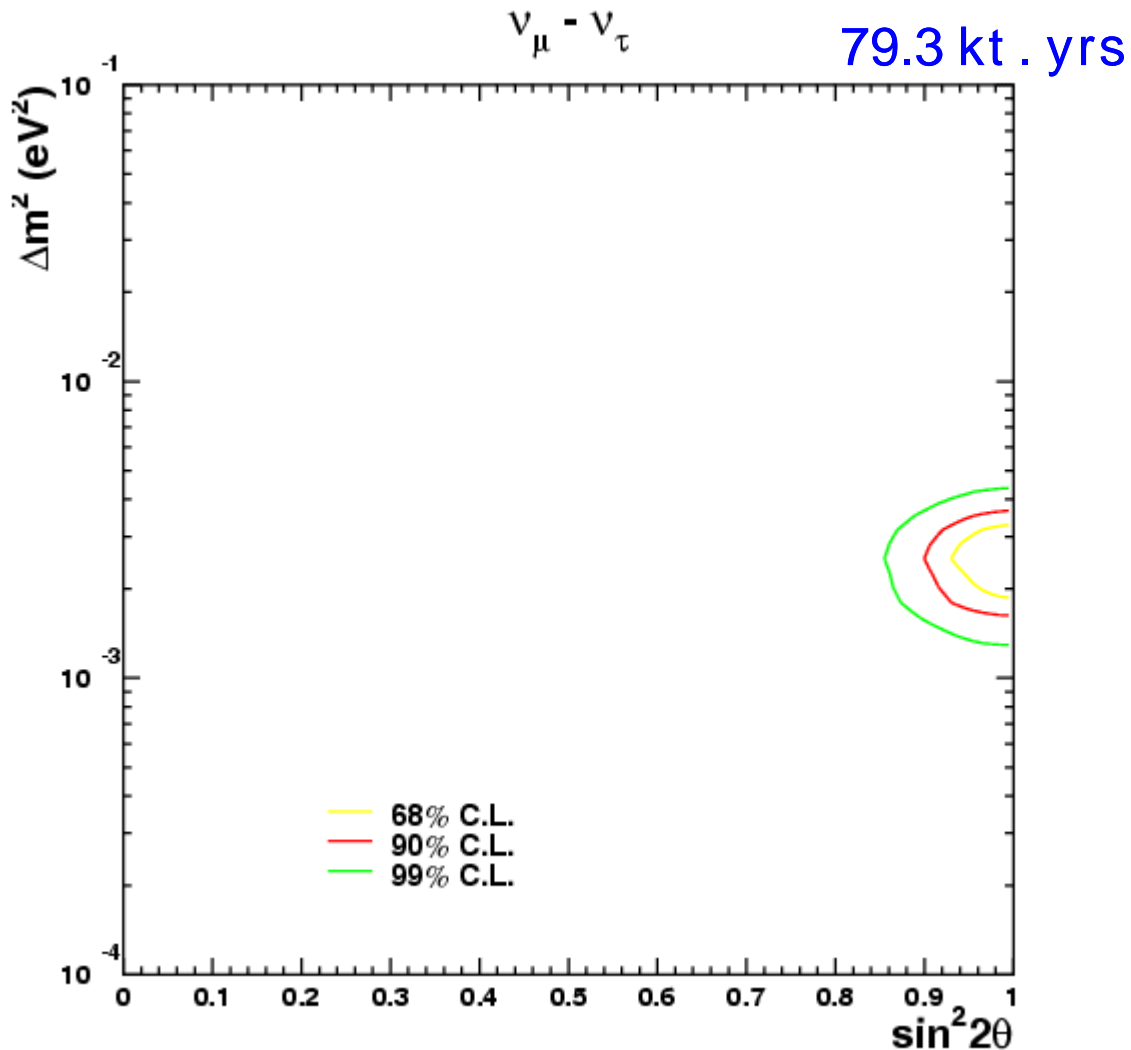
$$\sin^2 2\theta > 0.89 \quad (90\% \text{ C.L.})$$

Zenith angle distributions for the best fit

- No oscillation
- Best fit ($\Delta m^2 = 2.5 \times 10^{-3} \text{eV}^2$, $\sin^2 2\theta = 1.00$)



Allowed region (grand global fit)
(FC + PC + UP-thru +
UP-stop + multi-rings)



Within physical region;

$$\chi^2_{\min} = 157.5/170 \text{ dof}$$

$$\text{at } \sin^2 2\theta = 1.0, \Delta m^2 = 2.5 \times 10^{-3} \text{ eV}^2$$

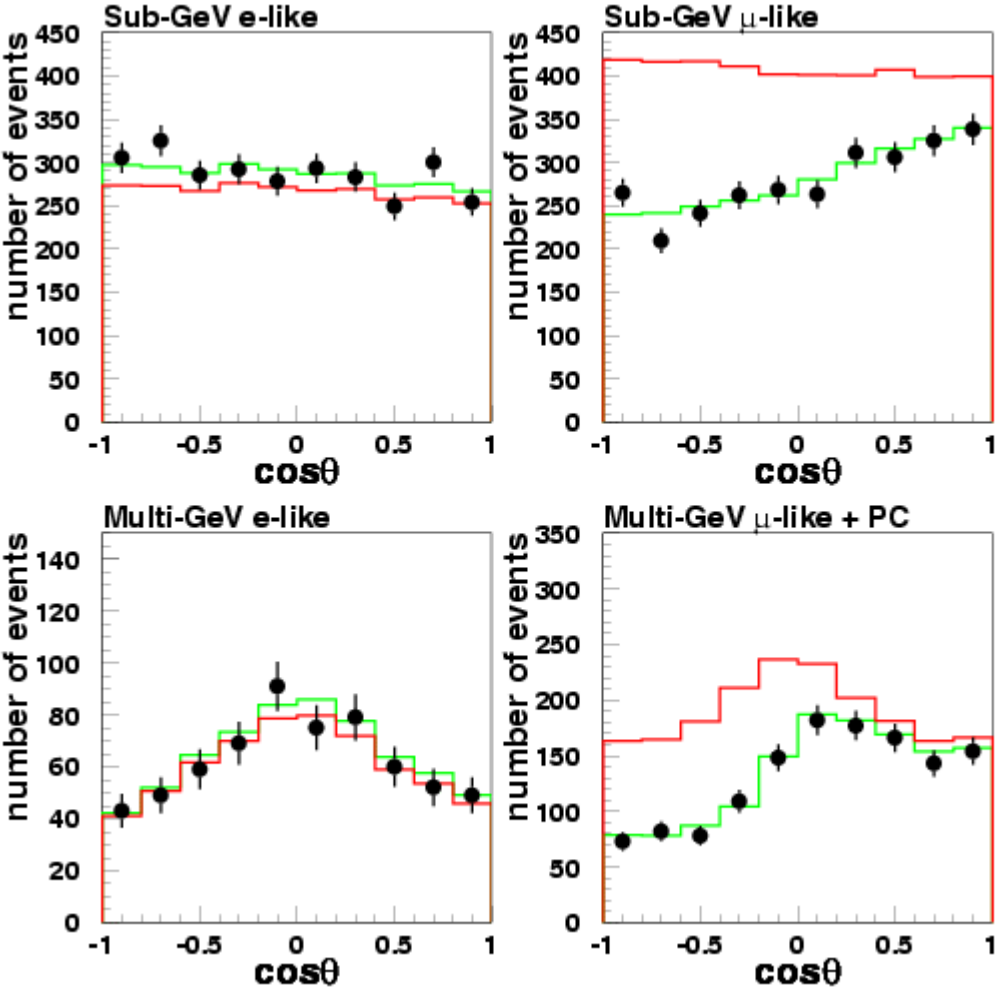
With unphysical region;

$$\chi^2_{\min} = 157.4/170 \text{ dof}$$

$$\text{at } \sin^2 2\theta = 1.01, \Delta m^2 = 2.5 \times 10^{-3} \text{ eV}^2$$

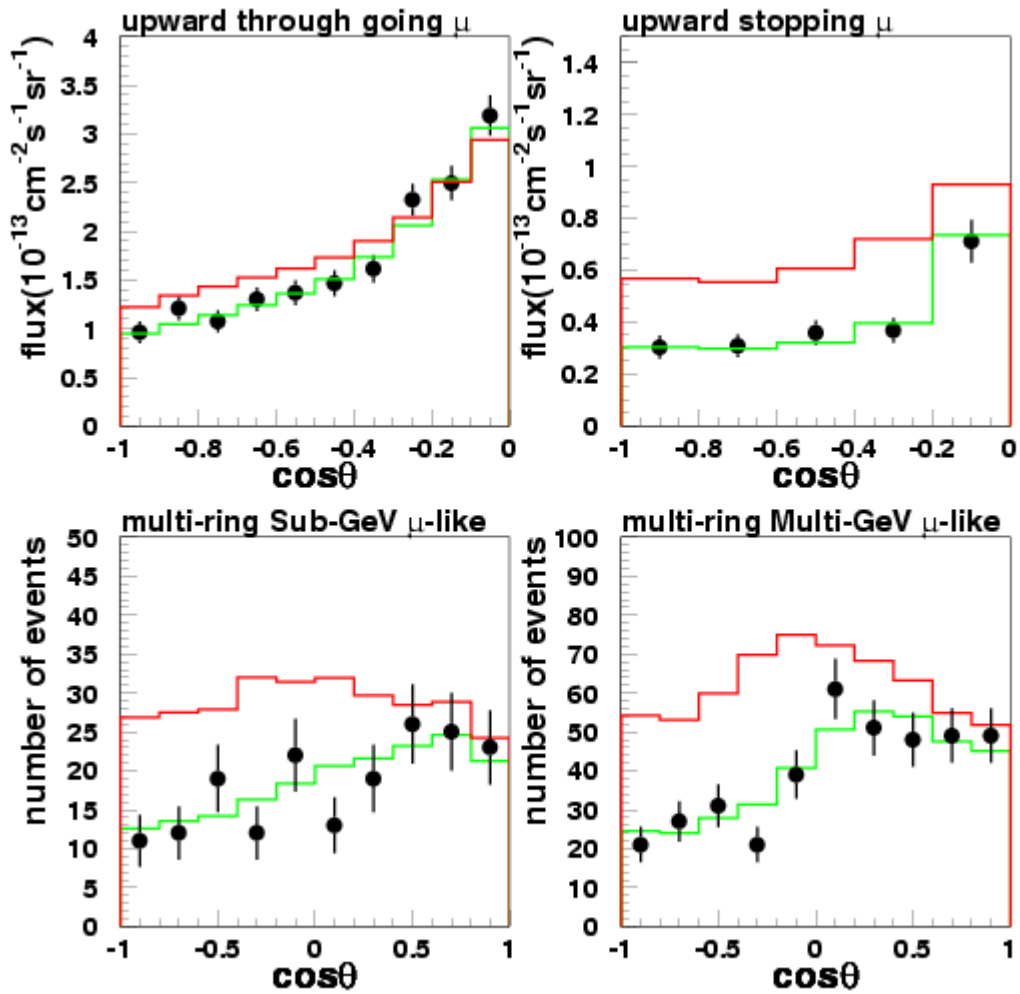
Zenith angle distributions for the best fit (grand global fit)

- No oscillation
- Best fit ($\Delta m^2=2.5 \times 10^{-3} \text{eV}^2, \sin^2 2\theta=1.00$)



Zenith angle distributions for the best fit (cont) (grand global fit)

- No oscillation
- Best fit ($\Delta m^2=2.5 \times 10^{-3} \text{eV}^2$, $\sin^2 2\theta=1.00$)



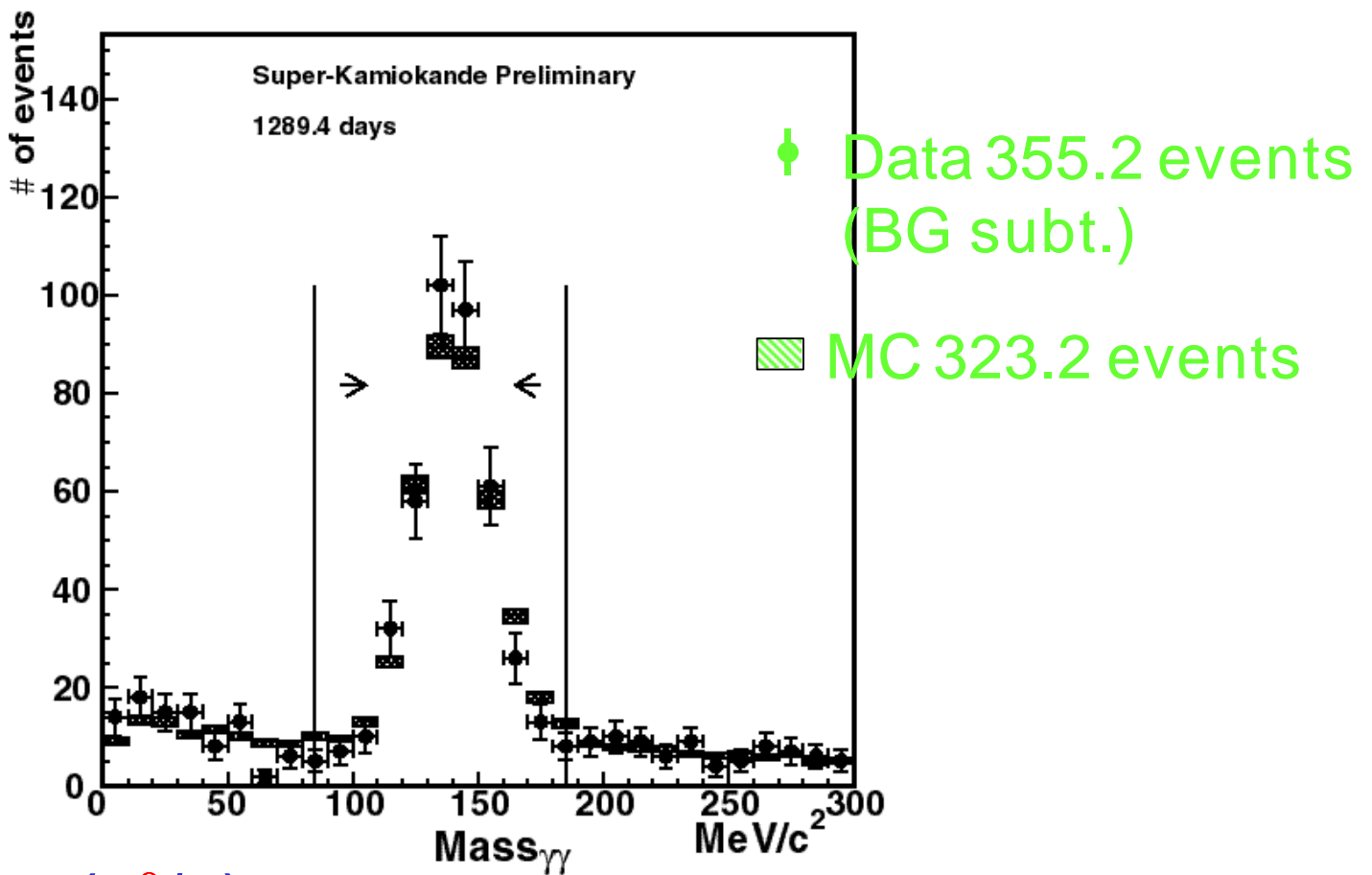
Systematics in the 1D fit

Combined Systematic Errors

		σ_i	best fit
α	Absolute Normalization Uncertainty	Free	3.4 %
δ	Ev Spectrum Index	0.05	-0.01
β_L	Sub GeV μ/e Ratio	8 %	-5.9 %
β_H	MultiGeV μ/e Ratio	12 %	-12 %
ρ	FC/PC Relative Normalization	8 %	1.1 %
η_L	Sub GeV Up/Down Asymmetry	2.4 %	-1.9 %
η_H	MultiGeV Up/Down Asymmetry	2.7 %	-0.6 %
β_1	FC+PC/Through $\uparrow\mu$ Relative Normalization	7 %	8.7 %
β_2	Through $\uparrow\mu$ /Stop $\uparrow\mu$ Relative Normalization	7 %	-0.7 %
	FC+PC Horizontal/Vertical Uncertainty	4 %	0.2 %
	$\uparrow\mu$ Horizontal/Vertical Uncertainty	3 %	0.2 %
	L/E Uncertainty	15 %	-2.5 %
	Mult-ring/1 ring (Sub-GeV) Relative Normalization	Free	-14.1 %
	Mult-ring/1 ring (Multi-GeV) Relative Normalization	Free	-15.7 %

$\nu_{\mu} \rightarrow \nu_{\text{sterile}}$ (π^0 method)

$$\frac{(\pi^0/\mu)_{\text{Data}}}{(\pi^0/\mu)_{\text{MC}}} \begin{cases} > 1 \text{ for } \nu_{\mu} \rightarrow \nu_{\tau} \\ \approx 1 \text{ for } \nu_{\mu} \rightarrow \nu_s \end{cases}$$

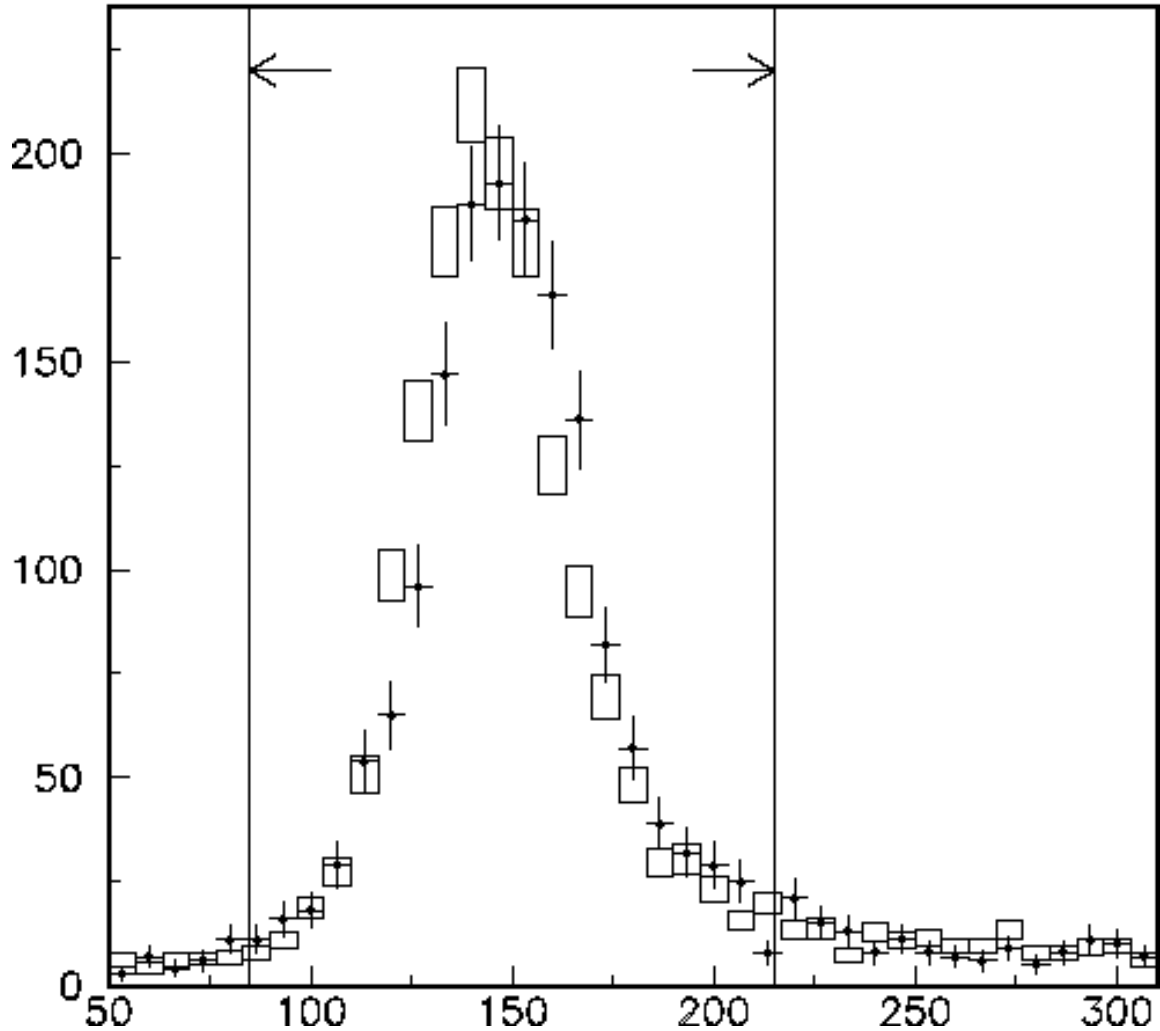


$$\frac{(\pi^0/\mu)_{\text{Data}}}{(\pi^0/\mu)_{\text{MC}}} = 1.49 \pm 0.08(\text{stat.}) \pm 0.11(\text{sys.})$$

Experimental only

π^0 info from K2K-1kt

Invariant Mass of 2R e-like

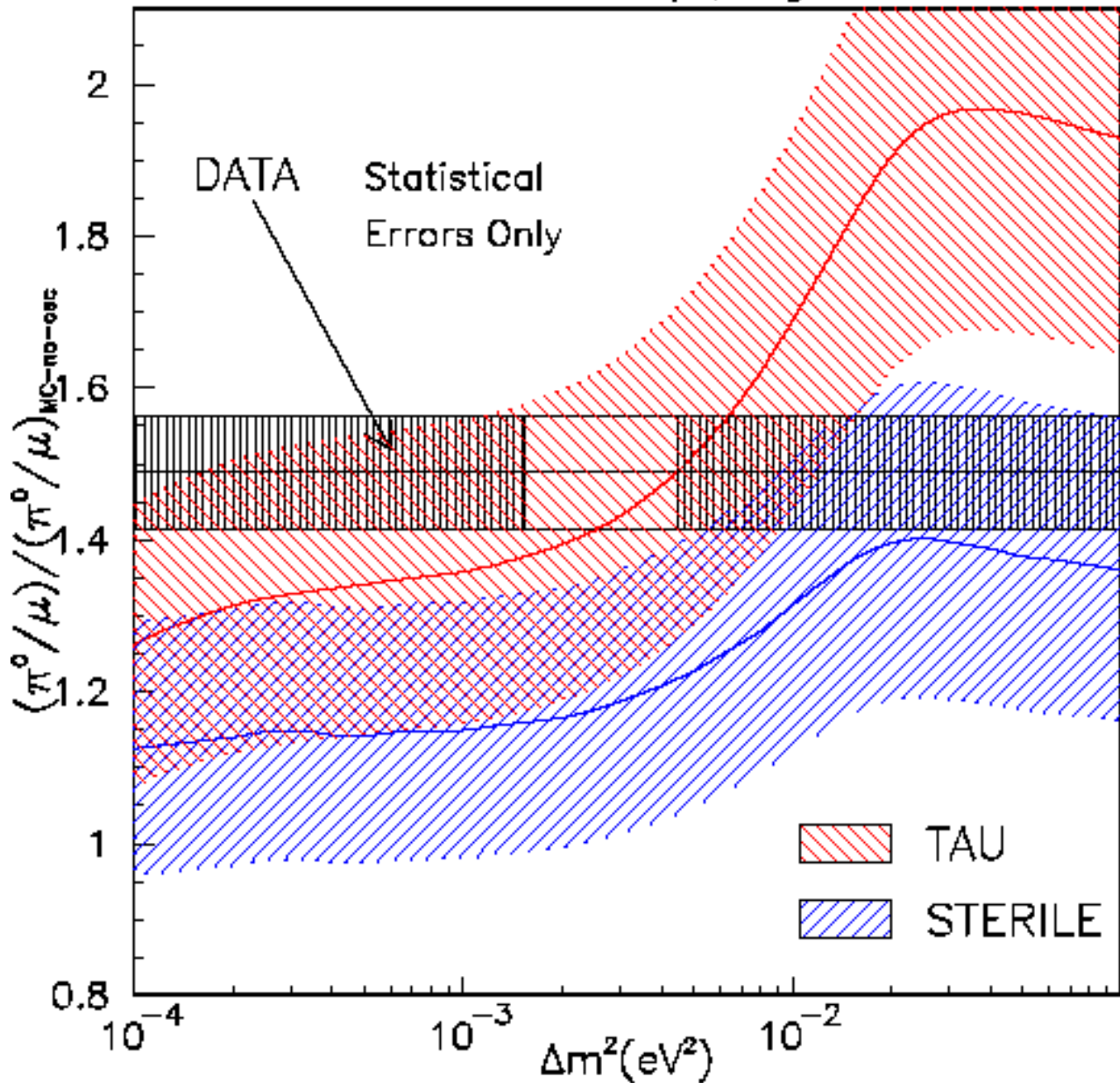


$$\frac{\left(\frac{\pi^0}{\text{FC-}\mu} \right)_{\text{data}}}{\left(\frac{\pi^0}{\text{FC-}\mu} \right)_{\text{MC}}} = \underline{0.99 \pm 0.03 \pm 0.1}$$

PRELIMINARY

$(\pi^0/\mu)_{\text{data}}$ VS $(\pi^0/\mu)_{\text{MC-no-osc}}$

Current $R\pi^0 \nu_\tau, \nu_s$ Cases



PRELIMINARY

$\nu_{\mu} \rightarrow \nu_{\text{sterile}}$ (matter in earth)

Using matter effect and enriched NC sample

$\nu_{\mu} \rightarrow \nu_{\tau}$: No matter effect

$\nu_{\mu} \rightarrow \nu_s$: With matter effect

Neutrino oscillation in matter:

$$\begin{pmatrix} \nu_{\mu} \\ \nu_s \end{pmatrix} = \begin{pmatrix} \cos\theta_m & \sin\theta_m \\ -\sin\theta_m & \cos\theta_m \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

$$\sin^2 2\theta_m = \frac{\sin^2 2\theta}{(\zeta - \cos 2\theta)^2 + \sin^2 2\theta}$$

$$\zeta = -\sqrt{2} G_F n_n E_{\nu} / \Delta m^2$$

$$\text{For } \sin^2 2\theta \sim 1 \quad \sin^2 2\theta_m \sim \frac{1}{\zeta^2 + 1}$$

And for $E_{\nu} = 30 \sim 100 \text{ GeV} \rightarrow \zeta \gg 1$ and
 $\sin^2 2\theta_m \ll 1$

Suppression !

Strategy:

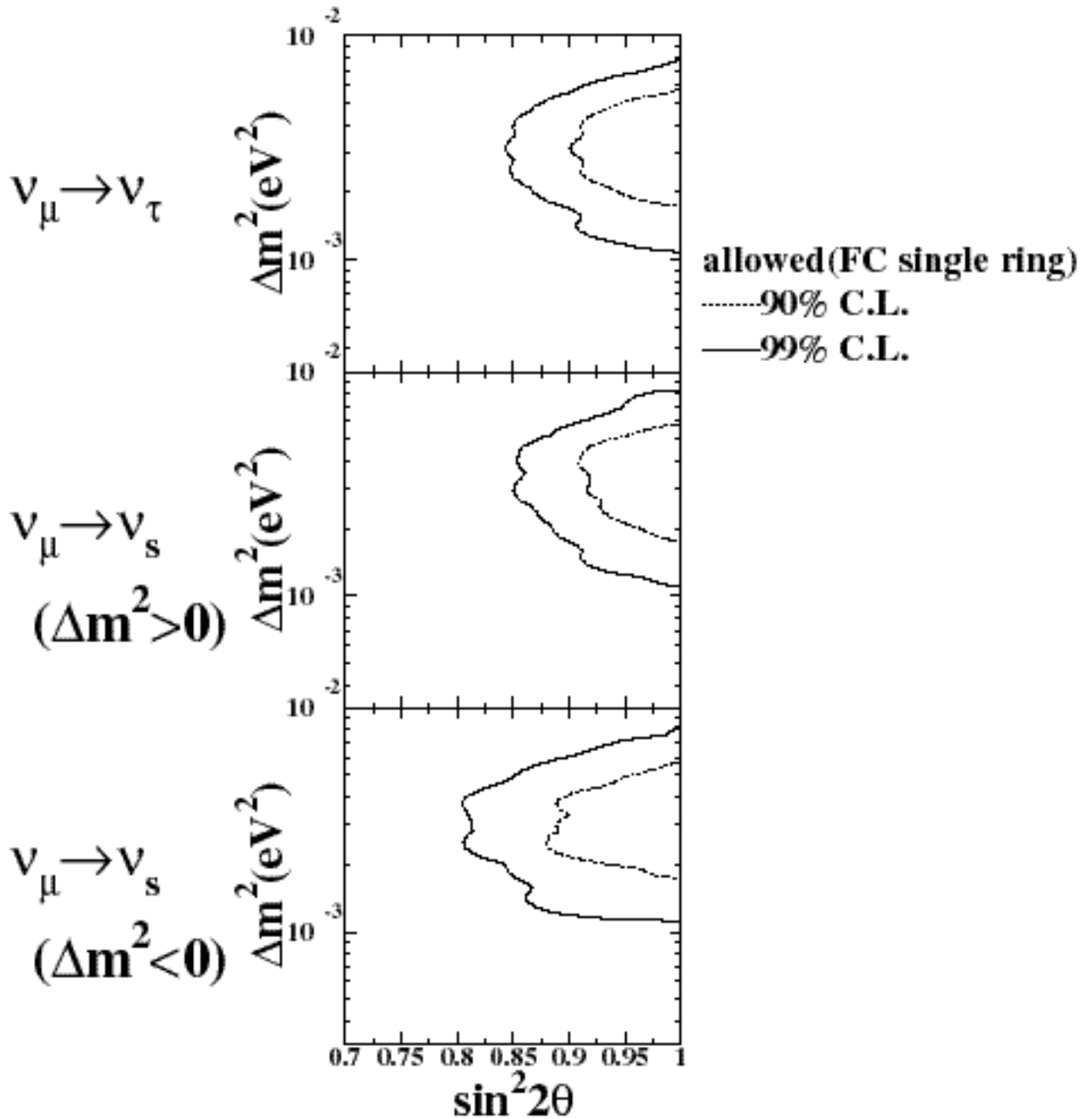
Obtain allowed region using lower energy events (Fully contained sample)

Then,

Test zenith angle of NC enriched events, high energy PC and through-going muon events.

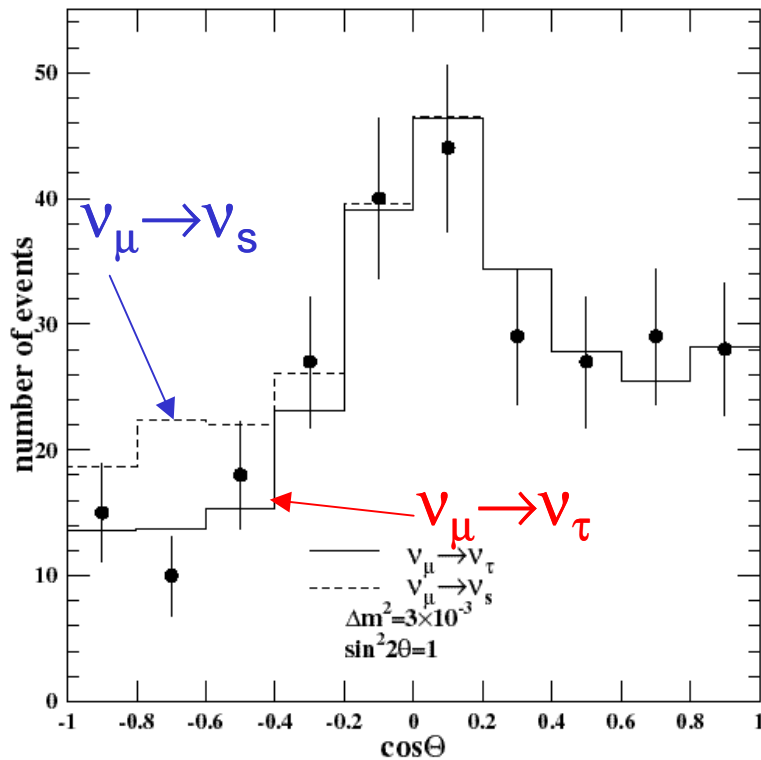
Allowed region using only FC events

allowed region from FC single-ring analysis



Zenith angle of high energy PC events

zenith angle distribution of high E ($E_{vis} > 5 \text{ GeV}$) PC events (1144 days)

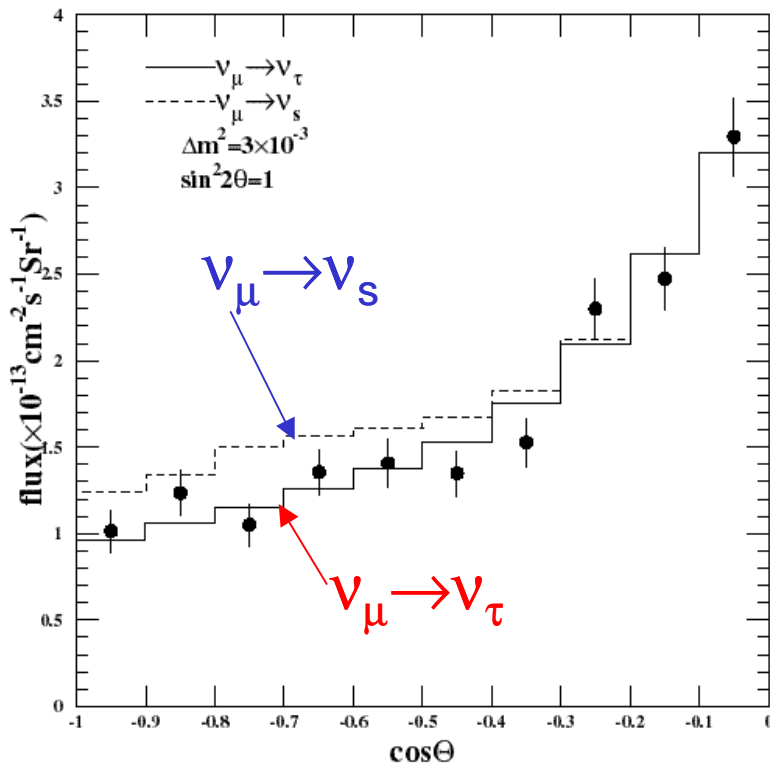


> 45000 p.e.
($E > \sim 5 \text{ GeV}$)
 $\langle E \rangle \sim 25 \text{ GeV}$

$\Delta m^2 = 3 \times 10^{-3} \text{ eV}^2$
 $\sin^2 2\theta = 1$

Zenith angle of upward-going muon

zenith angle distribution of upward through going μ events (1138 days)



$\Delta m^2 = 3 \times 10^{-3} \text{ eV}^2$
 $\sin^2 2\theta = 1$

Zenith angle of NC enriched events

Criteria

> 400 MeV visible energy

Multi-ring event

e-like ring is the most energetic ring

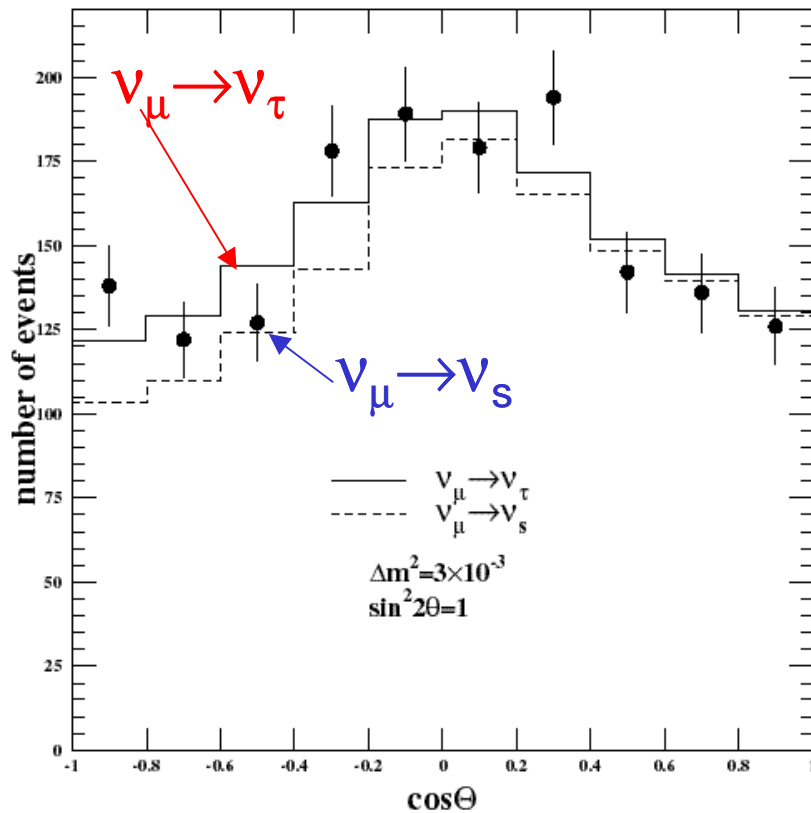
Contents

NC : 29 %

ν_e CC : 46 %

ν_μ CC : 25 %

zenith angle distribution of N.C. enriched multi-ring events (1144days)

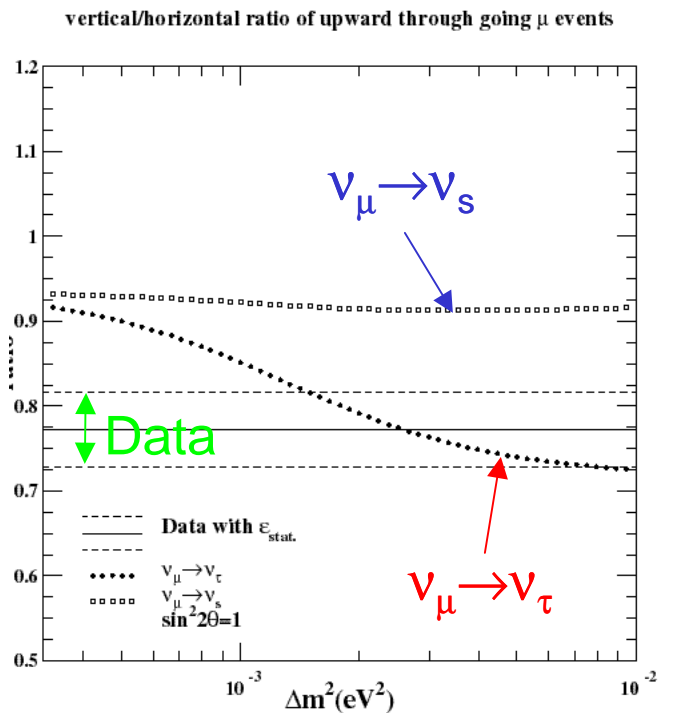
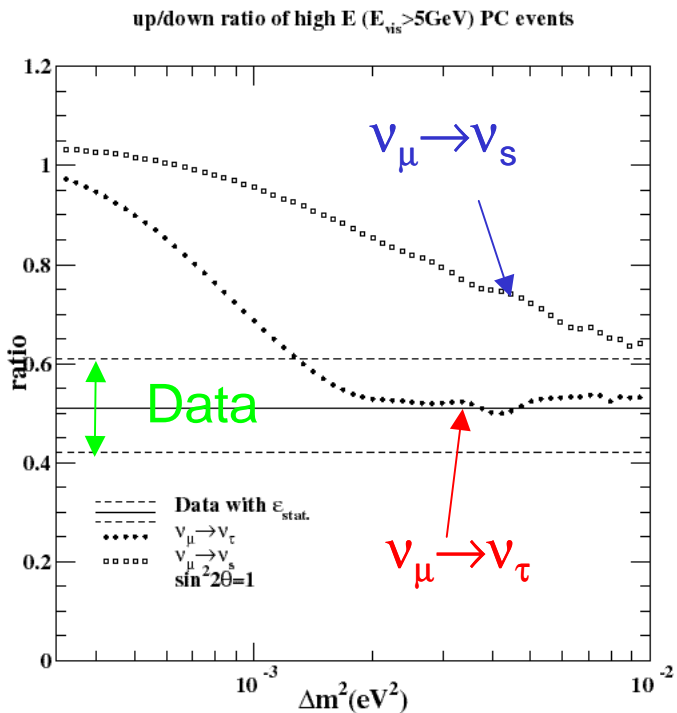
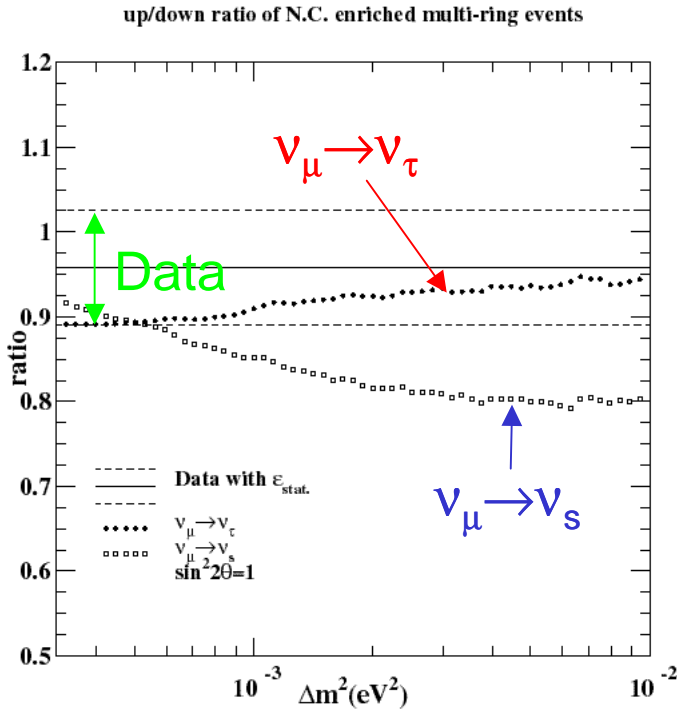


$$\Delta m^2 = 3 \times 10^{-3} \text{ eV}^2$$
$$\sin^2 2\theta = 1$$

Ratios vs. Δm^2

$\sin^2 2\theta = 1$

Up/Down ($\cos\Theta \leq -0.4$)
 ≥ 0.4)
 ratio of NC enriched
 multi-ring



Up/Down ($\cos\Theta \leq -0.4$)
 ≥ 0.4)
 ratio of High Energy PC

Vertical/Horizontal ratio
 ($\cos\Theta \gtrsim -0.4$) of up muons

10^{-3}

10^{-2} eV^2

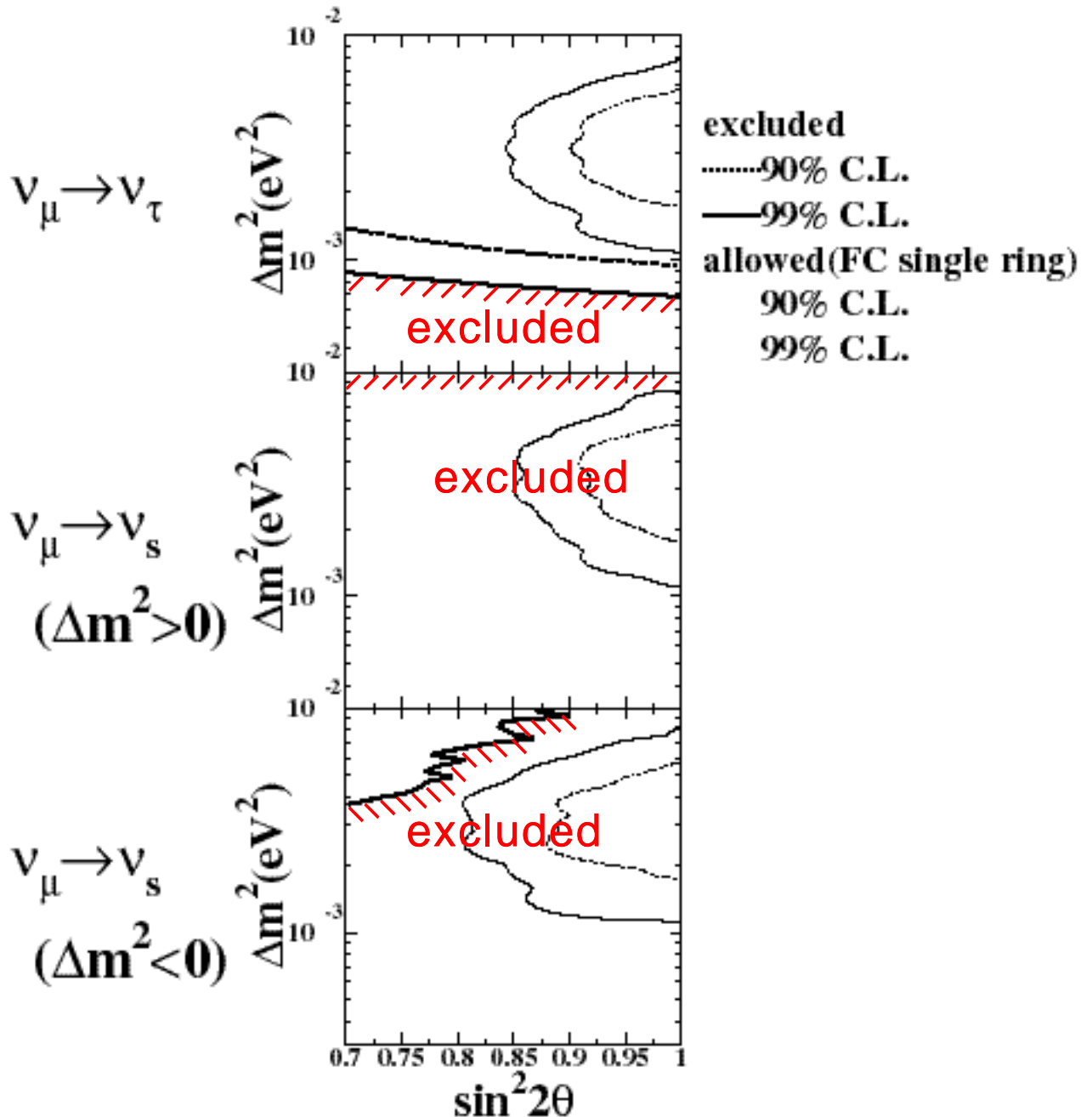
10^{-3}

10^{-2} eV^2

Allowed vs. excluded regions

combine NC enriched, high E PC and up muons

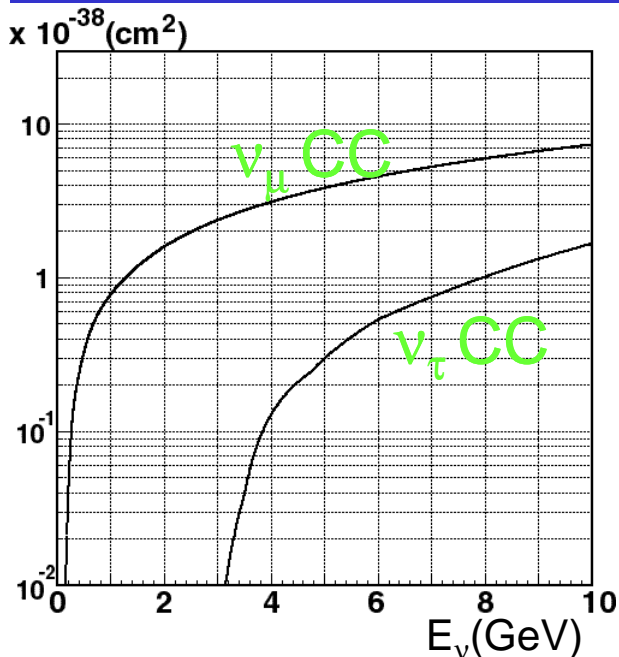
excluded region from combined analysis(multi+PC+up μ)



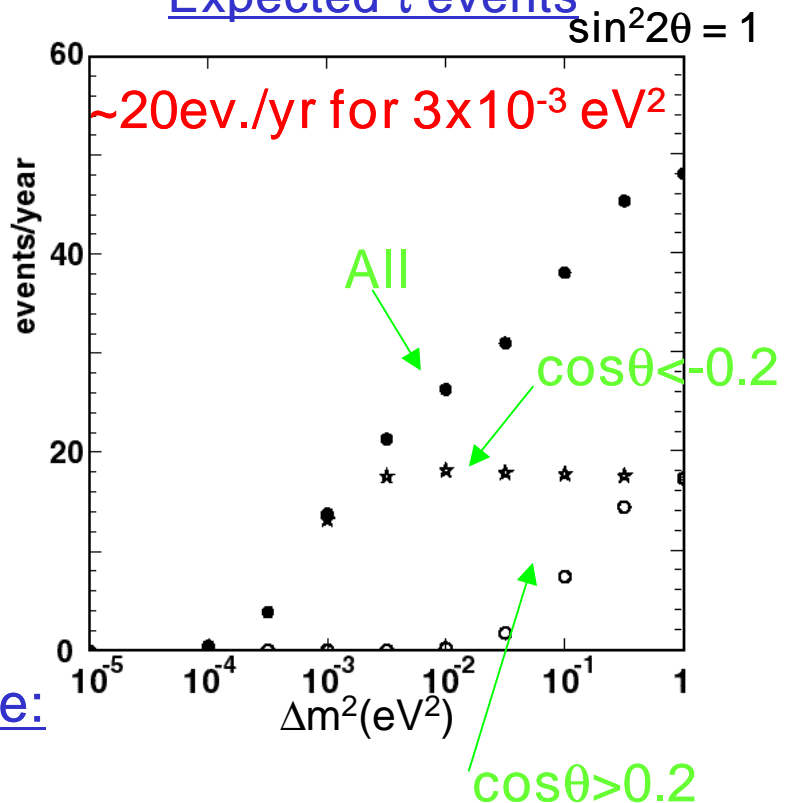
$\nu_\mu \rightarrow \nu_s$ is excluded with 99 % C.L.

Search for τ leptons

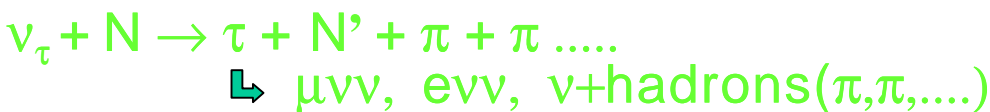
Neutrino CC cross sections



Expected τ events



Signature of τ appearance:



- Higher multiplicity of Cherenkov rings
- More $\mu \rightarrow e$ decay signals
- More spherical event pattern

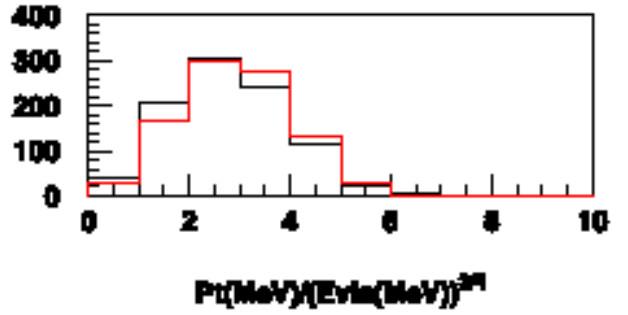
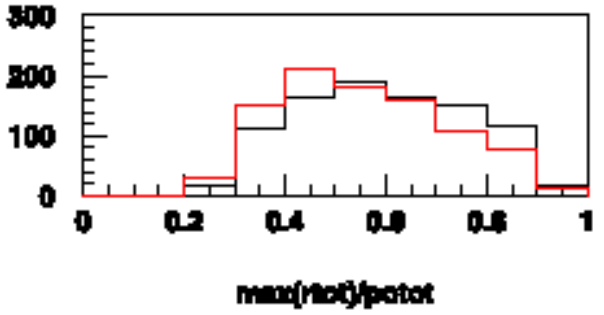
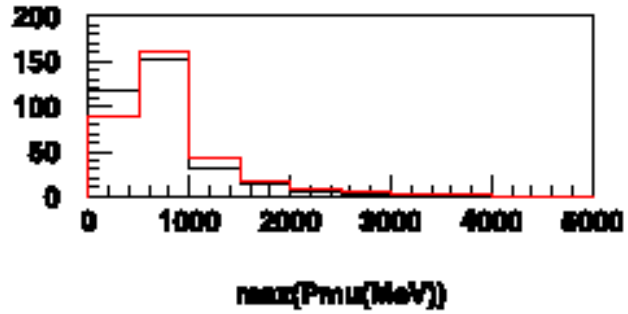
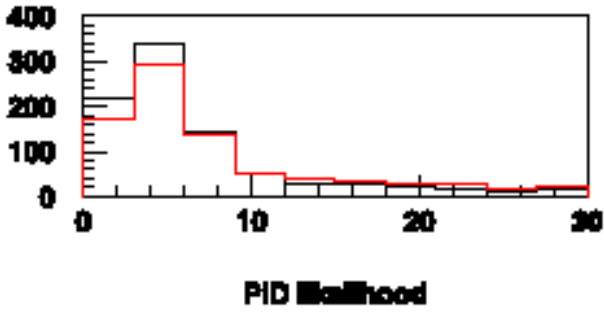
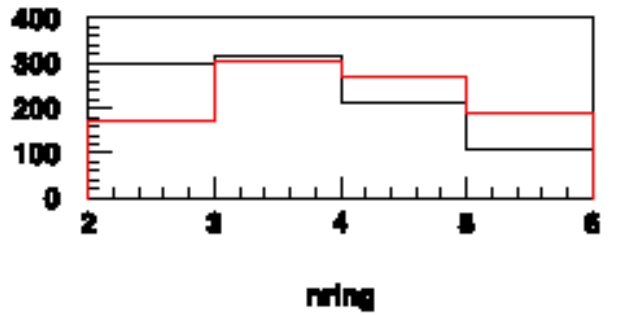
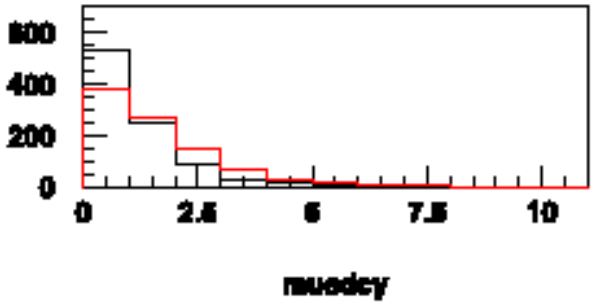
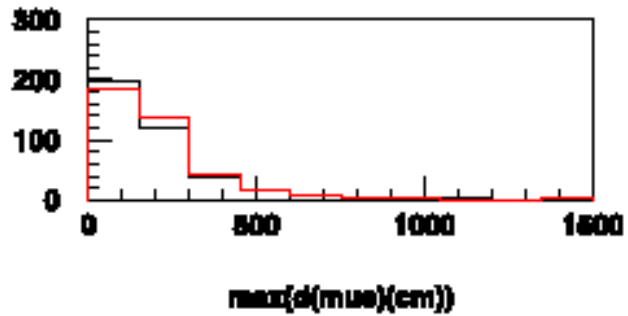
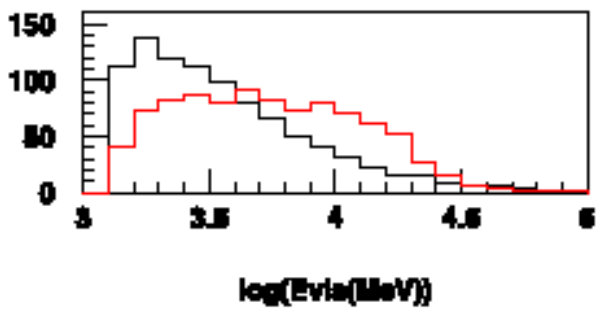
Search for τ appearance (3 methods) :

- (1) Energy flow and event shape analysis
- (2) Likelihood method using # of rings, $\mu \rightarrow e$, max p.e. ring and etc.
- (3) Neural network method

Each method is optimized using only downward going events and then looks at upward going events. (I.e. blind method to disable systematic bias.)

Multi-ring samples

— : atm $\nu_\mu + \nu_e$ w/o ν_τ
— : ν_τ CC



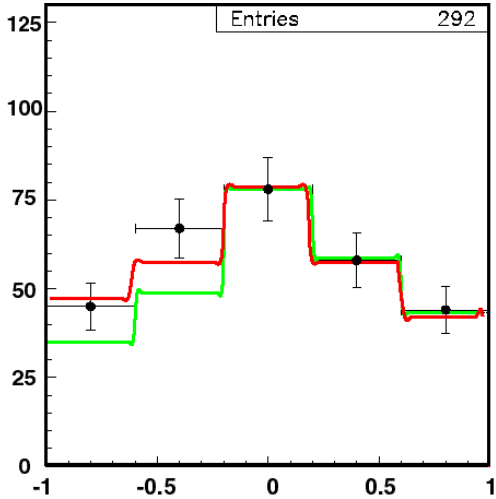
Zenith-angle distribution

— MC without τ

— MC with τ

$\Delta m^2 = 3 \times 10^{-3} \text{eV}^2, \sin^2 2\theta = 1.00$

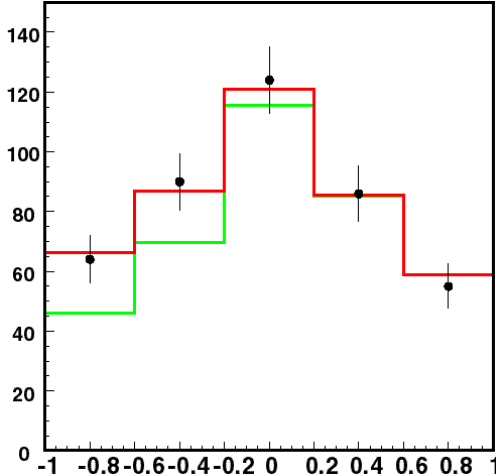
(expected # of τ : 74 events)



Energy flow method

Observed # of τ : 25.5 $^{+14}_{-13}$
Efficiency for τ : 32 %

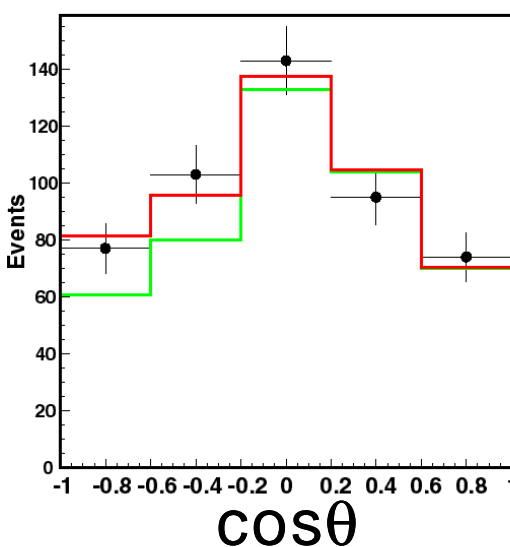
of τ production: 79 $^{+44}_{-40}$



Likelihood method

Observed # of τ : 27 $^{+17}_{-16}$ $^{+9}_{-8}$
Efficiency for τ : 43.5 %

of τ production: 62 $^{+39}_{-27}$ $^{+21}_{-18}$



Neural network method

Observed # of τ : 42 ± 19 $^{+13}_{-13}$
Efficiency for τ : 45 %

of τ production: 92 ± 35.3 $^{+14}_{-0}$

All methods show $\sim 2\sigma$ excess of τ -like events.
The result is consistent with $\nu_\mu \rightarrow \nu_\tau$ oscillations.

Probability of exotic oscillation models

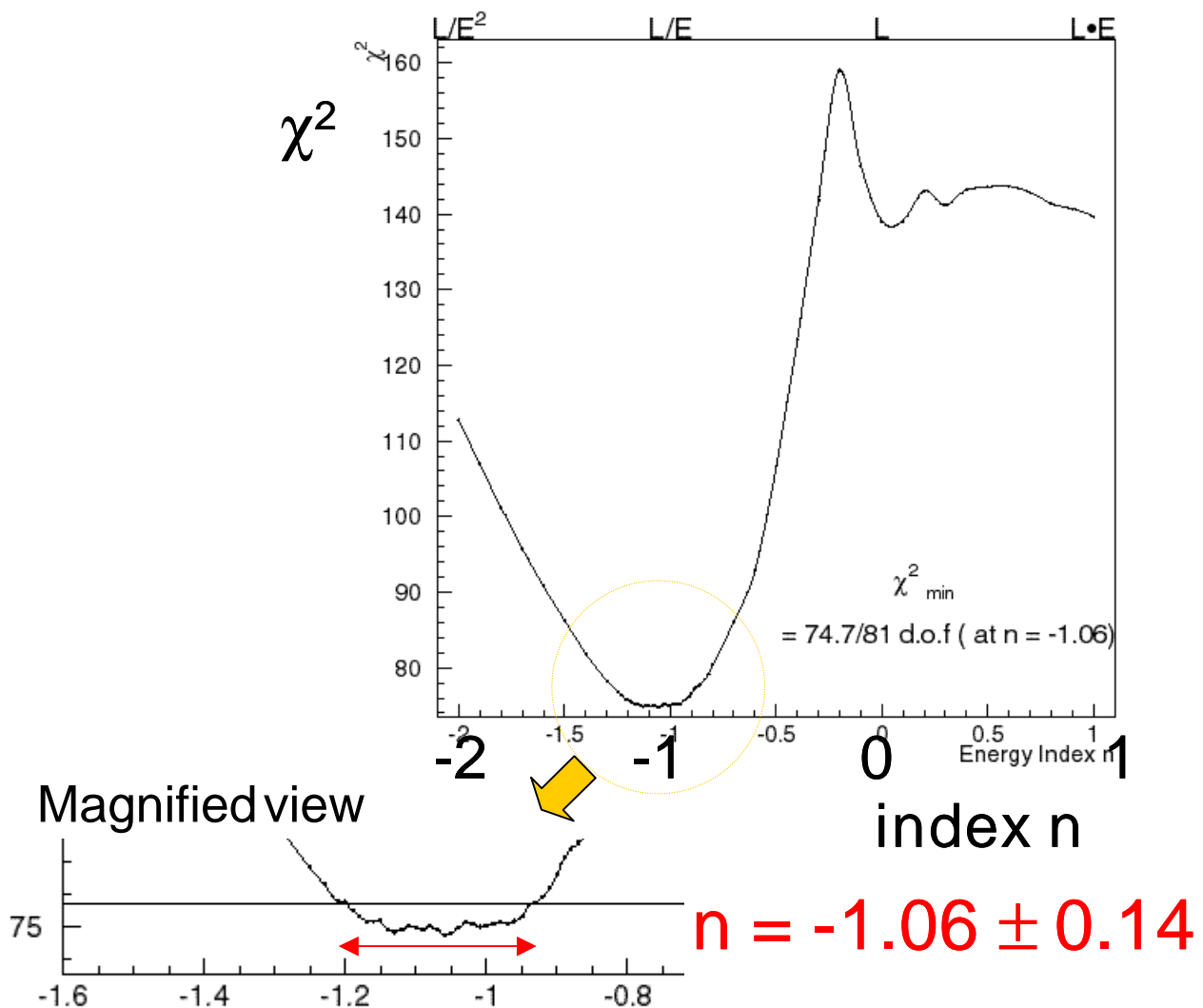
Test $\nu_\mu \rightarrow \nu_\tau$ oscillation with :

$$P(\nu_\mu \rightarrow \nu_\tau) = \sin^2 2\theta \sin^2(\beta L \times E^n)$$

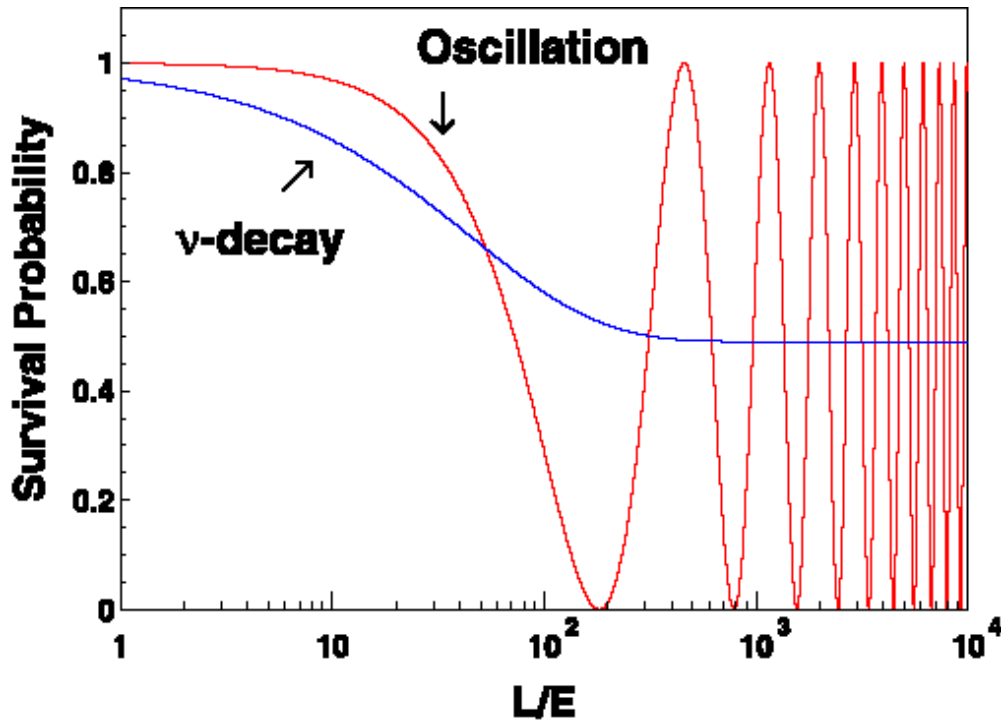
(θ, β, n : parameters)

$n = -1$ is the standard neutrino oscillation

Use FC, PC, Up-through, and Up-stop data



Neutrino decay



Let neutrinos oscillate and decay $\nu_3 \rightarrow X(\text{invis})$;

$$P(\nu_\mu \rightarrow \nu_\mu) = \sin^4\theta + \cos^4\theta \exp\left(-\frac{m_3}{\tau_3} \frac{L}{E}\right) + \sin^2\theta \exp\left(-\frac{m_3}{2\tau_3} \frac{L}{E}\right) \cos\left(\frac{\Delta m^2 L}{2E}\right)$$

Consider two cases;

$\lambda_{\text{dcy}} \gg \lambda_{\text{osc}}$, and $\lambda_{\text{dcy}} \ll \lambda_{\text{osc}}$,

where

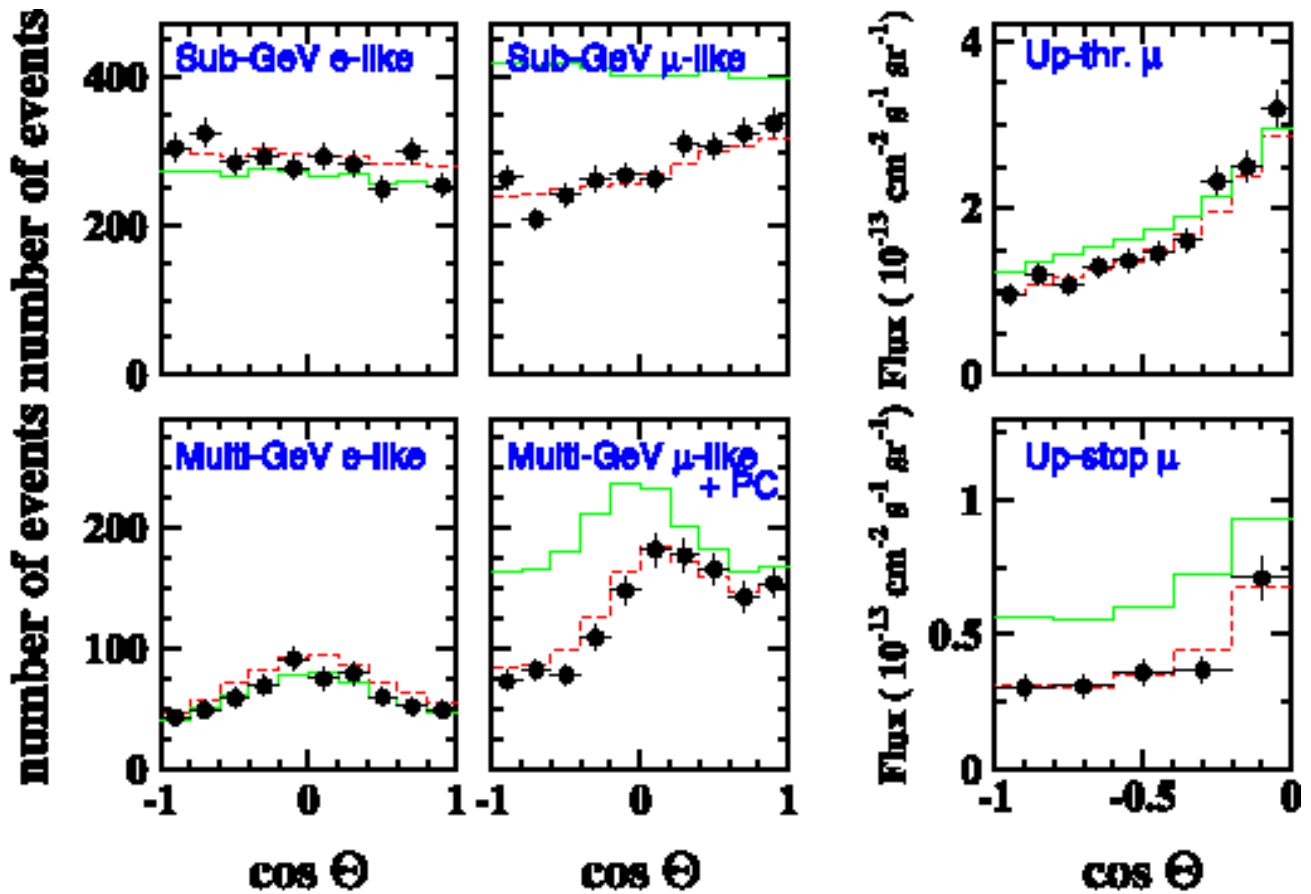
$$\lambda_{\text{dcy}} = \frac{\tau_3 E}{m_3}, \quad \lambda_{\text{osc}} = \frac{4\pi E}{\Delta m^2}$$

$\lambda_{dcy} \gg \lambda_{osc}$

For $\Delta m^2 \rightarrow \infty$,

$$\chi^2_{\min} = 221.2/153 \text{ dof}$$

Bad fit !



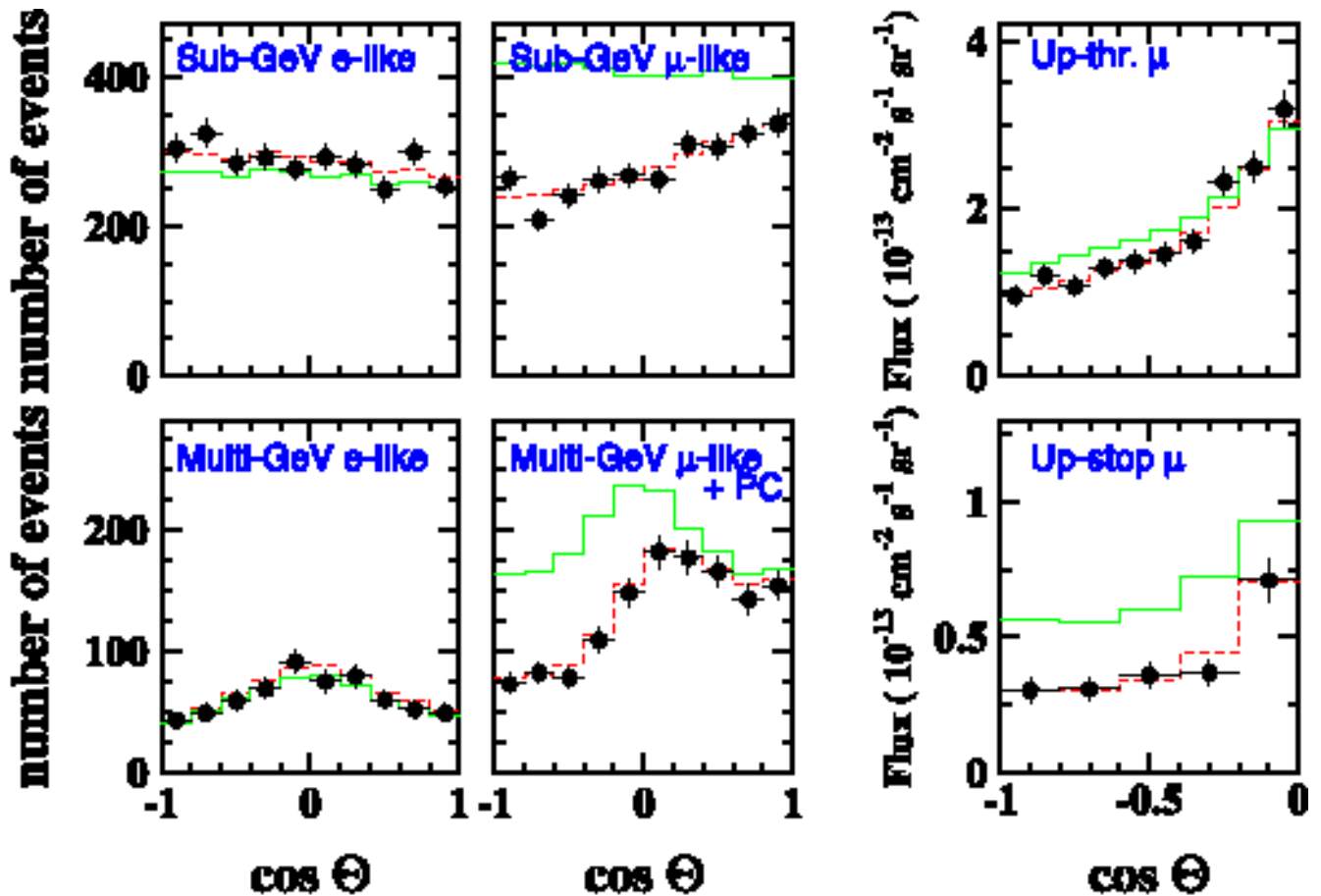
$$\underline{\lambda_{dcy} \ll \lambda_{osc}}$$

For $\Delta m^2 \rightarrow 0$,

$$\chi^2_{\min} = 147.1/153 \text{ dof}$$

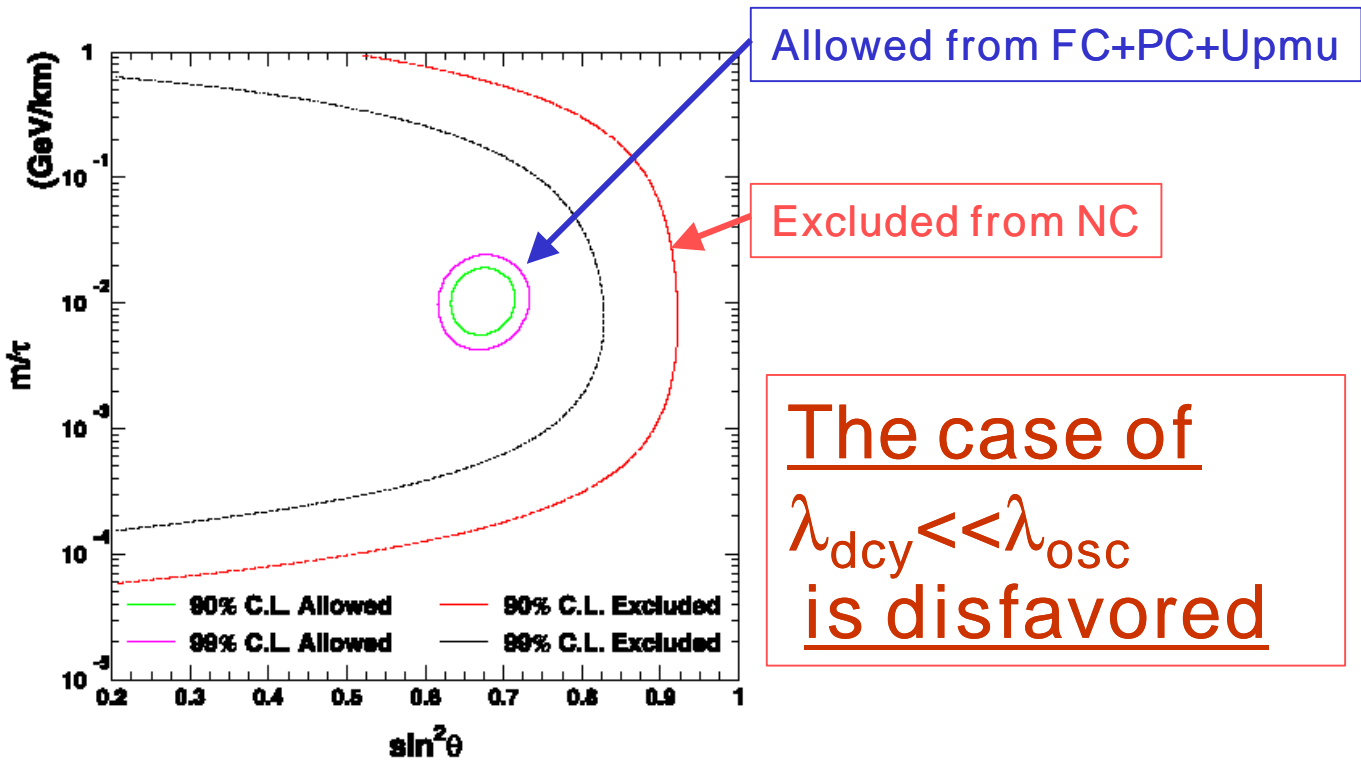
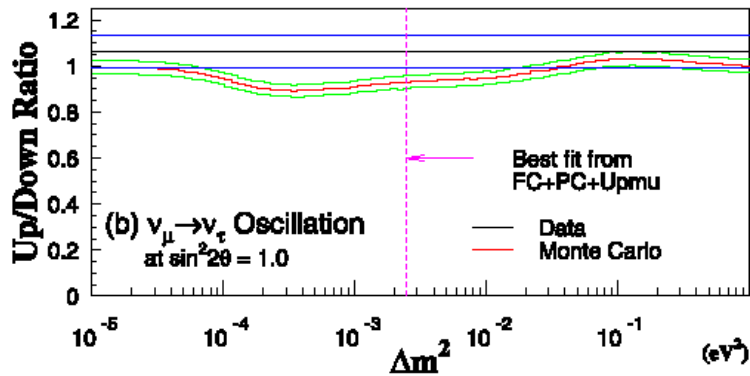
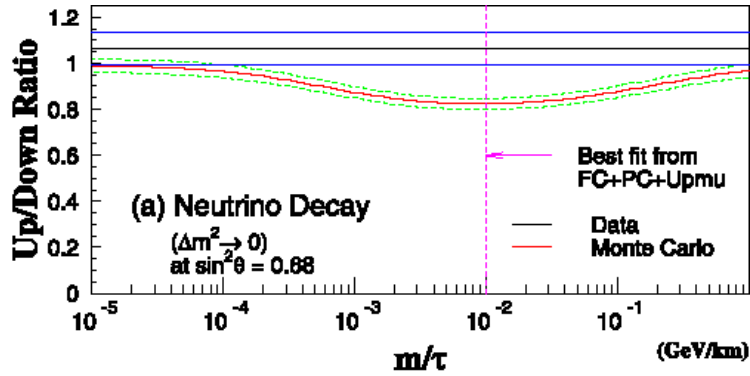
$$\text{at } (\sin^2\theta, m_3/\tau_3) = (0.68, 0.01 \text{ (GeV/km)})$$

Good fit !



Up/down of NC enriched events (short λ_{dcy})

FC, Nring>1, Evis>400MeV, Brightest ring = e-like



Conclusions on atmospheric neutrinos

- Oscillation parameters for $\nu_\mu \rightarrow \nu_\tau$:
 $\Delta m^2 = 1.7 \sim 4 \times 10^{-3} \text{ eV}^2$, $\sin^2 2\theta > 0.89$
(90%CL)
- 3D flux does not change the conclusion but more precise 3D calculations are needed
- $\nu_\mu \rightarrow \nu_s$ is strongly disfavored
- π^0/μ ratio is consistent with $\nu_\mu \rightarrow \nu_\tau$
- Excess from τ leptons $\sim 2\sigma$
- Decay senario is disfavored with $> 2\sigma$
for $\lambda_{\text{dcy}} \gg \lambda_{\text{osc}}$ and $\lambda_{\text{dcy}} \ll \lambda_{\text{osc}}$