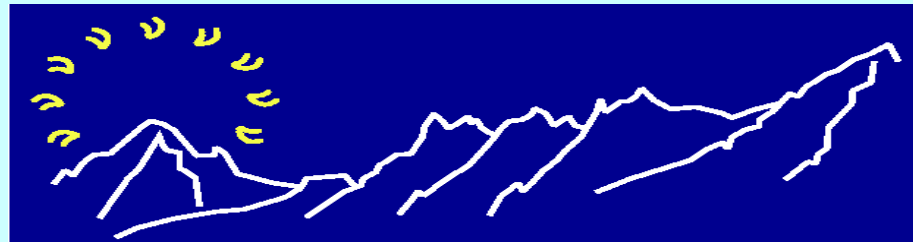


ATMOSPHERIC NEUTRINO PRODUCTION

Teresa Montaruli



Bari University and INFN



**Special thanks to G. Battistoni, A. Ferrari, P. Sala,
P. Lipari, T.K. Gaisser, T. Stanev and M. Honda**

Les Houches, 18-22 June 2001 - Neutrino Masses and Mixings

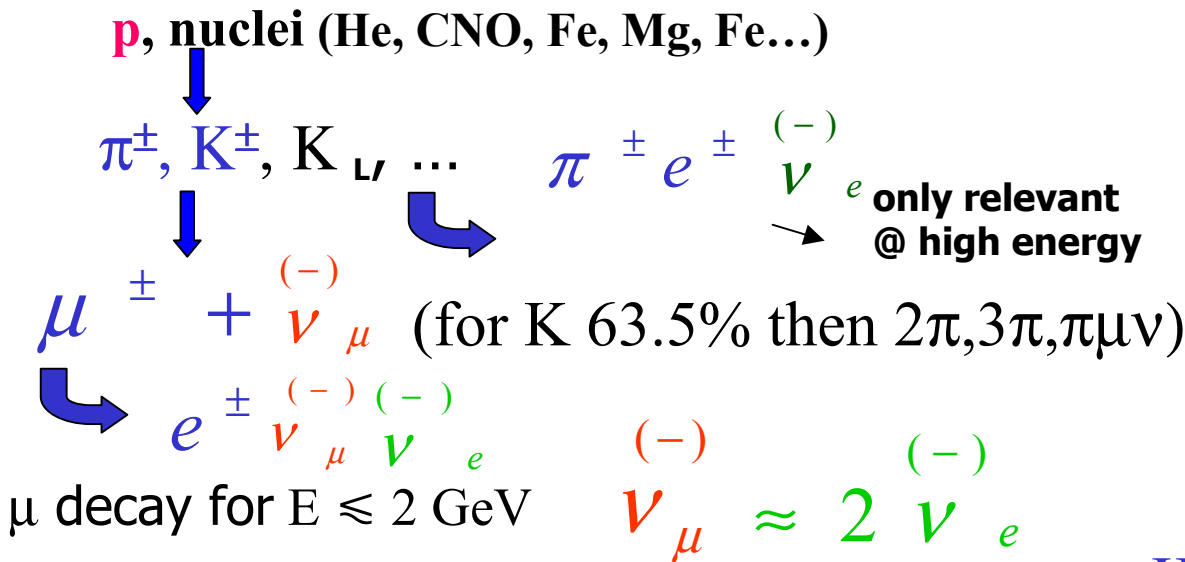
Outline

- Atmospheric neutrino results (SK, MACRO, Soudan2) are explained by new physics (oscillations into active or sterile ν , ν decay, FCNC, ...)
- Almost model-independent quantities have been singled out:
flavor ratio and asymmetry 
zenith angular flux shape 
- Atmospheric ν study requires investigations on interaction models, primary cosmic rays and other secondary spectra, geomagnetic field and solar modulation
- **Warning:** not man made ν source \Rightarrow high precision calculations needed
- Status of current calculations, comparison between models and data, improvements for the future
- All this work aims at answering to "How precisely can we determine Δm^2 ?"

Model independent quantities

Absolute flux normalization still uncertain (20-30%) level but model independent quantities:

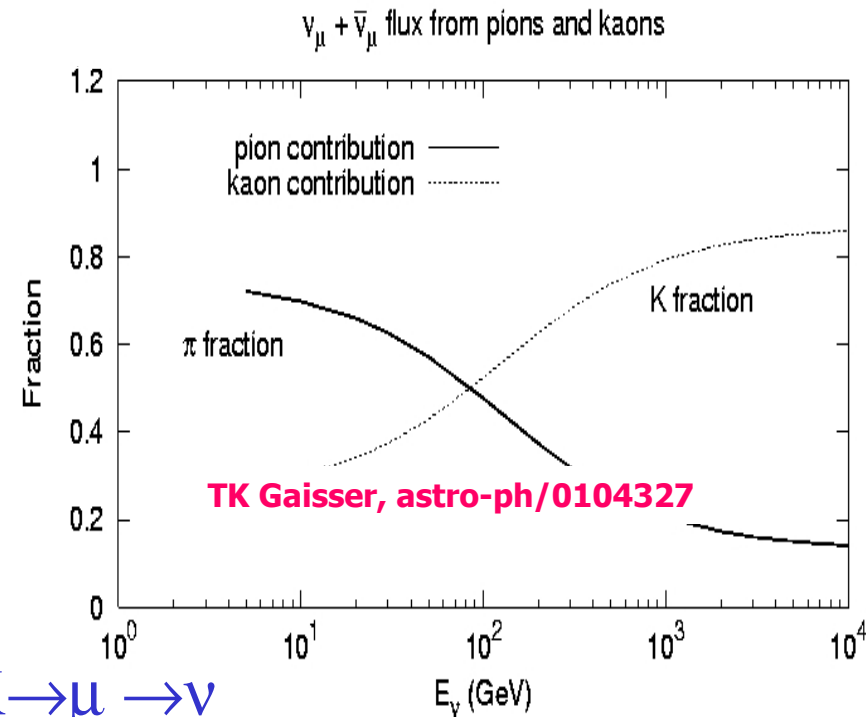
- Up/Down symmetry far from geomagnetic effects $E_\nu \gtrsim 2 \text{ GeV}$
- Flavor ratio (μ/e)
- Upgoing Through-going $\mu \cos\theta$ distribution and horizontal/vertical (important for $\nu_\mu \rightarrow \nu_\tau / \nu_\mu \rightarrow \nu_{\text{sterile}}$ discrimination)



$$\left\langle \frac{E_\nu}{E_\pi} \right\rangle \approx 0.213 \nu_\mu, 0.265 \bar{\nu}_\mu, 0.257 \nu_e$$

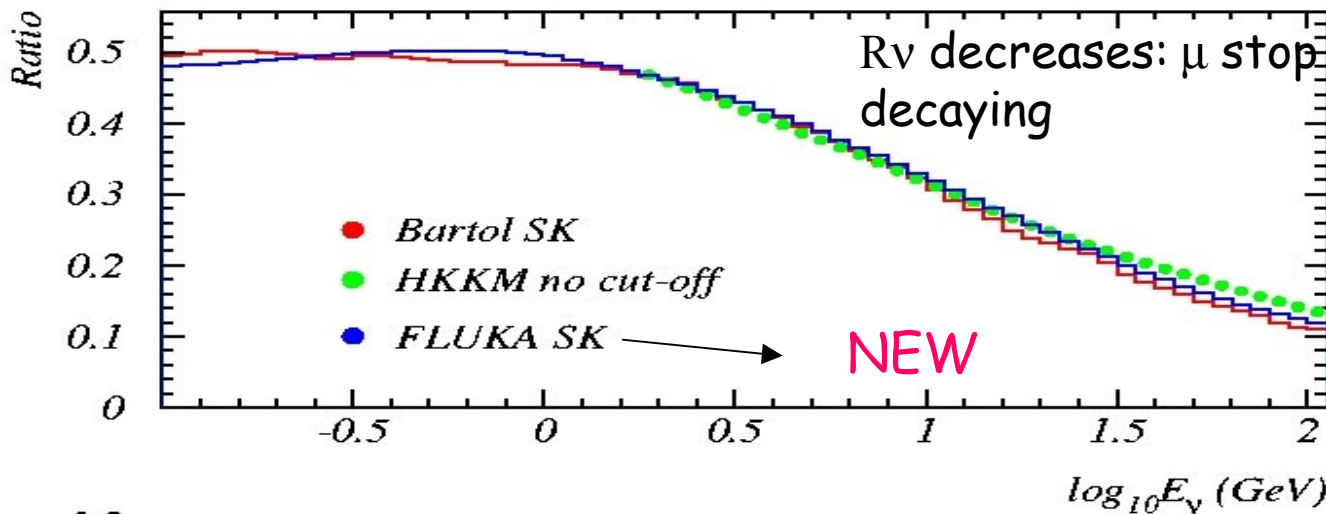


$$\left\langle \frac{E_\nu}{E_K} \right\rangle \approx 0.477 \nu_\mu, 0.159 \bar{\nu}_\mu, 0.205 \nu_e$$



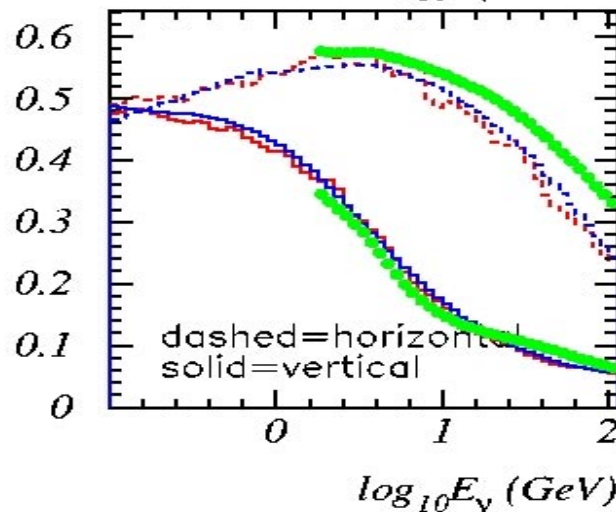
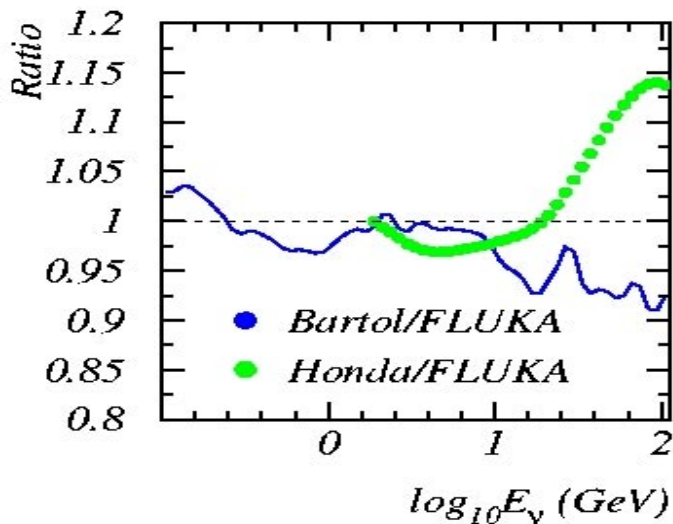
Flavor ratio comparison: $\nu_e + 1/3 \bar{\nu}_e / \nu_\mu + 1/3 \bar{\nu}_\mu$

$$(\nu_e + 1/3 \bar{\nu}_e) / (\nu_\mu + 1/3 \bar{\nu}_\mu) \text{ Solar min SK}$$



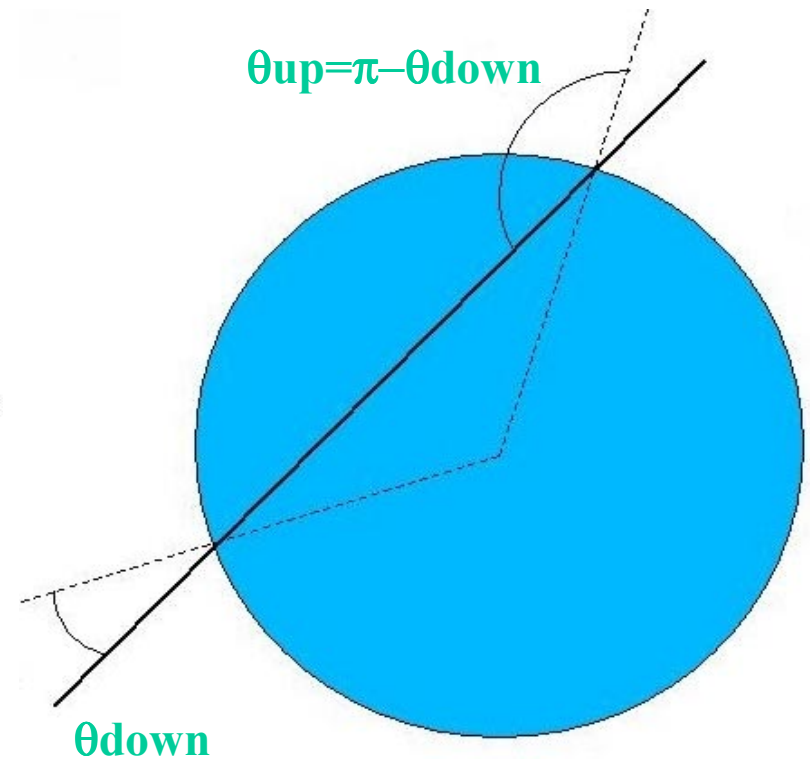
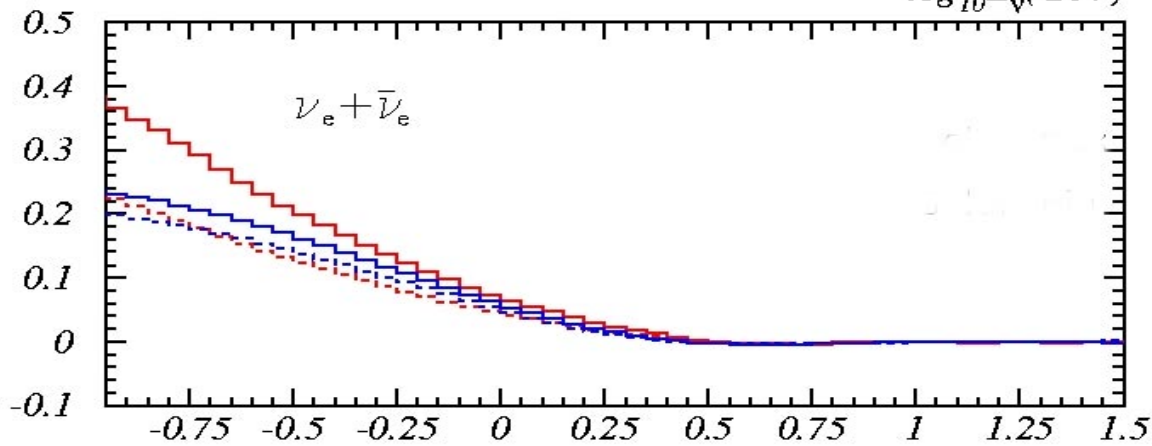
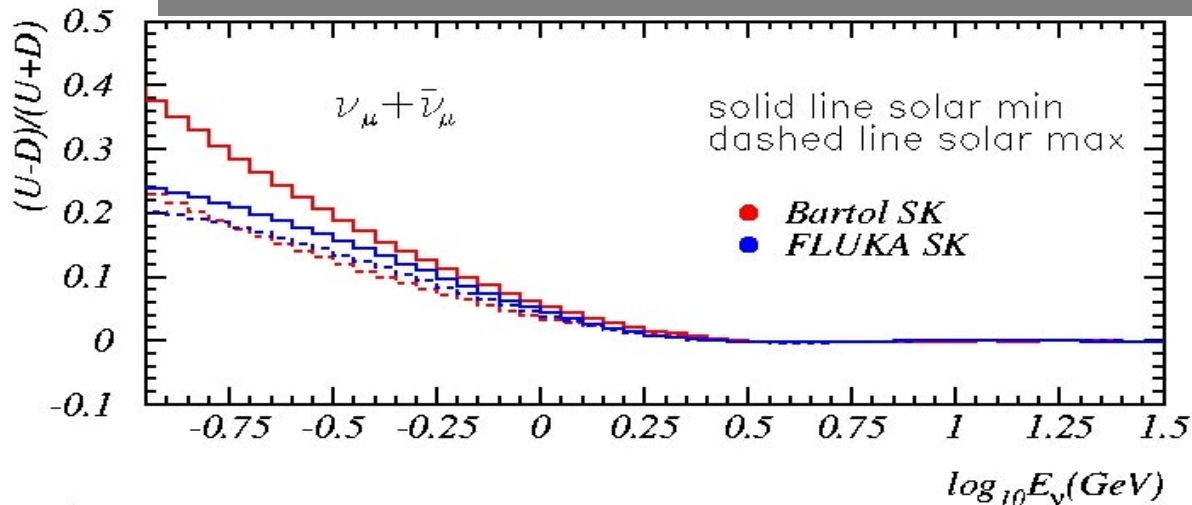
For $E_\nu < 30$ GeV
agreement $\sim 5\%$

At larger energies larger uncertainties in K physics (must be understood)



$R_\nu = e/\mu$ decreases more at vertical due to longer path at horizon available for μ decay

Up/Down Asymmetry



Earth spherical symmetry
 +CR flux isotropy \Rightarrow
 $\Phi(E\nu, \theta) = \Phi(E\nu, \pi - \theta)$

At $E_\nu \geq 2$ GeV solar modulation
 +geomagnetic effects negligible \Rightarrow
 asymmetry is model independent

Shape of the angular distribution

HE events have larger uncertainties due to:

- external **upgoing μ s** \Rightarrow no electron flavor, lower hemisphere
- flux **normalization larger uncertainty** than at lower E due to primary flux measurements and role of K decay more relevant
- **Horizontal/vertical important to discriminate active/sterile oscillations**

Uncertainties:

$$1) \delta(V/H)/(V/H) \sim 0.12 \delta(K/\pi)/(K/\pi)$$

$$L_{\text{dec}} \sim 0.75 (E(\text{GeV})/100) \text{ km (K)}$$

$$L_{\text{dec}} \sim 5.6 (E(\text{GeV})/100) \text{ km } (\pi)$$

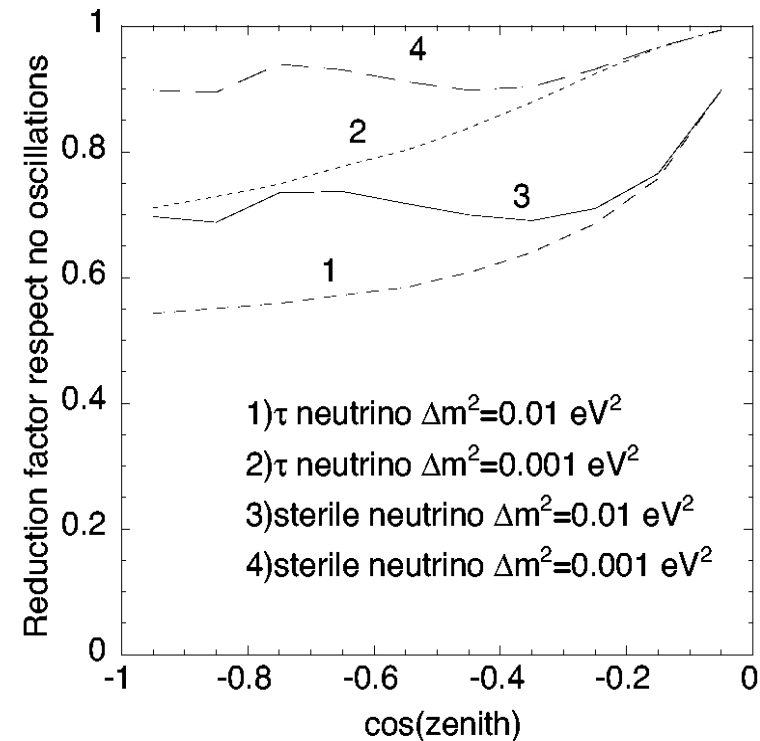
almost all K decay at $\sim 100 \text{ GeV} \Rightarrow$ almost isotropic ν contribution with θ

competition of interaction/decay for π^\pm : decay more easily at horizon for increasing energy \Rightarrow horizontal $>$ vertical flux

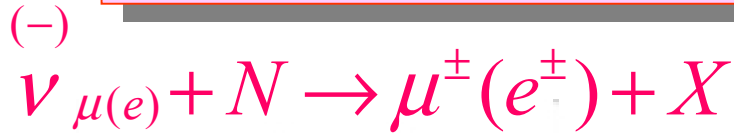
$$2) \delta(V/H)/(V/H) \sim 0.25 \delta\alpha$$

uncertainty in the slope

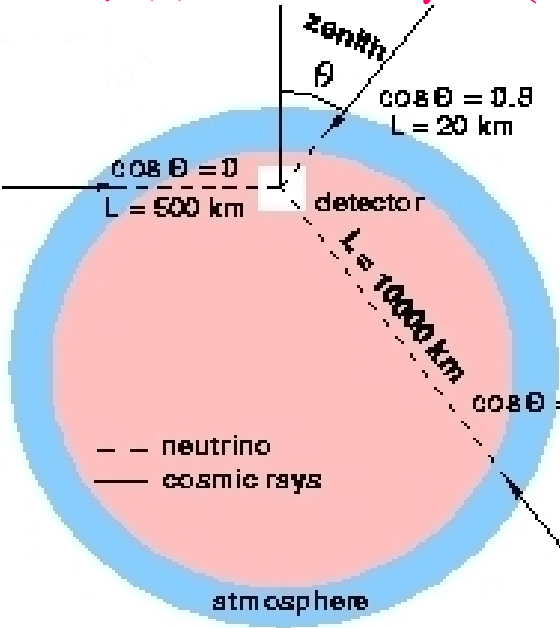
In quadrature: $\sim 3\%$ error on V/H



Atmospheric ν events

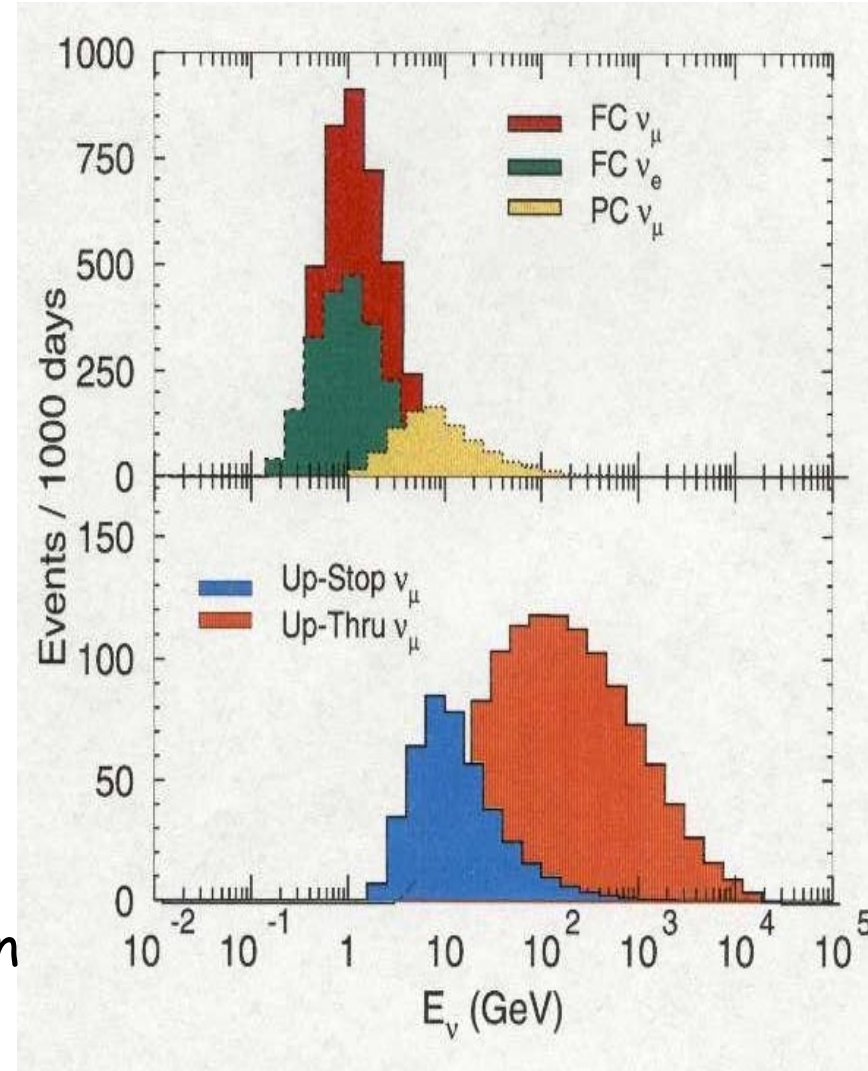


Super-Kamiokande response curves

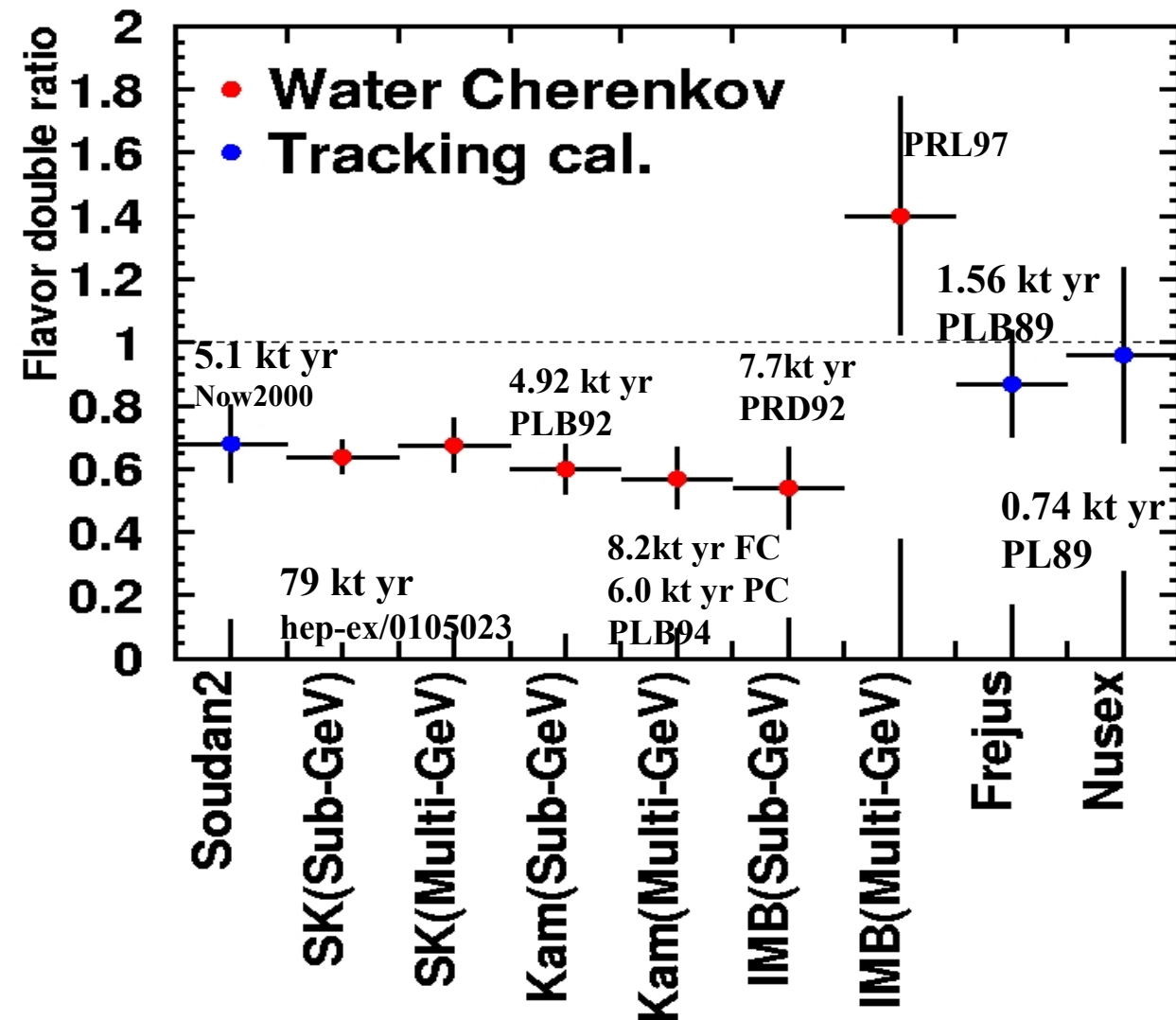


Volume events: ν CC
int. vertex inside
detectors

Surface events: through-going/stopping μ s
from external interactions
upward versus to discriminate atm μ
background; detection region increased by muon
range



Do atmospheric vs need a new physics?



Flavor ratio:

$$R = \frac{\left(\frac{\mu - \text{like}}{e - \text{like}} \right)_{DATA}}{\left(\frac{\mu - \text{like}}{e - \text{like}} \right)_{MC}}$$

μ -like (tracks): deficit

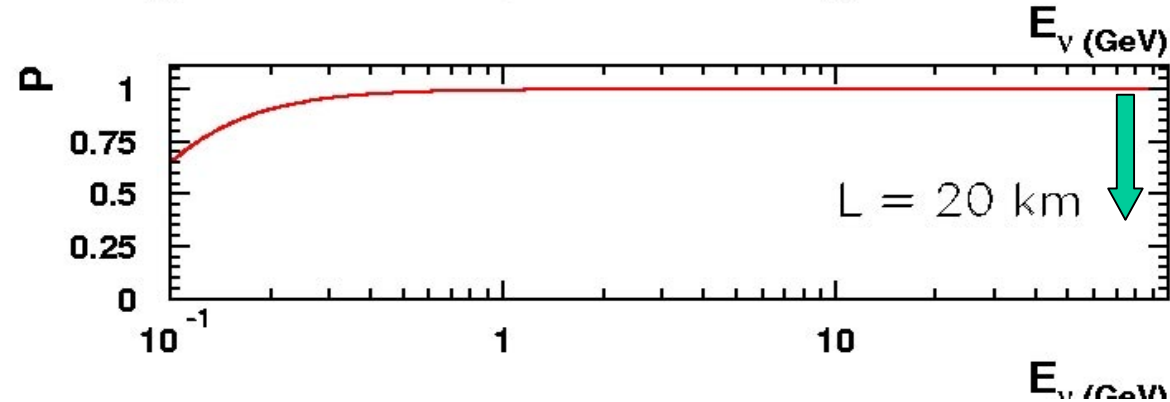
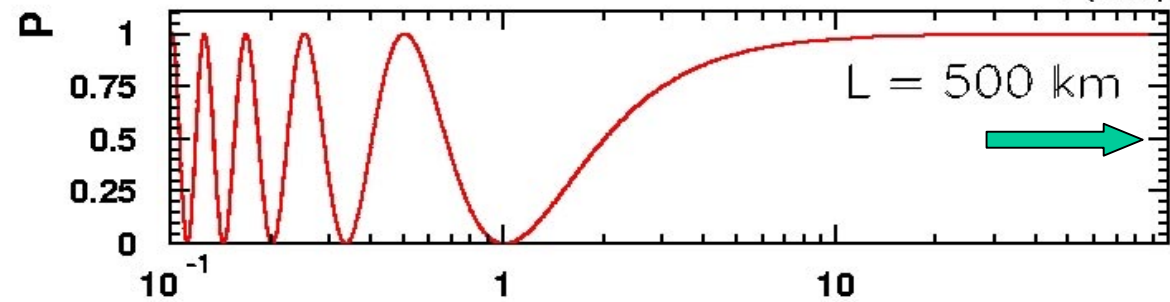
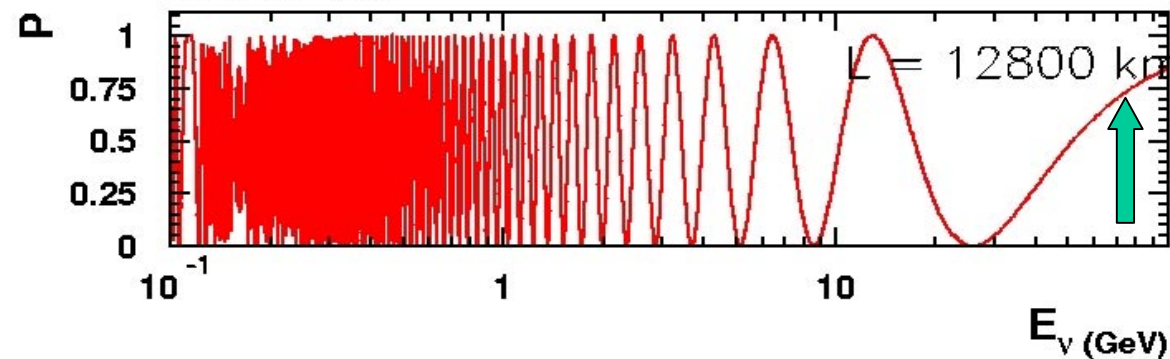
e -like (showers): in agreement with expected

Kamiokande Multi-GeV:
flavor ratio angular
dependence as expected
from oscillations

Oscillations in atmospheric vs

Survival Probability

$\Delta m^2 = 2.5e-3 \text{ eV}^2$



$100 \text{ MeV} \lesssim E_\nu \lesssim 10 \text{ TeV}$

$10 \text{ km} \lesssim L \lesssim 10^4 \text{ km}$

Wide range to investigate oscillations!

For Sub-GeV and Multi-GeV

$$P(\nu_e \rightarrow \nu_e) = 1 - \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E_\nu} \right)$$

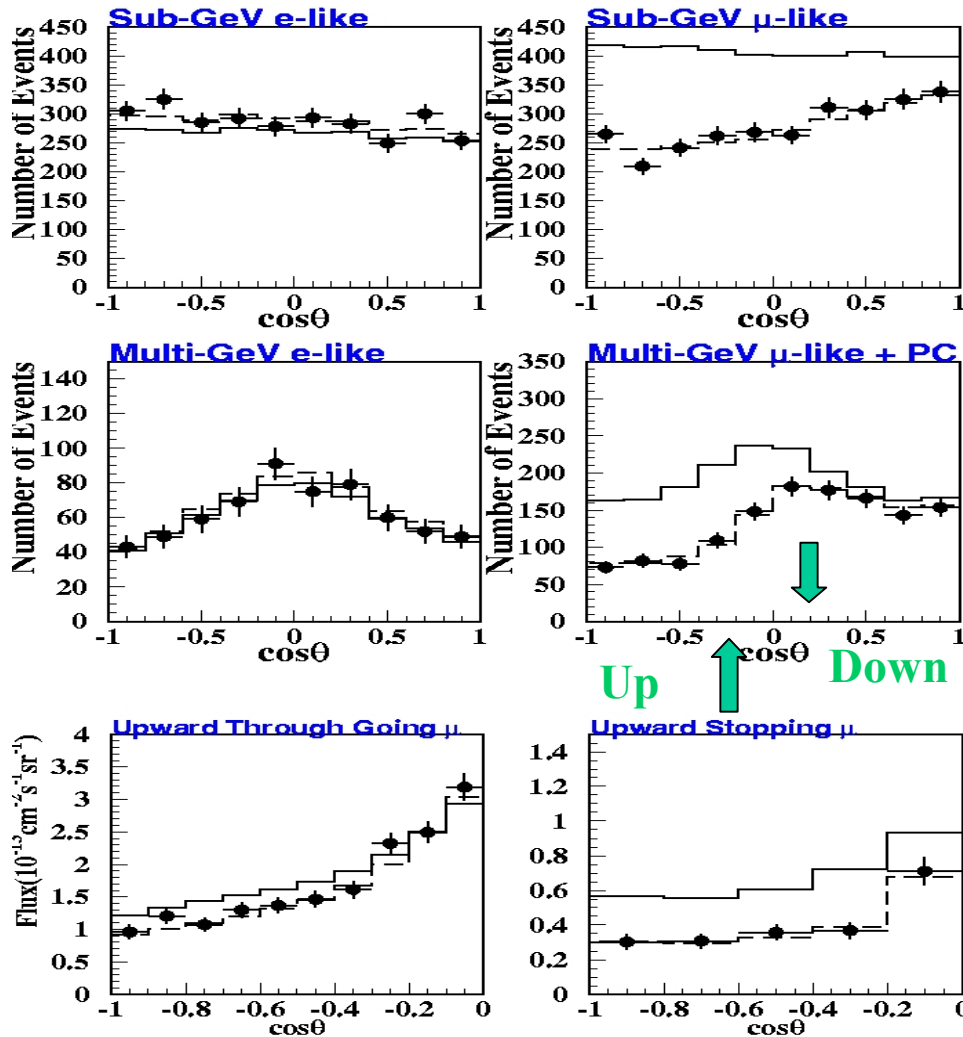
$$\langle P(L \leq 100 \text{ km}) \rangle \rightarrow 1$$

$$\langle P(L \geq 2000 \text{ km}) \rangle \rightarrow 1 - \frac{\sin^2 2\theta}{2} \Rightarrow \frac{1}{2}$$

Horizontal events in transition region $L \sim 500 \text{ km}$ are important to determine Δm^2

Super-Kamiokande evidences

Super-Kamiokande data (Y. Totsuka talk) explained by $\nu_\mu \rightarrow \nu_\tau$ oscillations



$\nu_\mu \rightarrow \nu_{\text{sterile}}$ disfavoured 99%cl

Muon deficit is energy dependent

Best fit: $\Delta m^2 = 0.0025 \text{ eV}^2$
 $\sin^2 2\theta = 1, \chi^2/\text{dof} = 142/152$

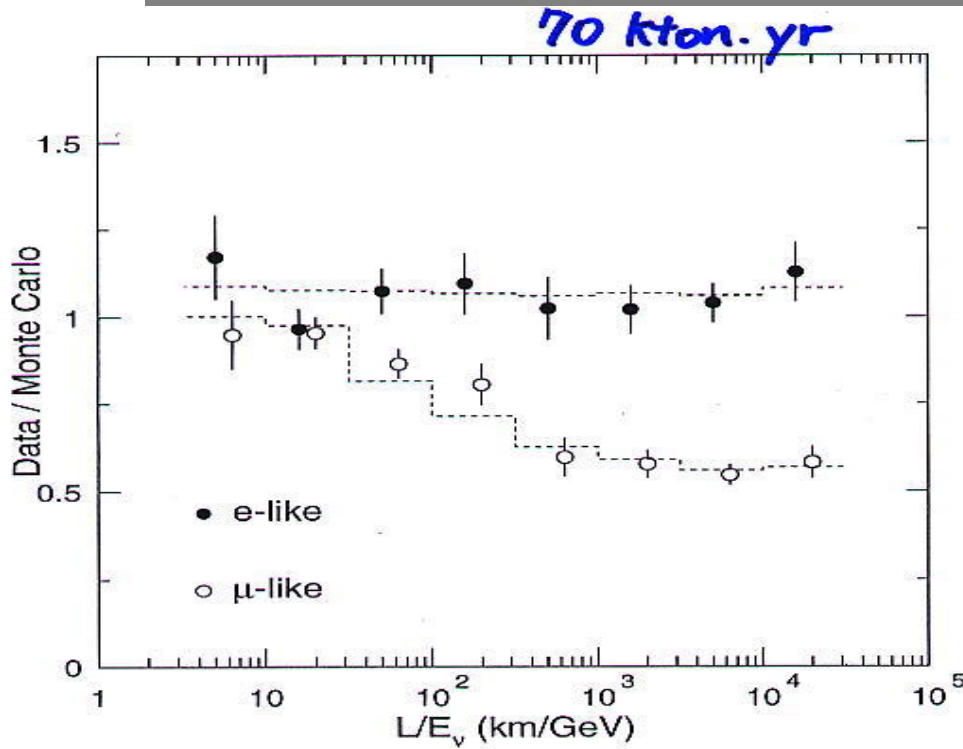
Smoking gun:

asymmetry UP/Down μ -like
 (70kt yr)

$0.54 \pm 0.04 \pm 0.01 (9\sigma)$

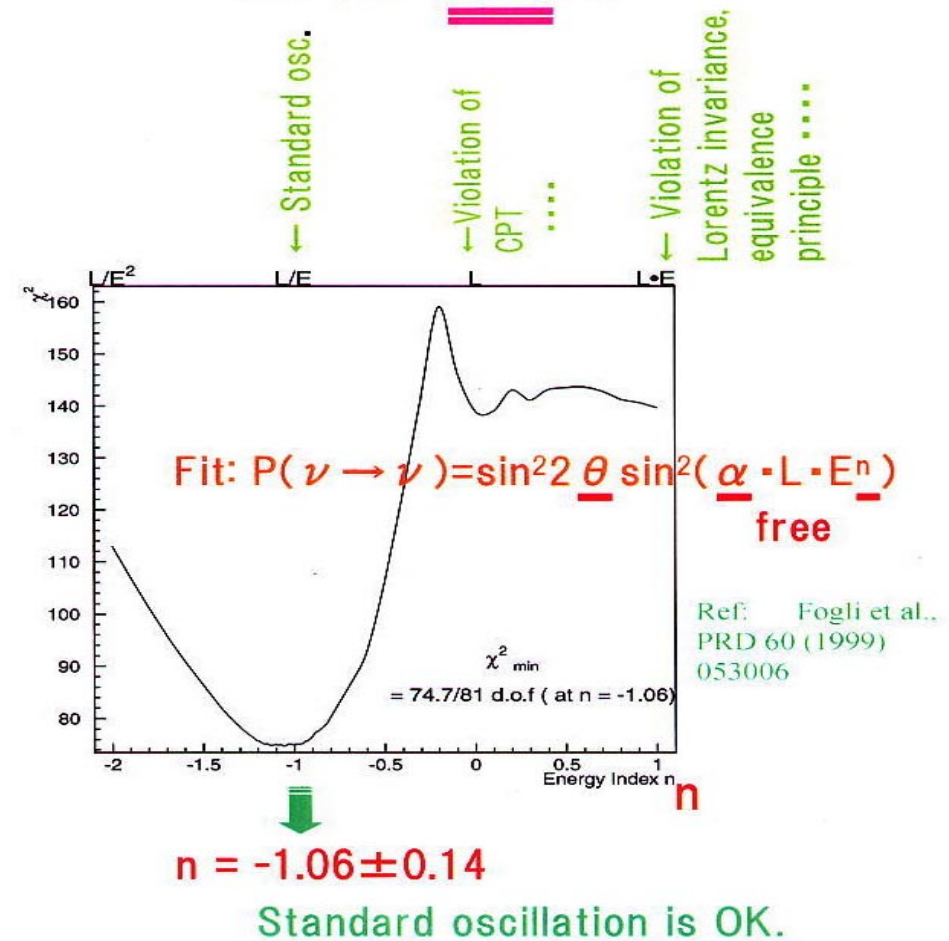
79 kt yr
 (1289 d)

Super-Kamiokande: L/E dependence



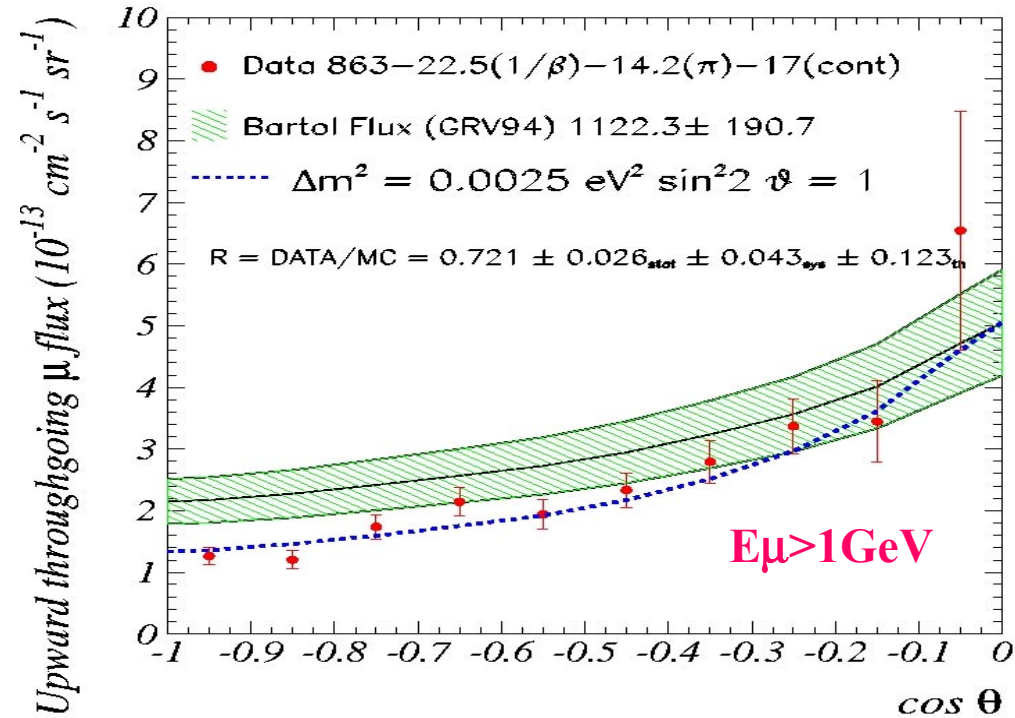
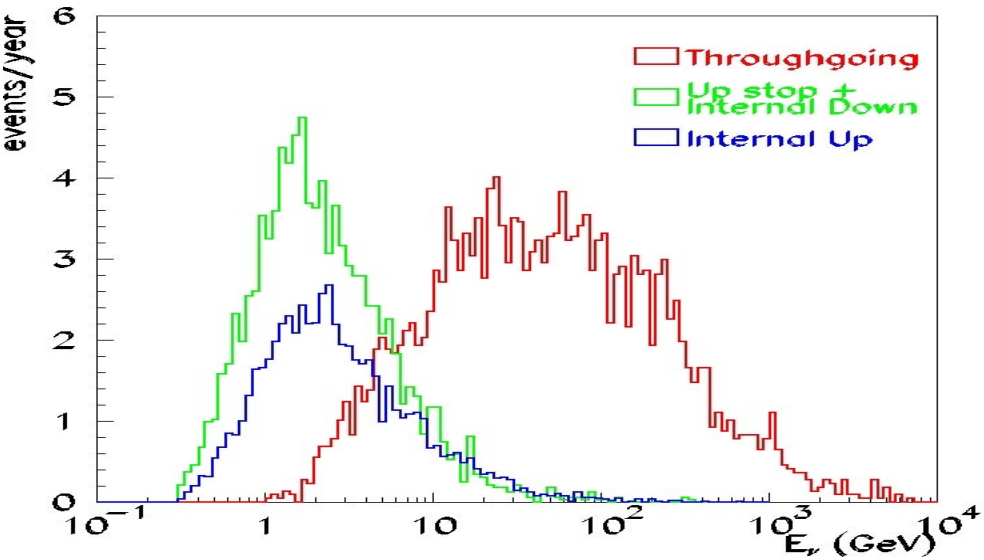
Warning: oscillation pattern in L/E remains unobserved!

Oscillations are proportional to $\sin^2(\alpha \cdot L/E)$?



T.Kajita Now2000

MACRO: different technique



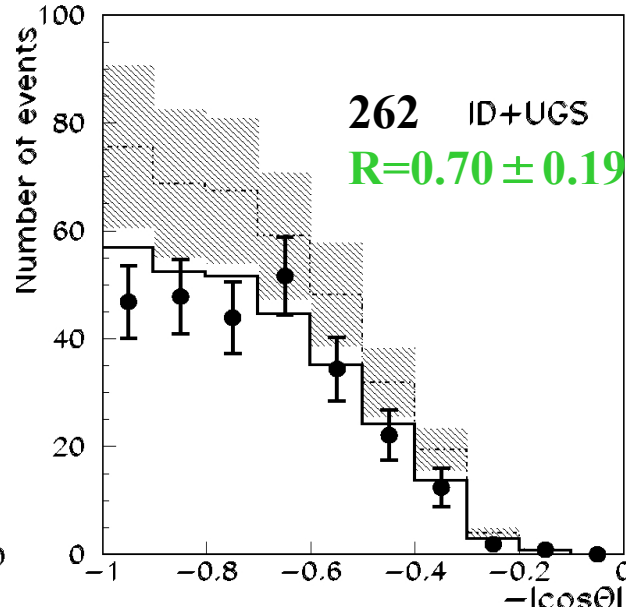
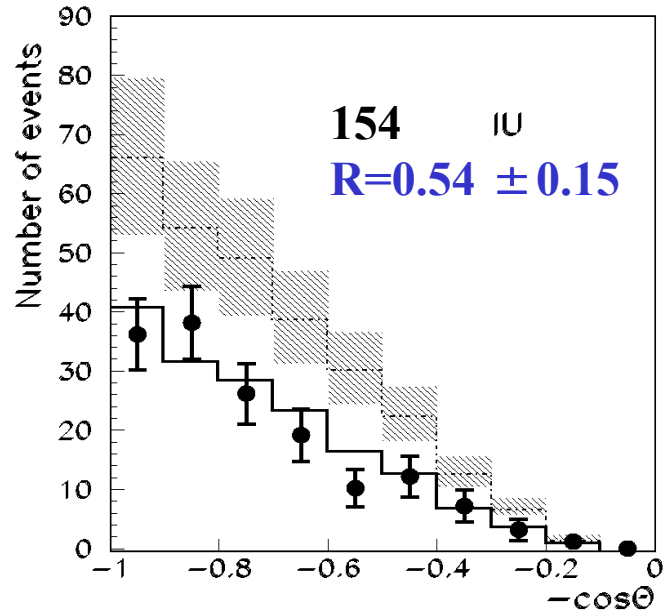
Different topologies:

- **Through-going** ($\langle E_\nu \rangle \sim 50 \text{ GeV}$, 180/yr)
- **Internal Up** ($\langle E_\nu \rangle \sim 4 \text{ GeV}$, 50/yr)
- **μ Stop+Internal Down** ($\langle E_\nu \rangle \sim 4 \text{ GeV}$, 35+35/yr)

} contamination from
NC + CC $\nu_e \sim 10\%$

Vertical/horizontal through-going μ s exclude $\nu_\mu \rightarrow \nu_{\text{sterile}}$ @ 99% c.l.

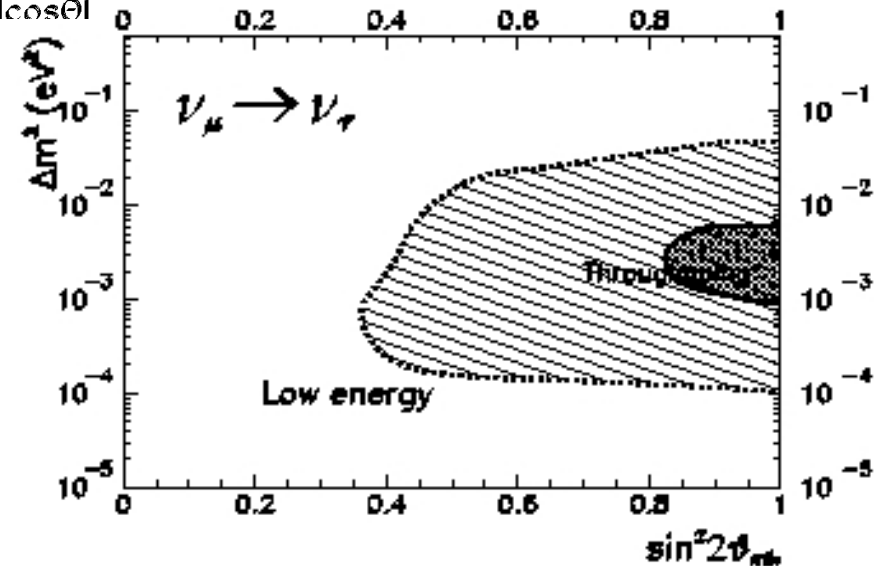
MACRO favors $\nu_\mu \rightarrow \nu_\tau$



(ID+UGS/IU)meas = 0.59 ± 0.06 stat
 (ID+UGS/IU)no osc = 0.76 ± 0.06 sys+theor
 (sys = 5% theor = 5%)
 Probability of obtaining a ratio so far from expected 2.2%

Low energy events: max probability 87% (max mixing)

Through-going up μ : max probability of 66% at $\Delta m^2 = 0.0024 \text{ eV}^2$ and $\sin^2 2\theta = 1$ for $\nu_\mu \rightarrow \nu_\tau$



Montecarlo and analytical calculations

Montecarlo (all details can be included):

- **HKKM:** M. Honda, T. Kajita, K. Kasahara & Midorikawa, Phys. Rev D52 (1995)
 - **Bartol:** **G. Barr**, T.K. Gaisser and T. Stanev, Phys. Rev. D39 (1989) and ICRC95, V. Agrawal, T.K. Gaisser, P. Lipari, T. Stanev, Phys. Rev. D53 (1996)
- “Standard references” used in Super-Kamiokande, MACRO, Soudan2,...

New calculations (under development):

3D:

- G. Battistoni, A. Ferrari, P. Lipari, T. Montaruli, P.R. Sala & T. Rancati, Astrop. Phys. 12 (2000) [Updated results in <http://www.mi.infn.it/~battist/neutrino.html>]
- Y. Tserkovnyak, R. Komar, C. Nally, C. Waltham, hep-ph/9907450
- P. Lipari, Astropart.Phys.14:153-170,2000
- M. Honda, T. Kajita, K. Kasahara, S. Midorikawa, hep-ph/0103328
- V. Plyaskin, hep-ph/0103286

1D:

- G. Fiorentini, V. A. Naumov, F. L. Villante, hep-ph/0103322

NOT ALL
MENTIONED
HERE!

Analytical (fast and for tests to understand processes)

T.K. Gaisser, astro-ph/0104327, P. Lipari, Astropart. Phys.1 (1993)

Some comments

“Standard references” very close to **final** result: improvements/checks are going to be presented

New calculations can be validated through comparison to existing data; results from a set of calculations which are converging (HKKM, Bartol, Fluka,...) should be taken into account

Improvements are motivated by understanding that agreement (~10%) between HKKM and Bartol comes from compensation of errors

1. Bartol uses a primary flux closer to LEAP and recent measurements but seems to produce higher multiplicities of pions, kaons and different momentum distributions than FLUKA

2. HKKM uses a primary flux closer to Webber et al., higher than more recent measurements

Calculations are checked comparing each “ingredient” by changing them inside calculations under comparisons

Fundamental benchmark: muons

Calculation inputs

1. **Primary spectra** (fits to recent measurements, isotropy, superposition model, solar modulation)
2. **Hadronic interactions** (multiplicities, energy distributions, cross-sections)
3. **Shower modeling** (particle transport, energy losses, decays including polarization)
3. **Geometry**: 3D/1D
4. **Geomagnetic effects**: E-W asymmetry, under cut-off fluxes, bending of shower particles
5. **Atmosphere profiles and seasonal effects**
6. **Neutrino interaction cross sections: from neutrinos to leptons**
7. **Minor effects**: detector altitude, mountain profiles

Primary spectrum

Before 1990 primary spectrum $\leq 100 \text{ GeV}$ ambiguous due to 50% discrepancy between Webber et al. (1987) and LEAP (1991)

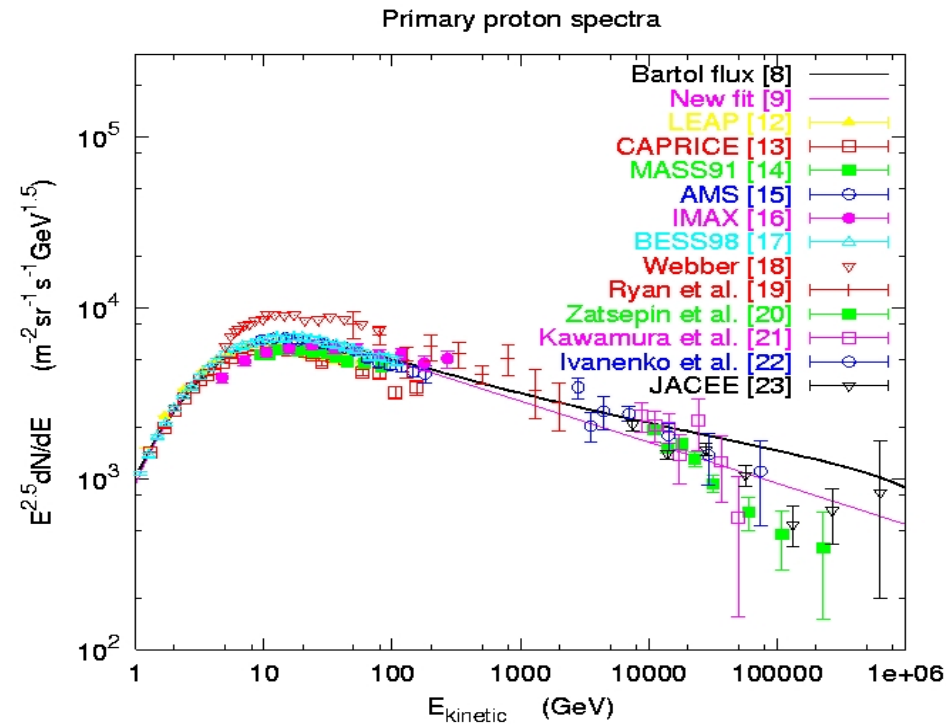
Recent data (CAPRICE, AMS, BESS) agree with lower LEAP normalization

Determination with systematic uncertainty $\sim \pm 5\%$ (agreement AMS-BESS98)

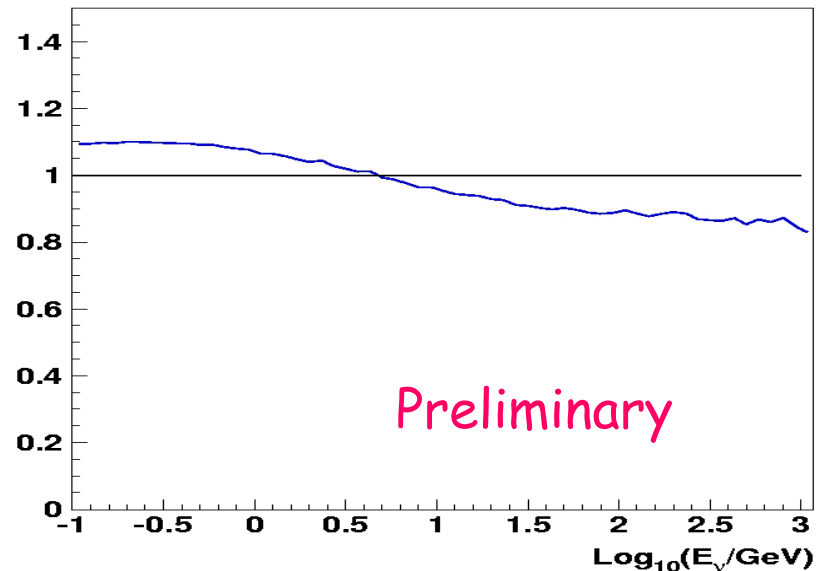
For $E \leq 1 \text{ TeV}$ uncertainty $\sim 10\%$ (important for upward muons)

At $E \geq 1 \text{ TeV}$ uncertainty $\geq 25\%$ but small contribution to observed fluxes

A new fit will be presented at ICRC by Bartol Group:



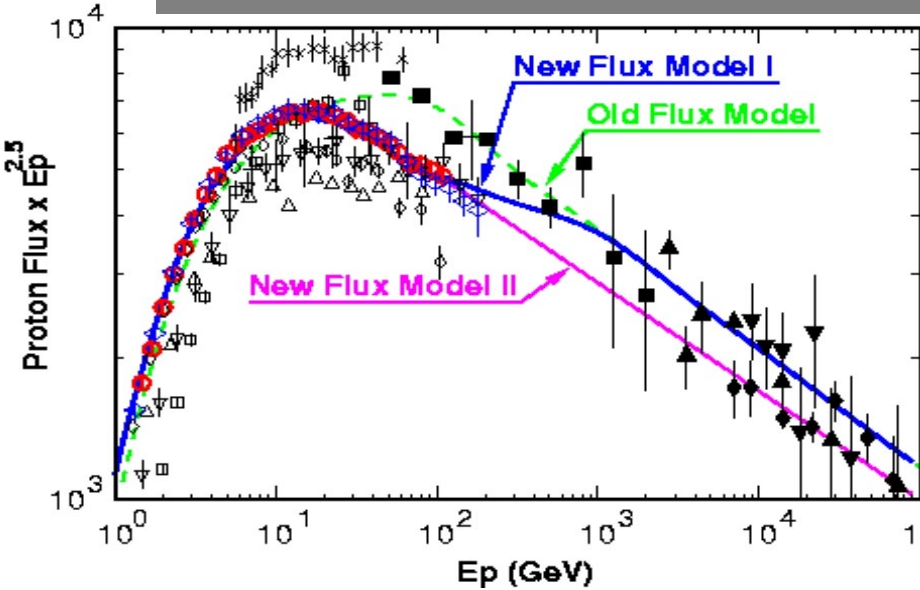
v_μ : Lipari/Bartol primary spectrum



Larger effect in the upward μ region

Preliminary

Primary spectrum



HKKM are studying 2 new models differing at HE energy

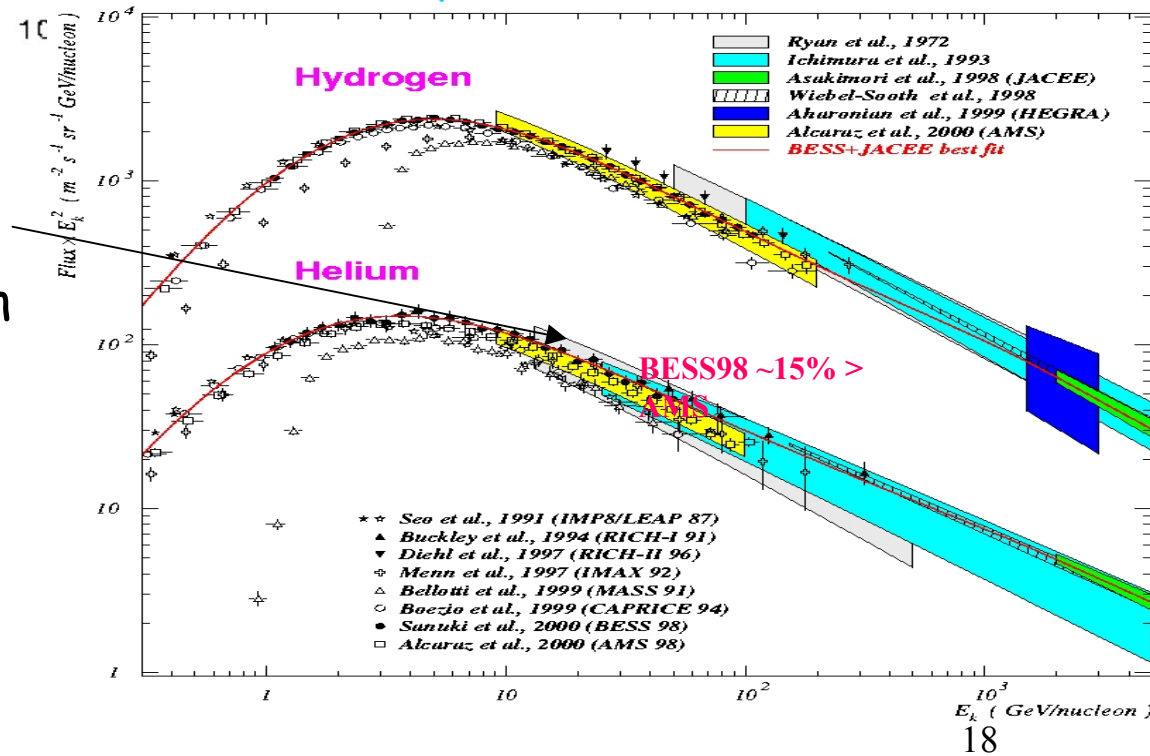
Neutrino flux difference < 2-3% @ 1 GeV
~10% @ 10 GeV

Old-New Model I: lower flux by 8-12% @ 1 GeV, ~20% @ 8 GeV

Other fit by Fiorentini et al.

Higher uncertainty for heavier components (~20% of total flux);
He flux still some disagreement
Future: Bess, Pamela (~200 GeV/n from H-C)

Important: converge towards a certified reference spectrum common to all calculations + algorithm for solar modulation



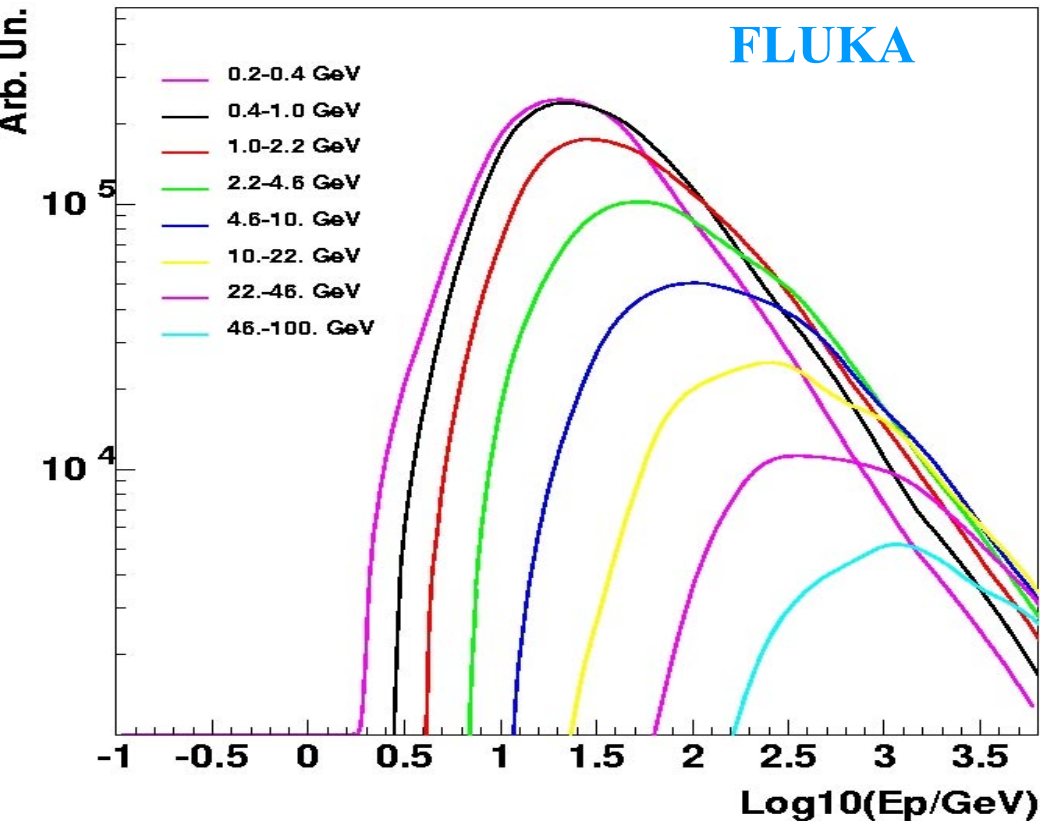
Primary and neutrino energies

Estimated uncertainties have implications on atmospheric ν s:

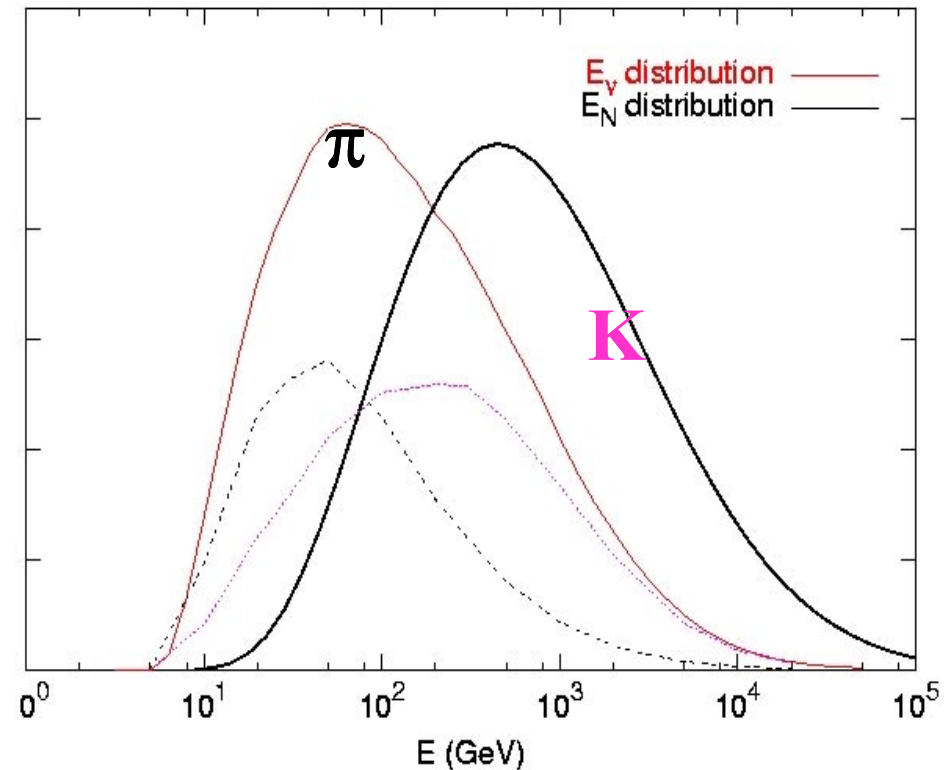
Sub-GeV $E_N \leq 1-200$ GeV, Multi-GeV $E_N \sim 10-1000$ GeV, μ stop $E_N \sim 20-2000$ GeV

Up-through μ $E_N \sim 100-50000$ GeV

Primary energy contributing to ν at Kamioka



Response for vertically upward muons in Super-K



Analytical: TKGaisser, astro-ph/ 0104327

Solar Modulation

Time dependence for $E \leq 10$ GeV more relevant @ low cut-off sites (Soudan)
Solar wind plasma + e.m. fields \Rightarrow heliosphere semi-transparent to opaque medium
for low energy CRs correlated with 11 yr-cycle (exact periodicity in 22 yr due to IMF polarity)

Sunspot monitoring by n monitors @ Earth (1-20 GeV): measure hadronic component through secondary interactions in lead + proportional counters

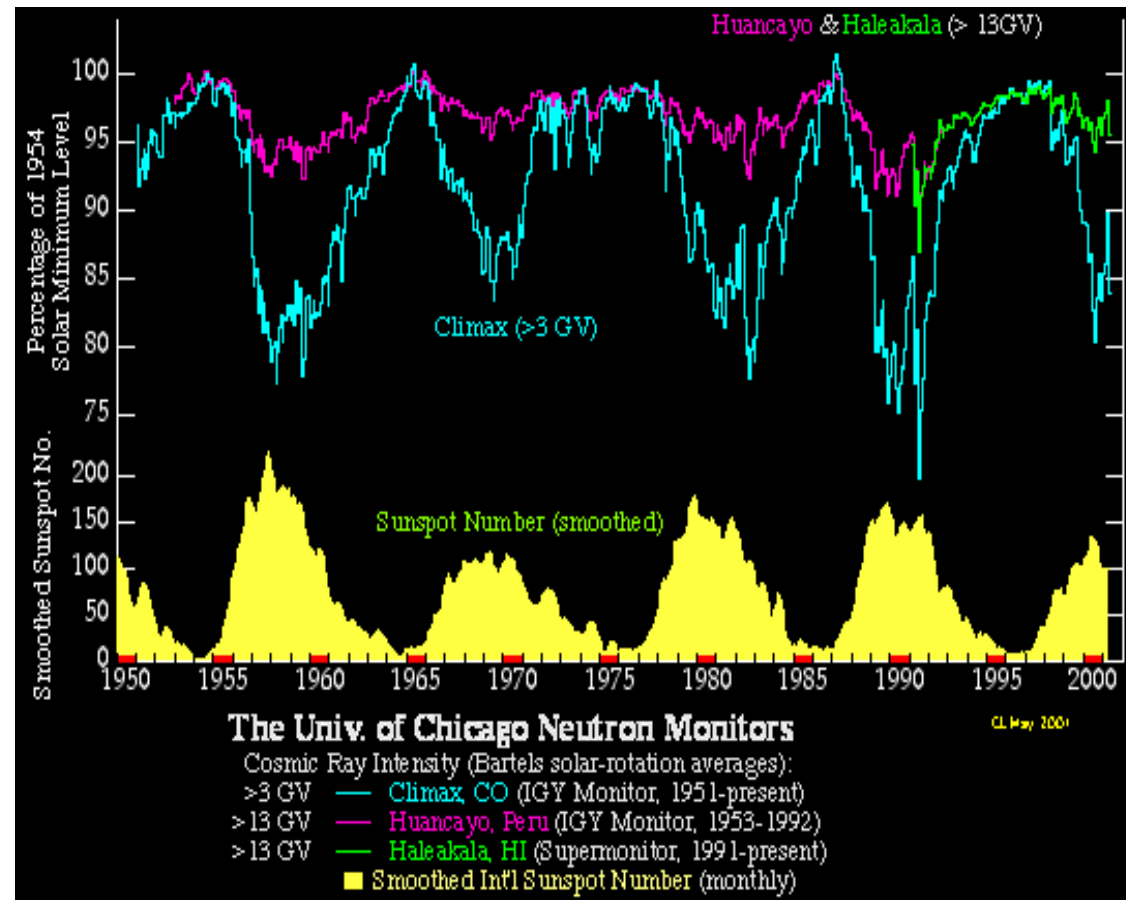
Depends on detector λ + altitude

Badhwar & O'Neill (used by FLUKA): $\Phi(MV)$ estimated from fits to Climax n counting rates + sunspot numbers (> 4 cycles) to predict modulation at later times

Predict galactic CR intensity inside $\pm 10\%$ for 3 month variations

Φ_V solar min / Φ_V solar max $\sim 5\%$

@ 1 GeV for SK site



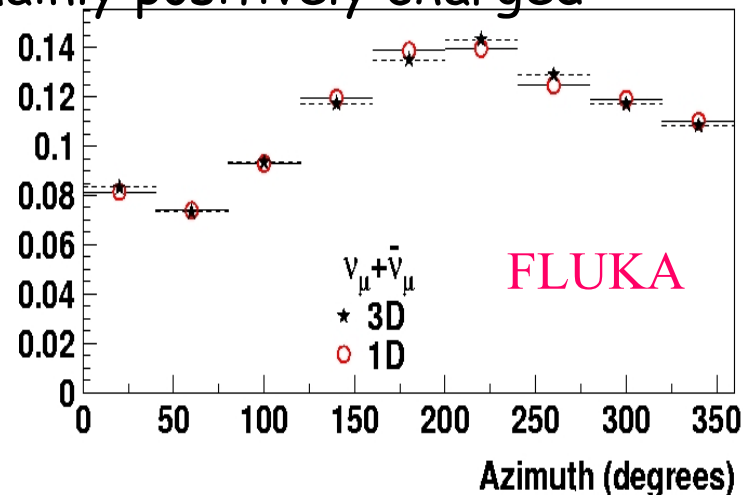
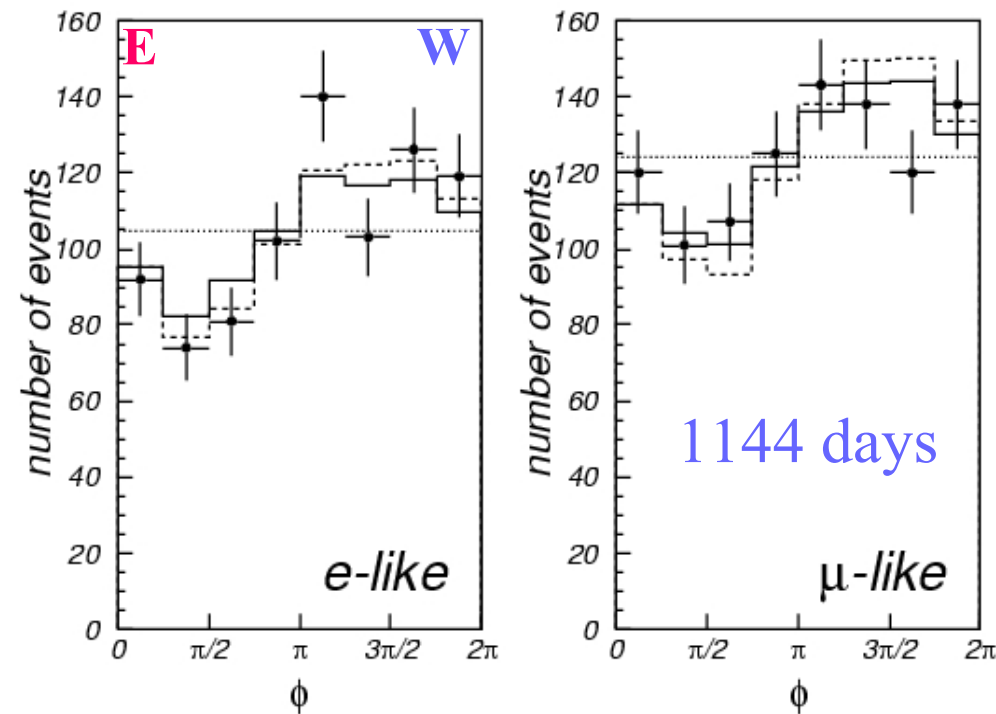
CR flux isotropy: geomagnetic effects

Geomagnetic field prevents low rigidity CRs from reaching atmosphere
 Dependence on detector location (higher flux at Poles) + CR direction

Most important source of asymmetry breaking at $E_{\nu} \leq 2 \text{ GeV}$

Test: Super-Kamiokande East-West asymmetry in azimuth

Secondary flux $>$ for W directions due to CR mainly positively charged



3D/1D small effect, but here no field in shower development: μ bending can improve agreement
 (measured $A_e = (E-W)/(E+W) > A_{\mu}$)

Ref.: P. Lipari: hep-ph/9905506, hep-ph/0003013, P. Lipari, T. Stanev & T.K. Gaisser, PRD58 (1998), HKKM, hep-ph/0103328, <http://nssdc.gsfc.nasa.gov/space>

CR flux isotropy: geomagnetic effects

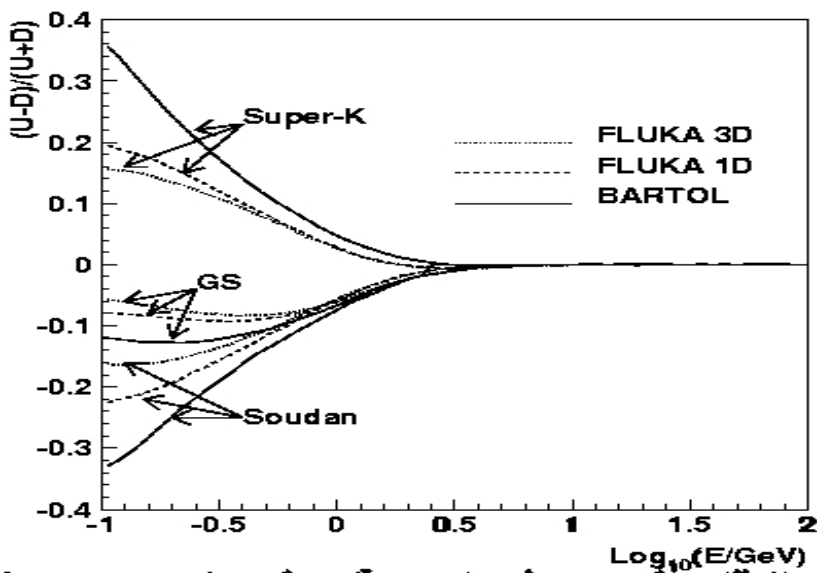
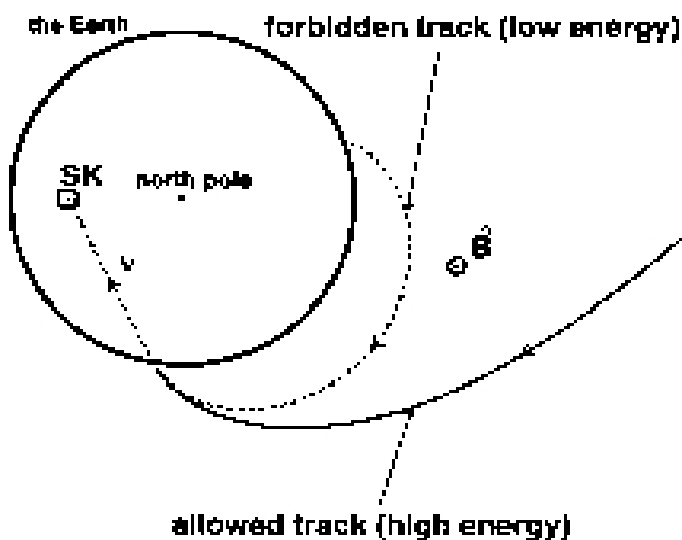
Offset dipolar model not precise enough

International Geomagnetic Reference Field employs spherical harmonic expansion of scalar potential (coefficients slightly vary with time)
Dipolar models can differ ~30% from IGRF

Back-tracing technique: backward path for CR with same A and E but opposite charge
(allowed = out of geomagnetic sphere to ∞)

AMS measurement of CR fluxes at different latitudes CR isotropy at 10% level
Asymmetry breaking: Up Sub-GeV flux
> Down @ SK due to high cut-off, < @ Soudan due to low cut-off

FLUKA < Bartol asymmetry due to lower ν yield



Sub-cutoff fluxes

AMS PLB472 (2000) @ ~ 400 km in $\pm 51.7^\circ$ latitude interval: **sub-cutoff secondary fluxes** produced by CR in upper atmosphere, bent by geomagnetic field toward higher altitudes; trapped at lower altitudes for seconds

Downgoing p fluxes

FLUKA 3D (Zuccon et al.): internal +external magnetic fields, p back-tracing

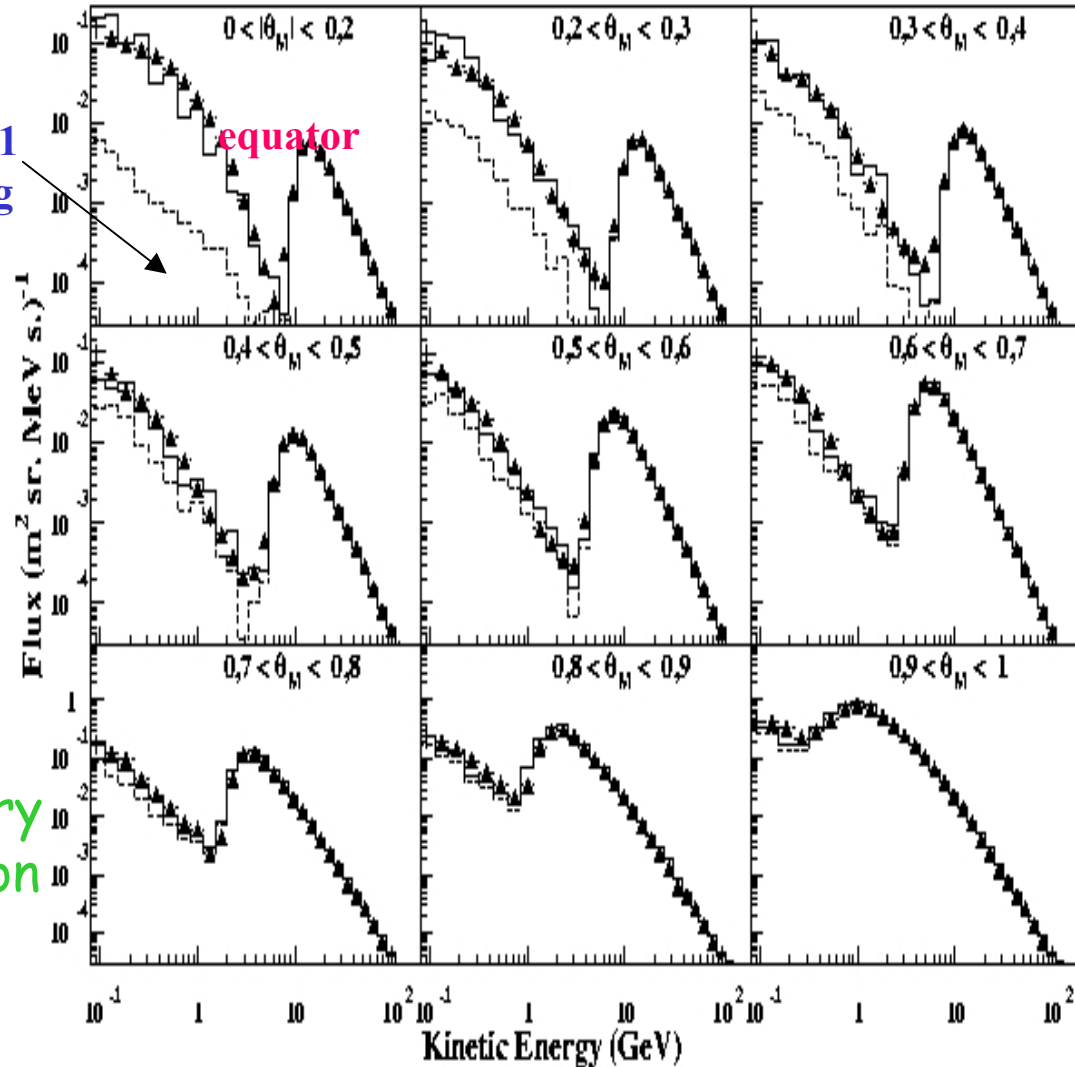
Detector: spherical surface @ 400 km, F.o.V.+acceptance

Very good agreement of upgoing/downgoing p, e^\pm

Some particles have large probability to cross many times detector mostly in equatorial region (high cut-off)

real p flux=1 det. crossing

Considering largest equatorial secondary flux $\Rightarrow 0.06$ (kton yr) $^{-1} \leq 1\%$ contribution (P. Lipari, astro-ph/0101559)



Atmosphere models

Atmosphere density profile depends on geographical position and seasonal temperature variations: affect competition between interaction-decay

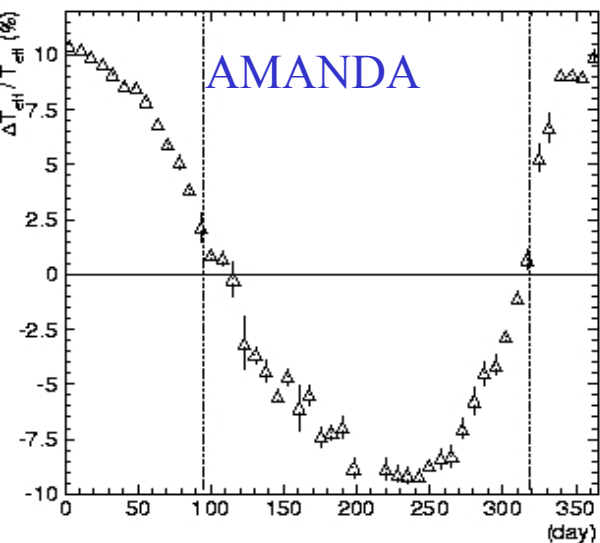
If T increases ρ decreases \Rightarrow mesons have decay prob. $>$ interaction prob.

AMANDA $\pm 10\%$, MACRO $\pm 1.5\%$

For atm. μ easier calculation than for ν coming from all over the Earth

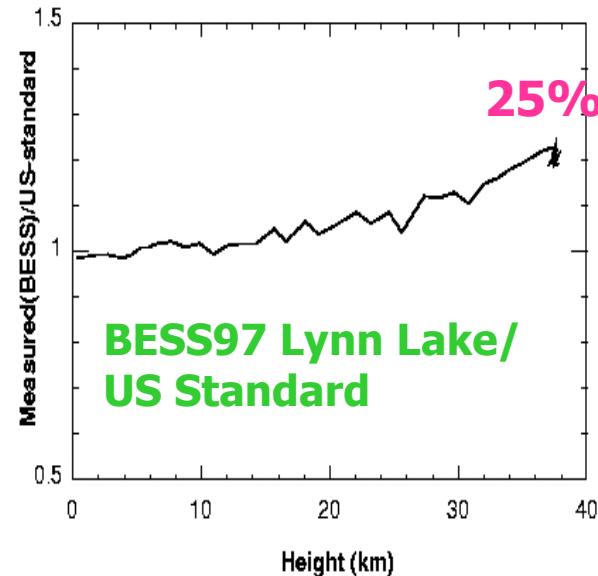
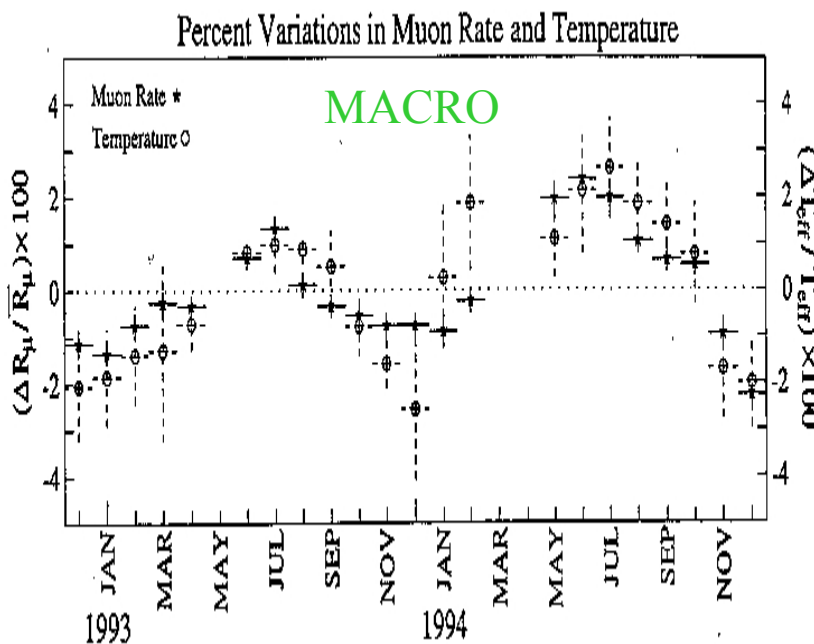
T is very different for downgoing/upgoing ν s

US-standard model widely used in calculations; comparisons with balloon measurements show differences (MACRO estimates effect $\sim 1\%$ for up μ s)



Apr 1997

Nov



Seasonal effects

Seasonal effects: additional source of uncertainty in vertical/horizontal to discriminate $\nu_{\text{sterile}}/\nu_{\tau}$ oscillations (SK, MACRO)

MACRO estimates 3% error on K/π , 2% from ν cross sections due to different energy distributions and (analytical calculation) 1.3% due to seasonal effects, 1% to different atmospheres than US standard

MACRO throughgoing μ s: $R = (-1 < \cos\theta < -0.7) / (-0.4 < \cos\theta < 0)$ divided in "winter" (Nov.-Apr.) and "summer" \Rightarrow winter-summer variation of vertical/horizontal $19 \pm 17\%$ (stat)

Honda: estimates variation on muon neutrino fluxes from winter to summer $\sim 6\%$ @ 100 GeV at vertical (max effect)

FLUKA group is preparing setup for 4 different atmospheres

Primary- ν directions

$\theta_{N\nu} = \theta_{N\pi} \oplus \theta_{\pi\nu}$ (when μ decay: $\theta_{N\nu} = \theta_{N\pi} \oplus \theta_{\pi\mu} \oplus \theta_{\mu B} \oplus \theta_{\mu\nu}$)

$\langle \theta_{N\pi} \rangle \sim \langle p_T \rangle / p_\pi \sim 0.35 \text{ GeV}/c / 4E_\nu \sim 5^\circ / E_\nu (\text{GeV})$

Negligible contributions:

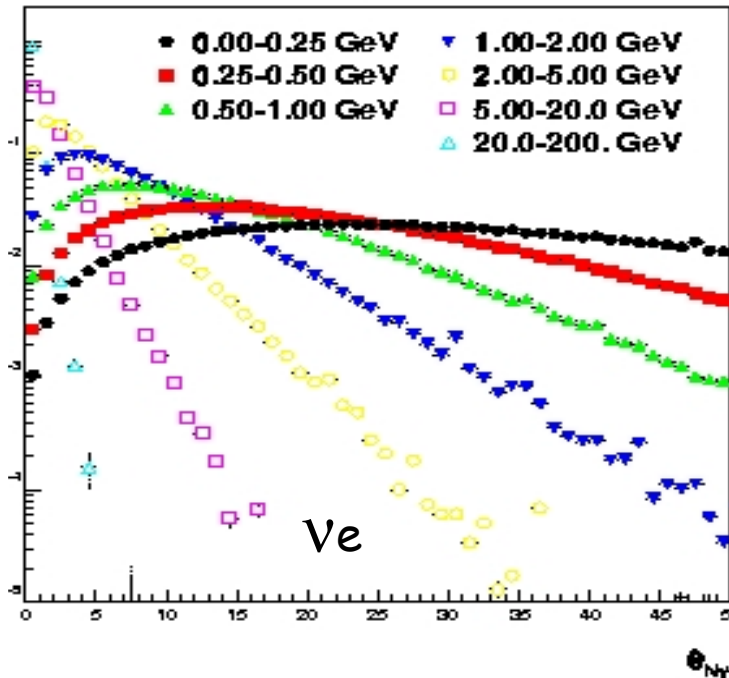
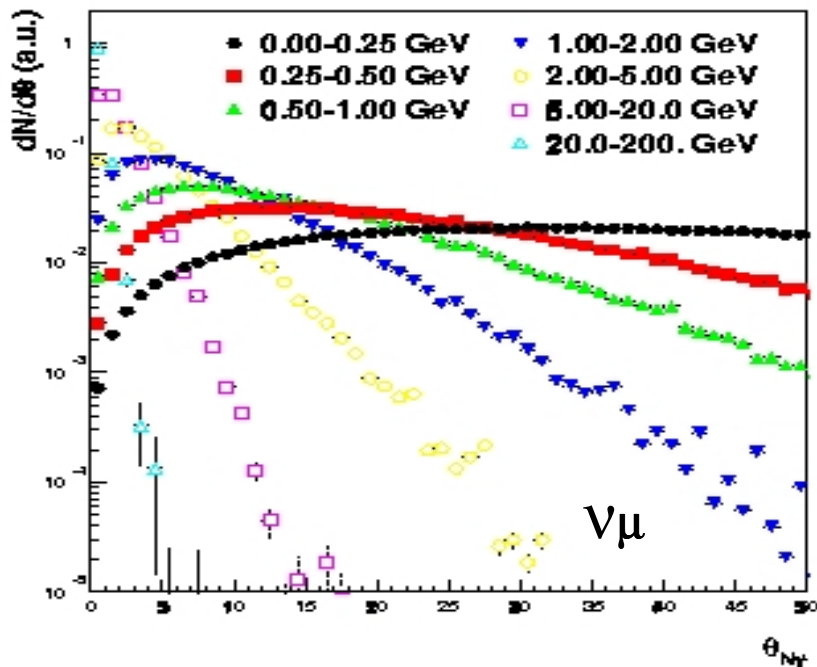
$\pi \rightarrow \mu\nu$: $\theta_{\pi\nu} \sim p_{cm} / p_\nu \sim 1.7^\circ / E_\nu$

$\theta_{\pi\mu} \sim p_{cm} / p_\mu \sim p_{cm} / 3p_\nu \sim 0.6^\circ / E_\nu$

$\mu \rightarrow \mu\nu\nu$: $\theta_{\mu\nu} \sim m_\mu / 3E_\nu \sim 2^\circ / E_\nu (\text{GeV})$

μ bending: $\theta_{\mu B} \sim L_\mu / R_\mu \sim (\tau_\mu p_\mu / m_\mu) (eB / p_\mu) \sim 10.7^\circ B (\text{Gauss})$

high $p_\mu \Rightarrow$ bend less but live longer $\Rightarrow B$ acts longer



$\langle \theta_{N\nu e} \rangle \gtrsim \langle \theta_{N\nu\mu} \rangle$
3rd generation
 $E_\nu (\text{GeV})$ ν_μ ν_e
 0.25-0.5 24° 28°
 5-20 1.8° 1.8°

→ No μ bending

3D/1D effects

Differences between 1D/3D calculations have been investigated

1D: p_T of secondaries in int./decay+multiple scatt. neglected \Rightarrow v collinear to primary) based on 2 hypotheses:

- 1) isotropy of primary CRs
- 2) spherical geometry of Earth+atmosphere

Valid approx. for Multi-GeV: θ_{Nv} increases for decreasing E_v

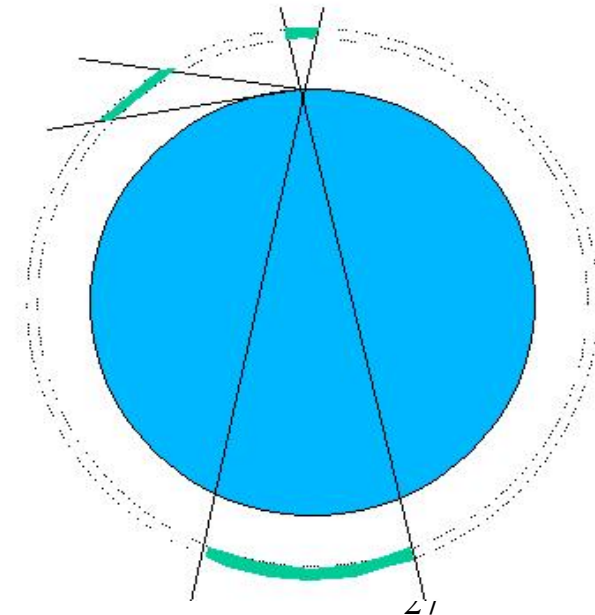
Differences in Sub-GeV angular distribution due to large θ_{Nv} :
3D enhancement @ horizon

Geometrical effect: vs between θ - $\theta+d\theta$ produced by atmosphere patch of area

$$dA = L^2(\theta)d\theta / \cos\theta_e$$

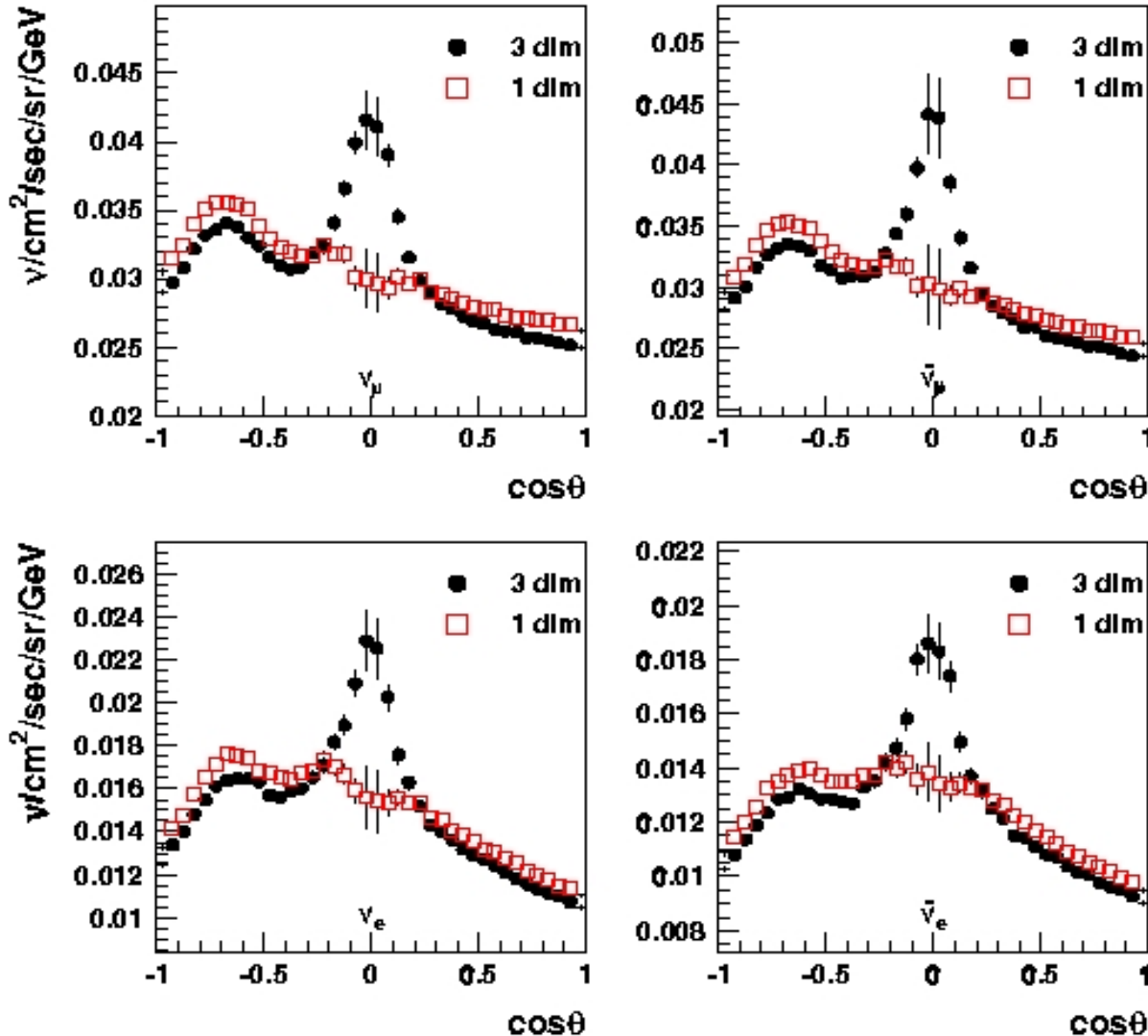
L = distance to detector $\theta_e = v$ emission angle

$1/\cos\theta_e$ responsible of horizontal enhancement



3D/1D: horizontal enhancement

Sub-GeV flux at Kamioka

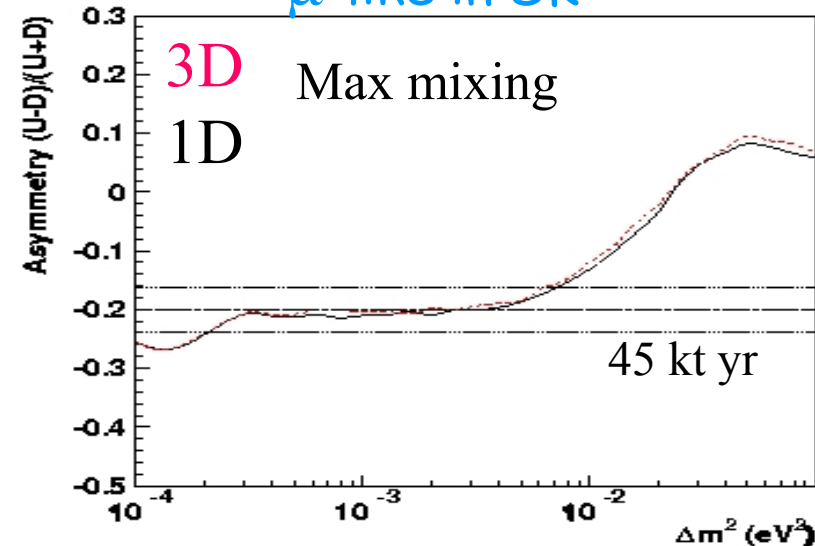


FLUKA 1D/3D

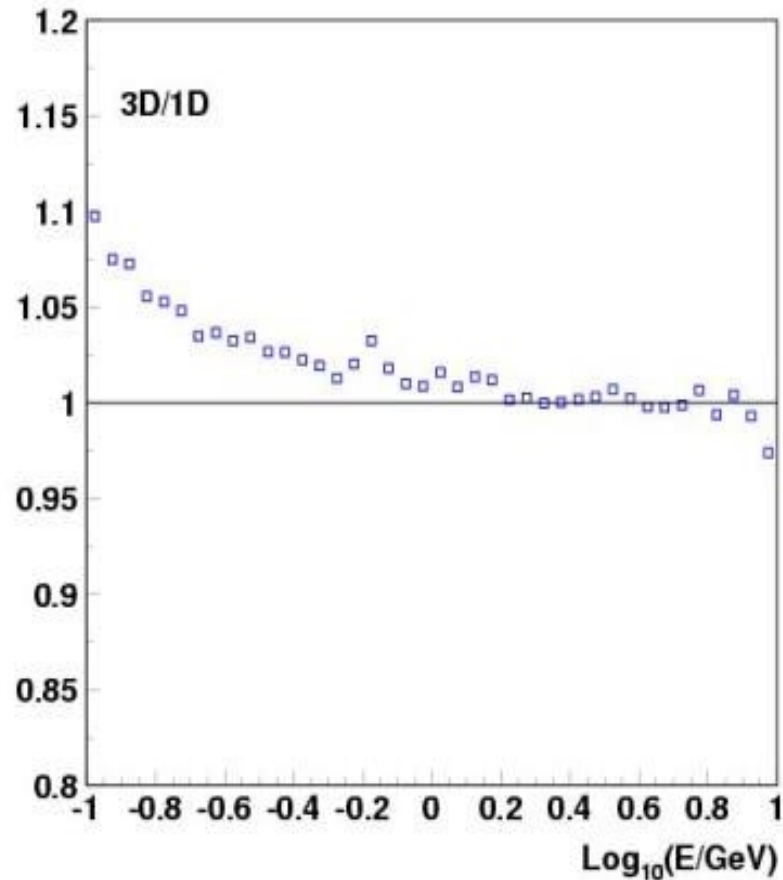
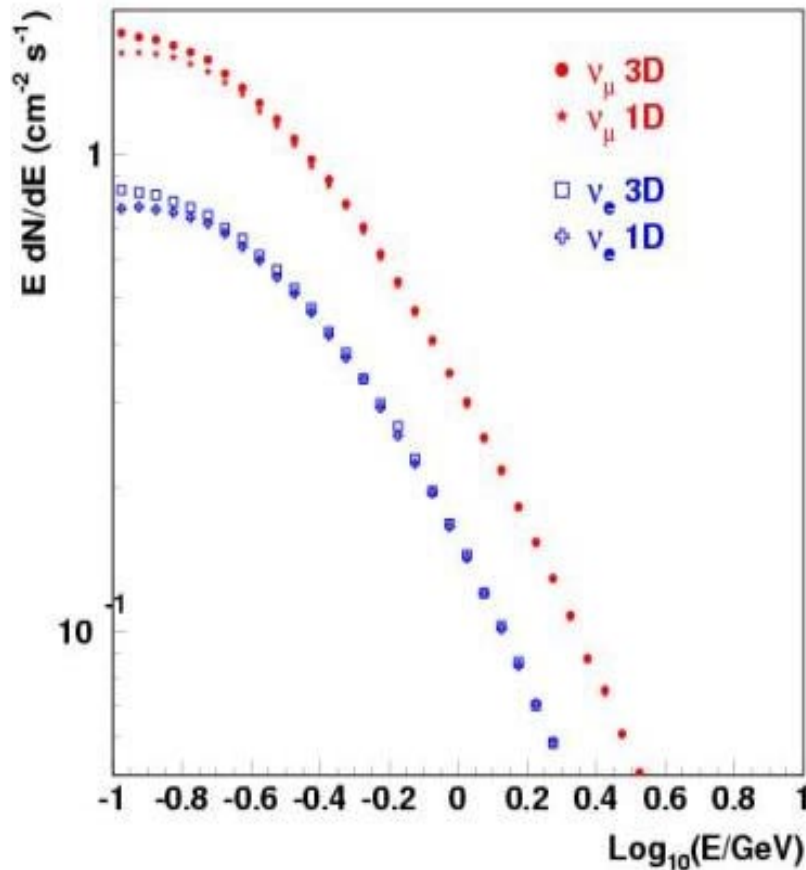
Battistoni et al., *Astrop. Phys.* 12 (2000)
 Similar results in P. Lipari, *Astrop. Phys.* 14 (2000)

Asymmetry not affected
 Modest contribution in Δm^2 evaluation

μ -like in SK



3D/1D: normalization



FLUKA 1D/3D

Superkamiokande site

Small effect on normalization $\sim 5\%$ for $E \nu < 1 \text{ GeV}$

1D/3D and geomagnetic field

Next step: introduce geomagnetic field in shower development

Loss of rotational symmetry \Rightarrow high inefficiency (calculations must be performed at detector site)

No B in shower development (FLUKA):

ν generated on sphere with $B=0$

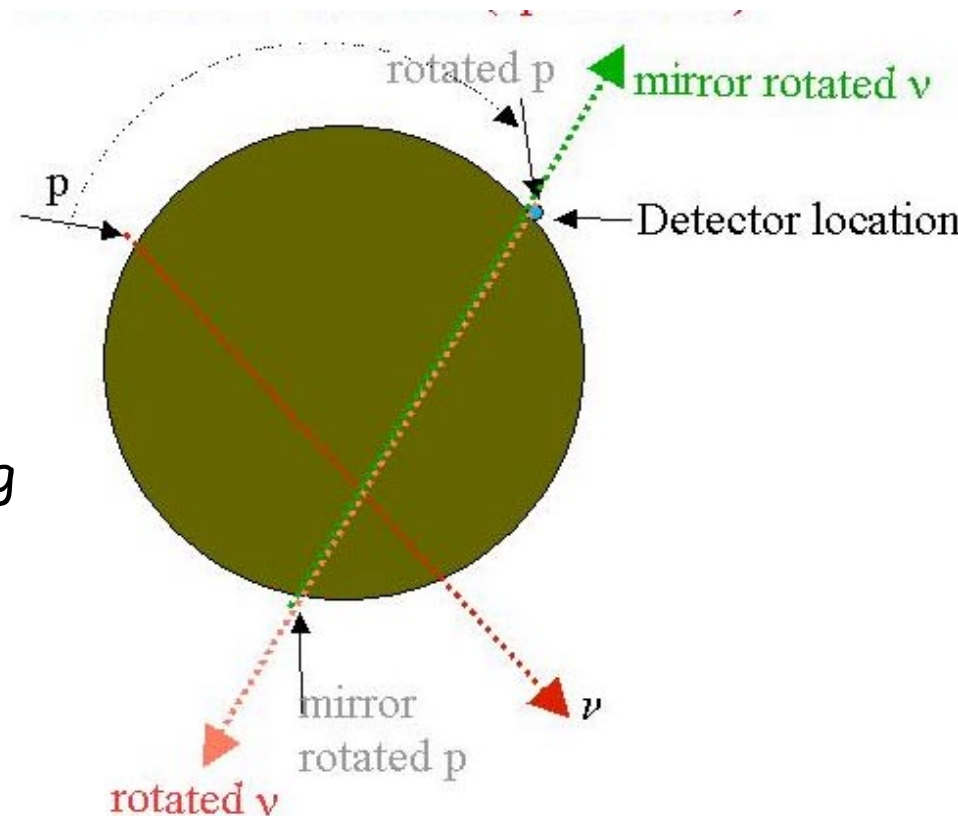
ν reaching surface can be rotated with its parent to detector site for cut-off calculations

For each upcoming ν a "mirror" downcoming ν is created (there is up-down symmetry because ν is generated with $B=0$)

FLUKA(next future): weighting towards detector location

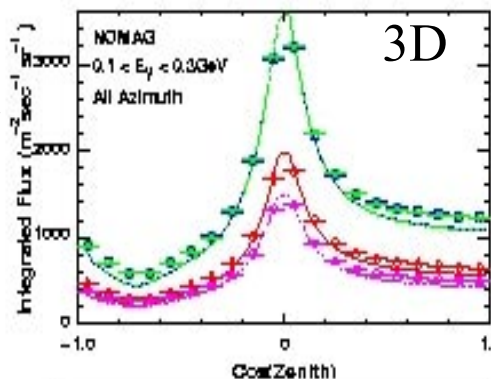
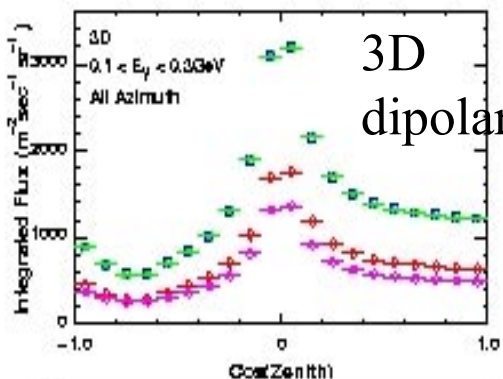
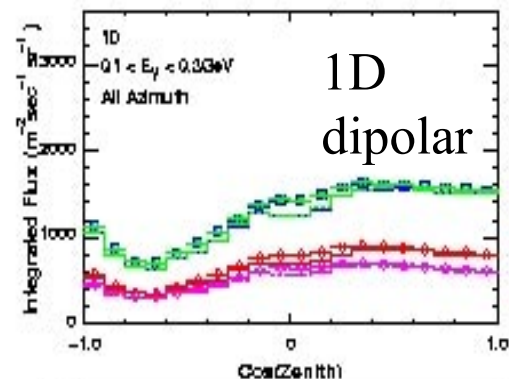
HKKM: dipolar field (axial symmetry)

Tservkovnyak et al., huge detector size

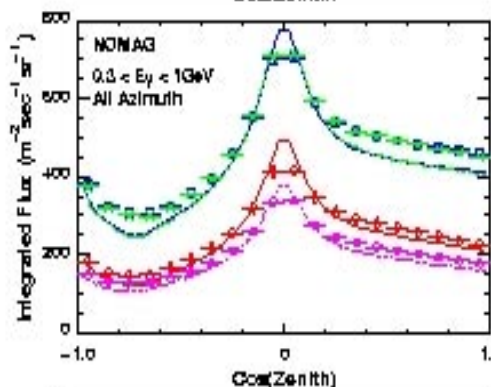
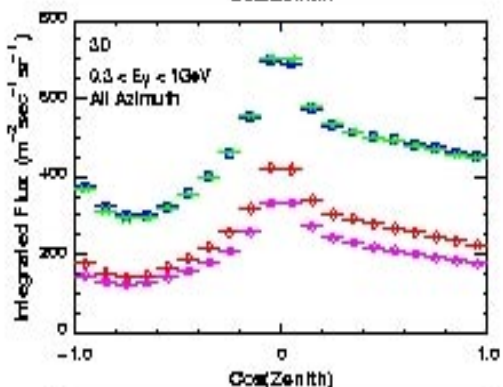
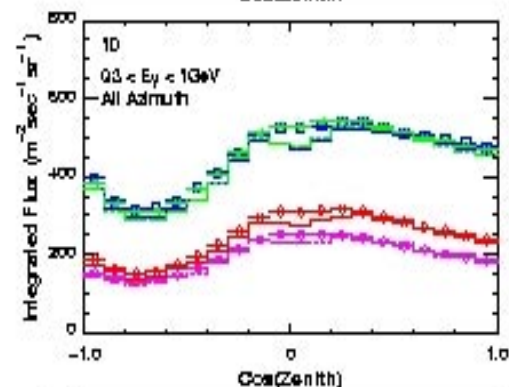


1D/3D zenith angular distributions

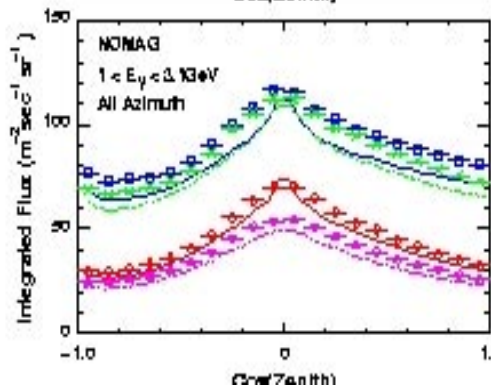
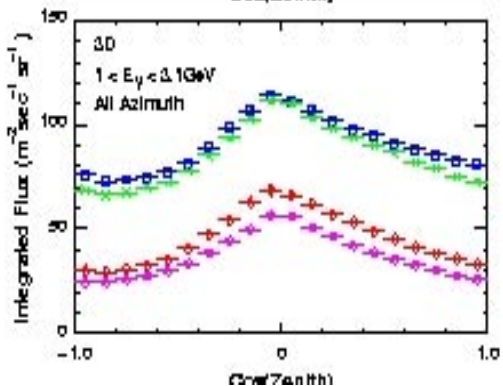
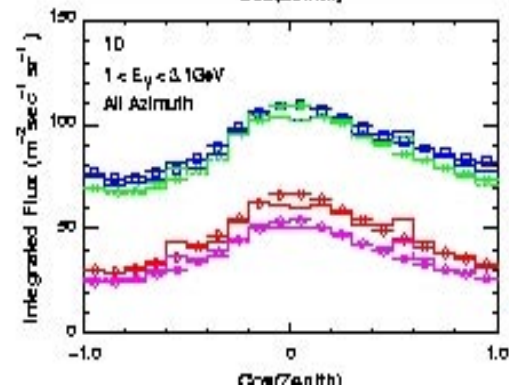
HKKM: confirm horizontal enhancement



1D no cut-off:
 average int. point
 $\sim 100 \text{ gr/cm}^2$
 Horiz. CR produce π at higher altitude than vert. \Rightarrow



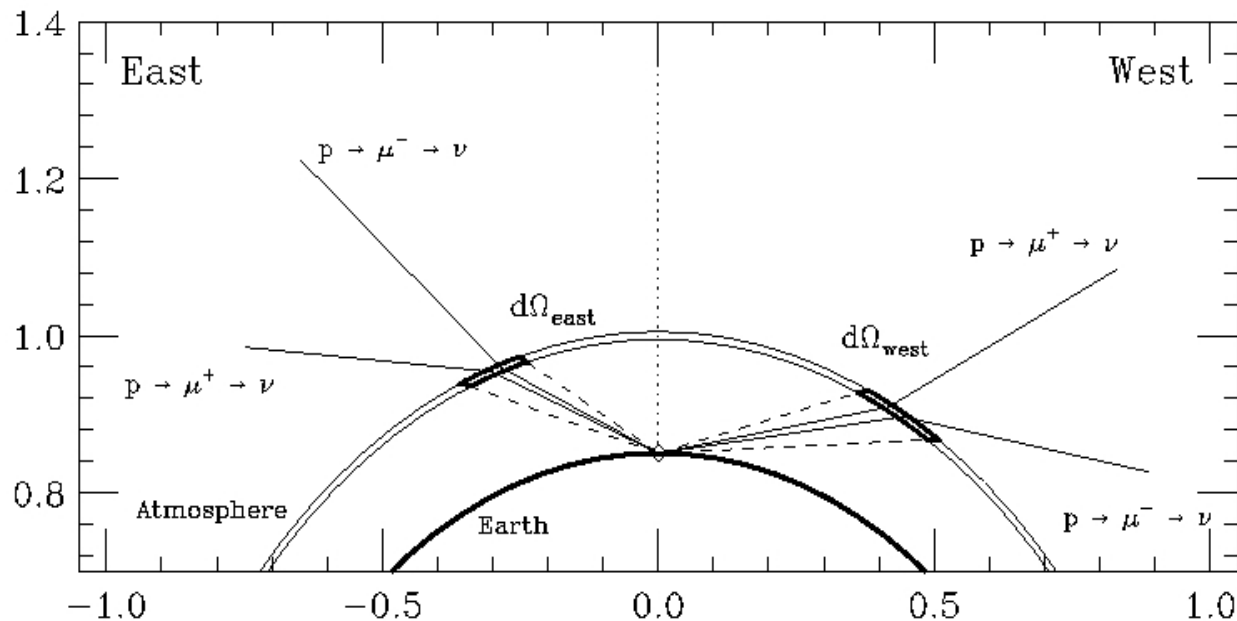
π - μ decay at lower density \Rightarrow int. prob. + μ energy loss increase with air density



Horiz. $v >$ vert. v
 Cut-off modifies zenith dependence
 (@ high magnetic lat. downward $>$ upgoing flux)

1D/3D: μ bending

Effect on E-W asymmetry (predicted in P. Lipari, astro-ph/0003013):



enhancement of asymm.
effect for V_e, V_μ from μ^+

suppression for $\overline{V_e, V_\mu}$
from μ^-

3D with geomagnetic
cut-off can reconcile

SK observation

$A_e > A_\mu$

(while 1D: $A_e = A_\mu$)

From W: for $p \rightarrow \pi^+ \rightarrow \mu^+ \rightarrow \nu$ $\langle \theta_{p\nu} \rangle = \theta_{p\pi} + \theta_{\mu B} < \theta_{p\pi}$

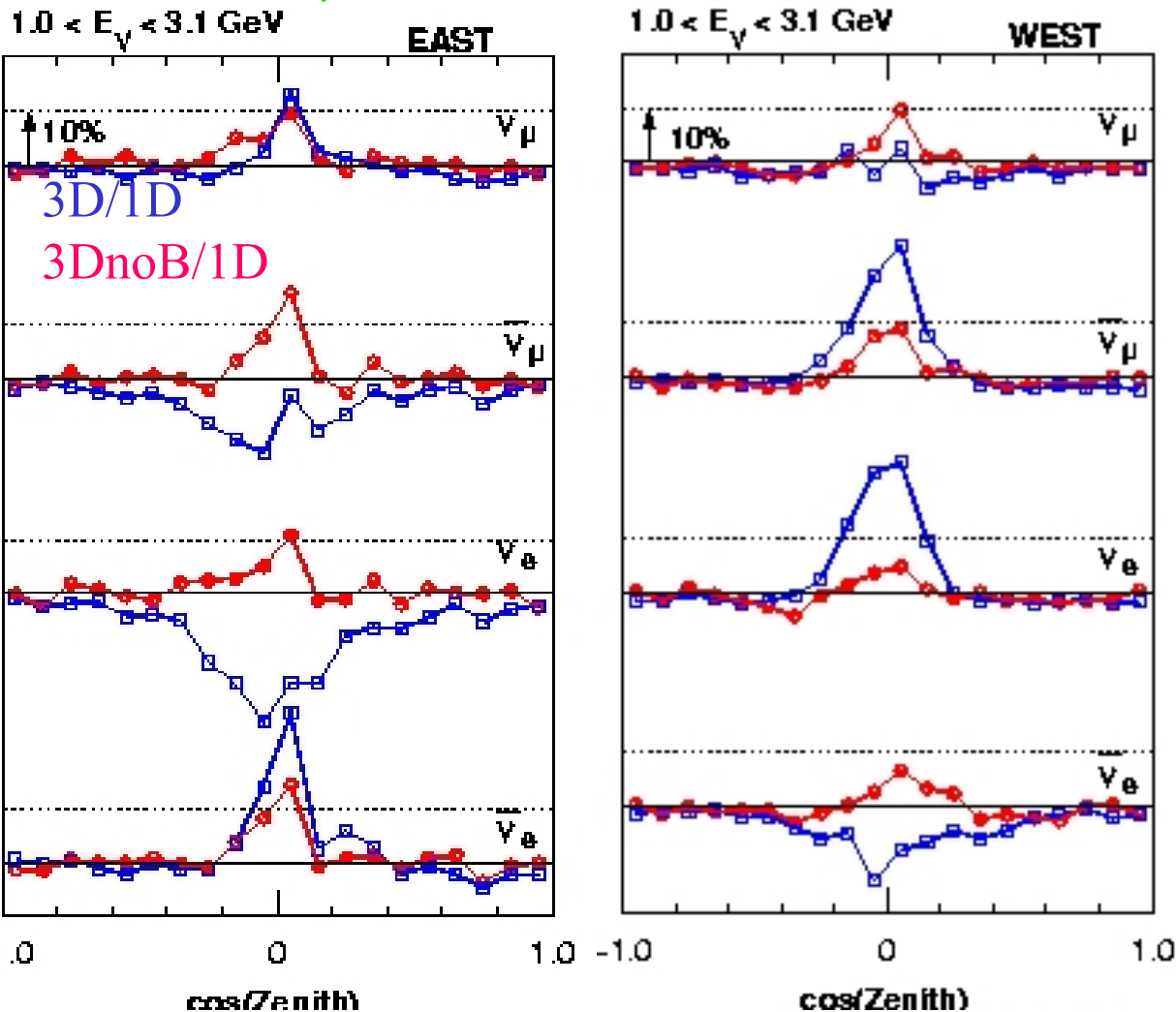
for $p \rightarrow \pi^- \rightarrow \mu^- \rightarrow \nu$ $\langle \theta_{p\nu} \rangle = \theta_{p\pi} + \theta_{\mu B} > \theta_{p\pi}$

From E: opposite effect

$d\Omega \propto \cos \theta_{p\nu}$ and $\Phi_\nu \approx \Phi_{\bar{\nu}} + \sigma_\nu > \sigma_{\bar{\nu}}$

Effect of geomagnetic field in shower development

HKKM: Super-Kamiokande site



3D: shows horizontal increase due to geometry
Geomagnetic field in shower development:
effects $\sim 10\text{-}20\%$ up to $\sim 10 \text{ GeV}$ almost independent on E_ν (when μ decay)

It is a precision check on geomagnetic treatment

These effects have small Impact on Δm^2

FLUKA setup

FLUKA2000 interaction and transport code

(A. Ferrari et al., Proc. of CALOR2000):

theory driven approach not phenomenological/tuned on experimental data

Conservation laws fulfilled *a priori* Extensive benchmark against data

h-A interactions based on resonance production and decay below **few GeV**

and on Dual Parton Model and h-A+A-A Glauber model to **tens of TeV**

The setup for atmospheric vs:

3D representation of Earth and atmosphere (50-100 shell) to ~100 km (0.1 gr/cm²)

with Shibata "standard atm" profile; all secondaries can be scored

Primary particles injected at ~100 km sampled from Bartol flux at solar min

Solar modulation from NASA tables and algorithms using Climax data

For μ benchmarks: cut-off+shower development through **back-tracing**

For vs: cut-off only (to be improved)

Superposition model will be replaced by DPMJET using nuclear projectiles

Change in primary spectrum can be obtained just through weighting

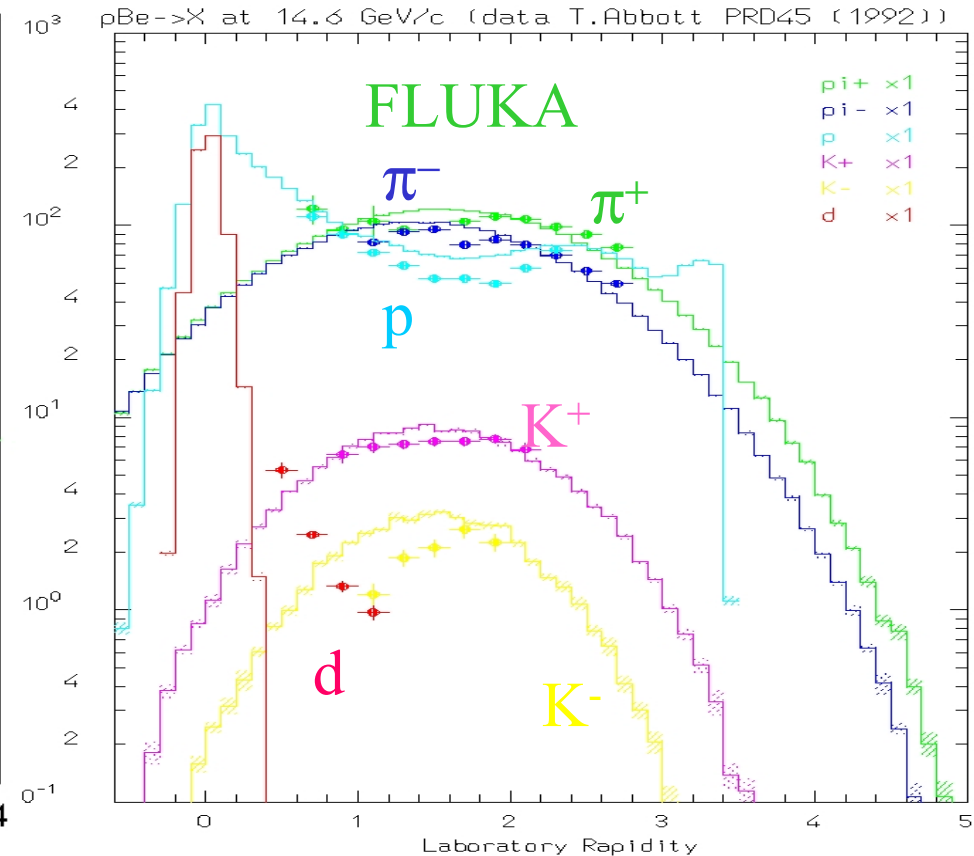
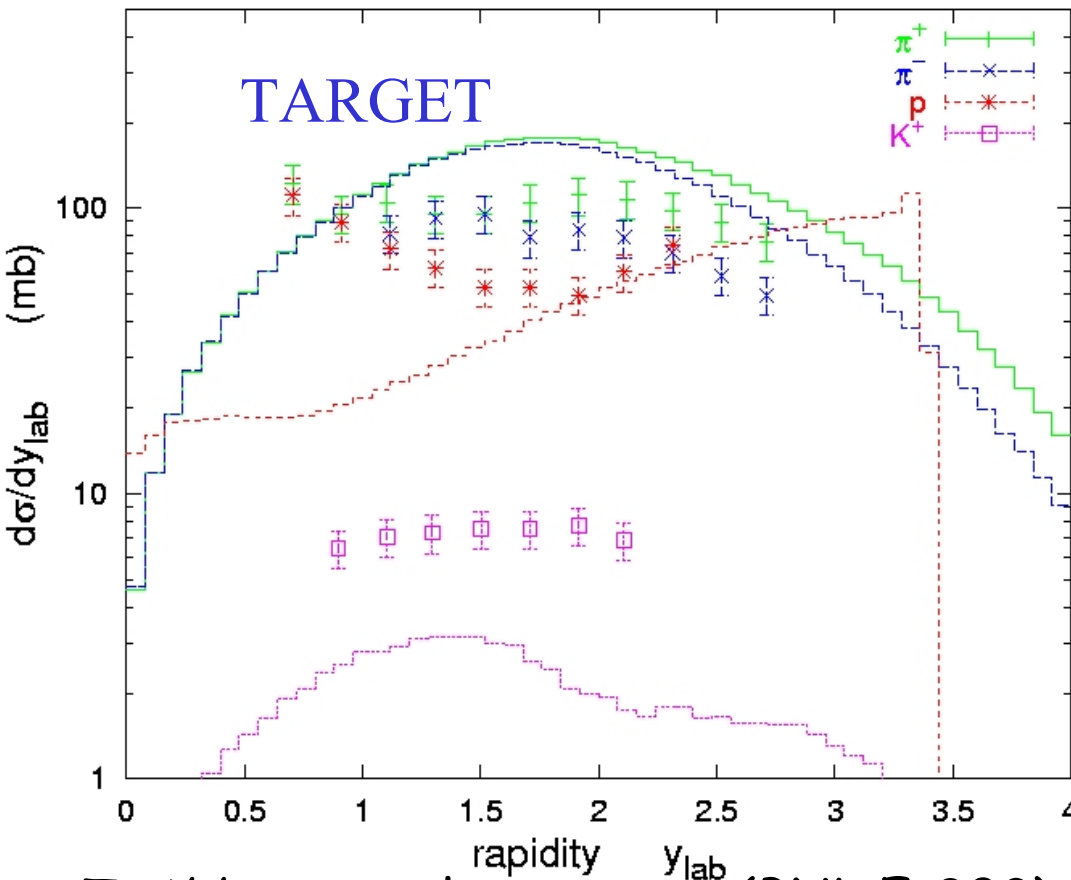
All relevant physics: polarization in decays, energy losses, multiple scatter.

FLUKA atm. v simulation will be used by ICARUS

Used for CNGS beam project, tested in Nomad and comparison with SPY

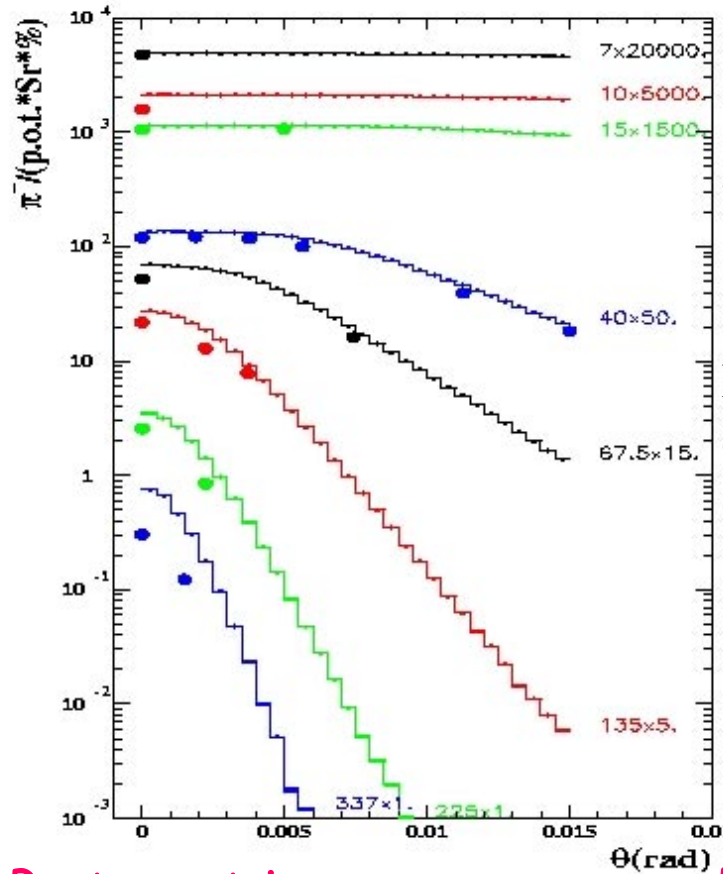
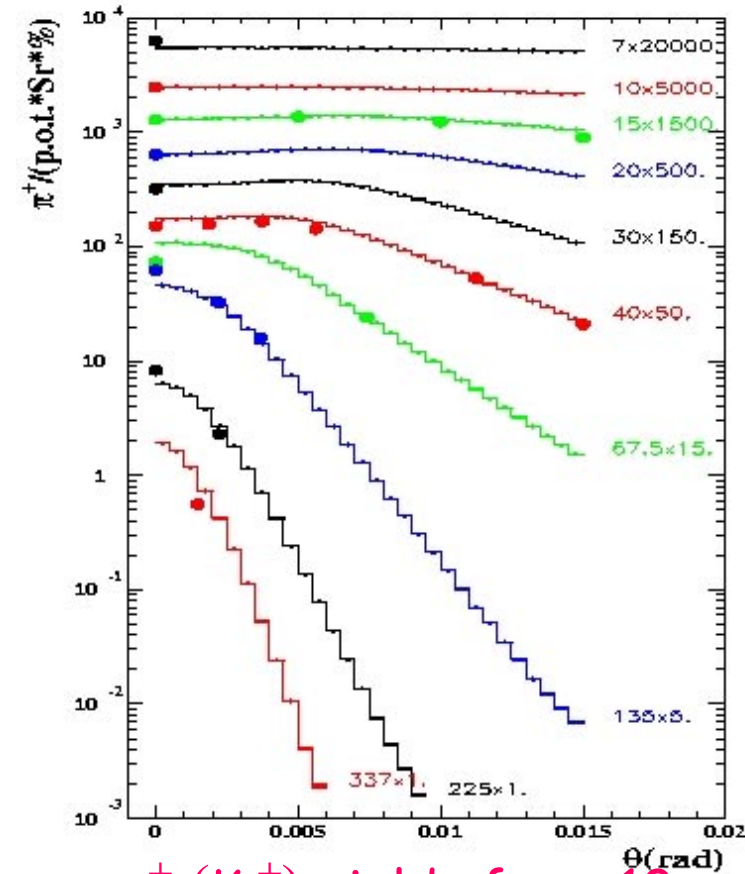
Interaction models: FLUKA/TARGET

p Be collisions at 14.6 GeV



T. Abbott et al. PRD45(1992) (BNL E-802): explored different targets (Be, Al, Cu, Au) at single lab energy, lab angle 5° - 58° , $X_{lab} \Rightarrow 0.1$ where most differences between atm. calculations but extrapolations needed to obtain dN/dx_{lab} from rapidity distributions

FLUKA: benchmarks



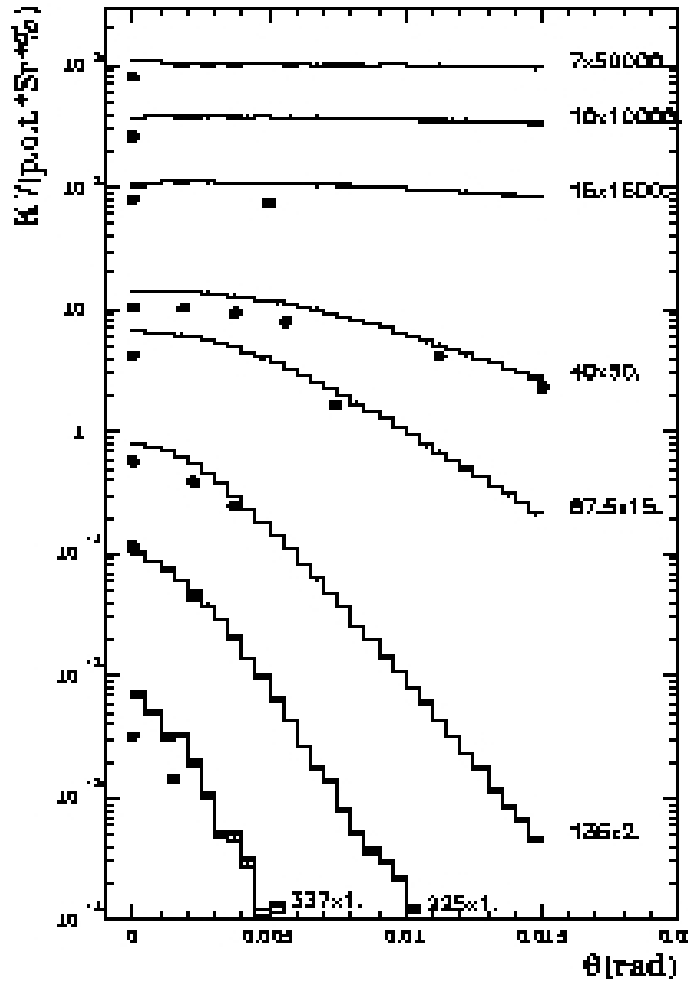
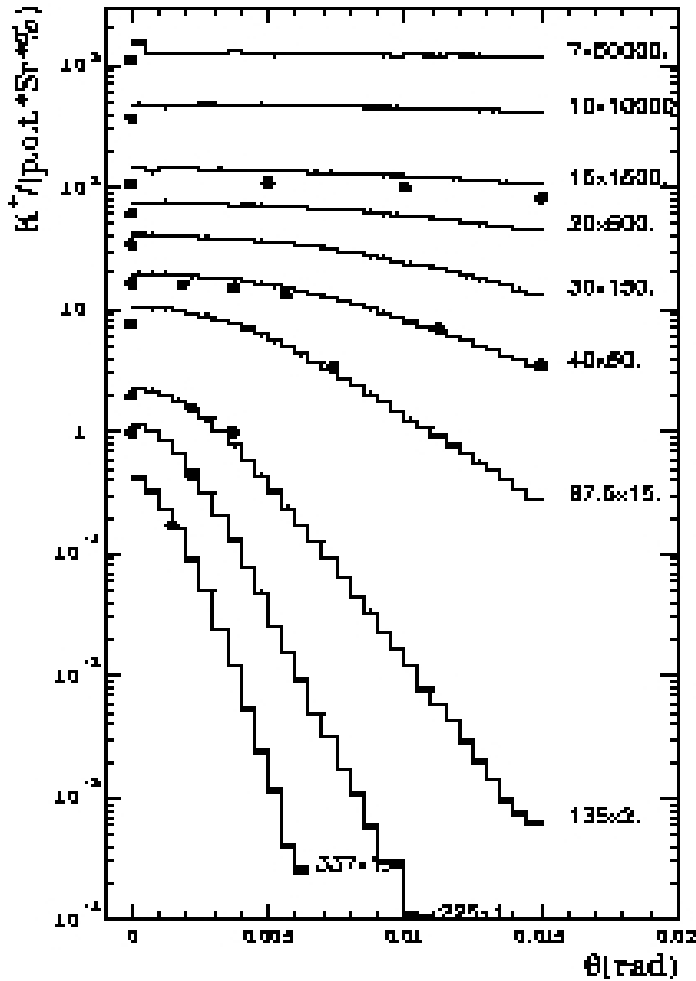
FLUKA compared to SPY: p(450 GeV/c) +Be with 3% precision on K/ π for p < 40 GeV/c (Ambrosini et al., Eur Phys JC10(1999) and Atherton et al. (CERN rep80-07) p(400 GeV/c)+Be for p > 67.5 GeV

π^\pm (K^\pm) yields from 10 cm Be target in p ranges vs production angle

Agreement at 20% (except for few points for K^-) and K/ π at 10% @ 30-100 GeV/c Important comparison for atm vs but small angle and large E_p

HARP: $E_p \sim 2-15$ GeV on thin and thick different targets, $d^2\sigma/dp_T dp_L$ 2% precision large solid angle (previous meas. have ~15% uncertainty)

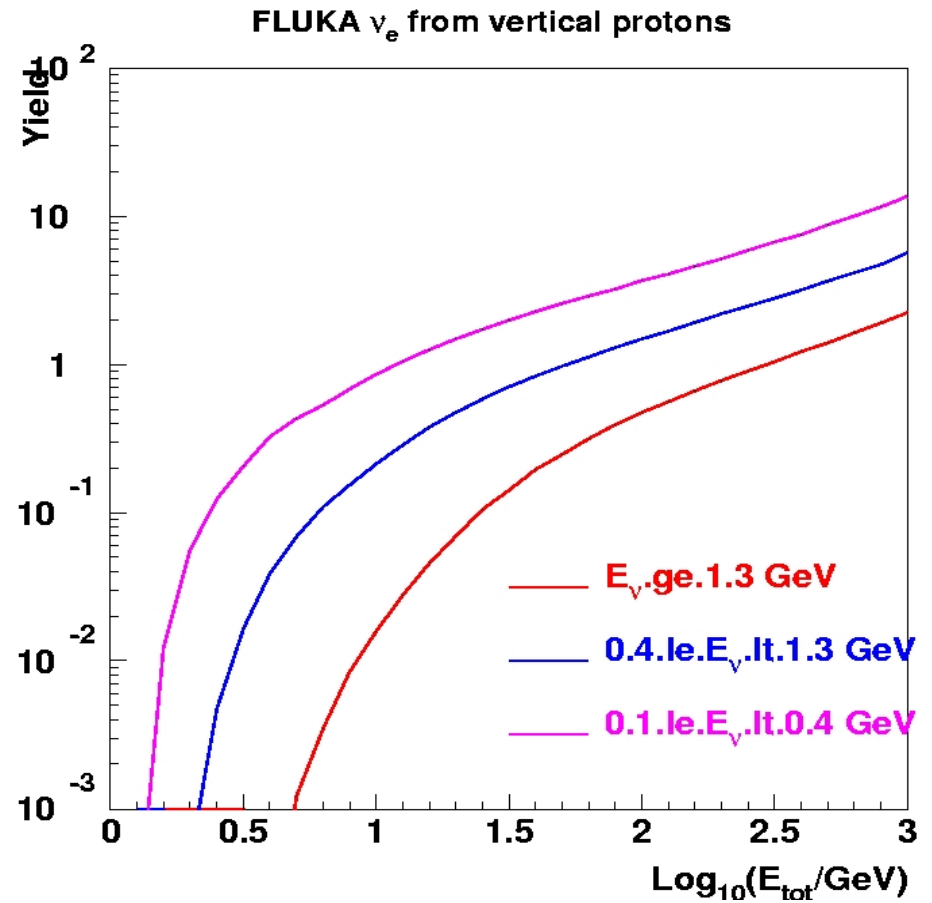
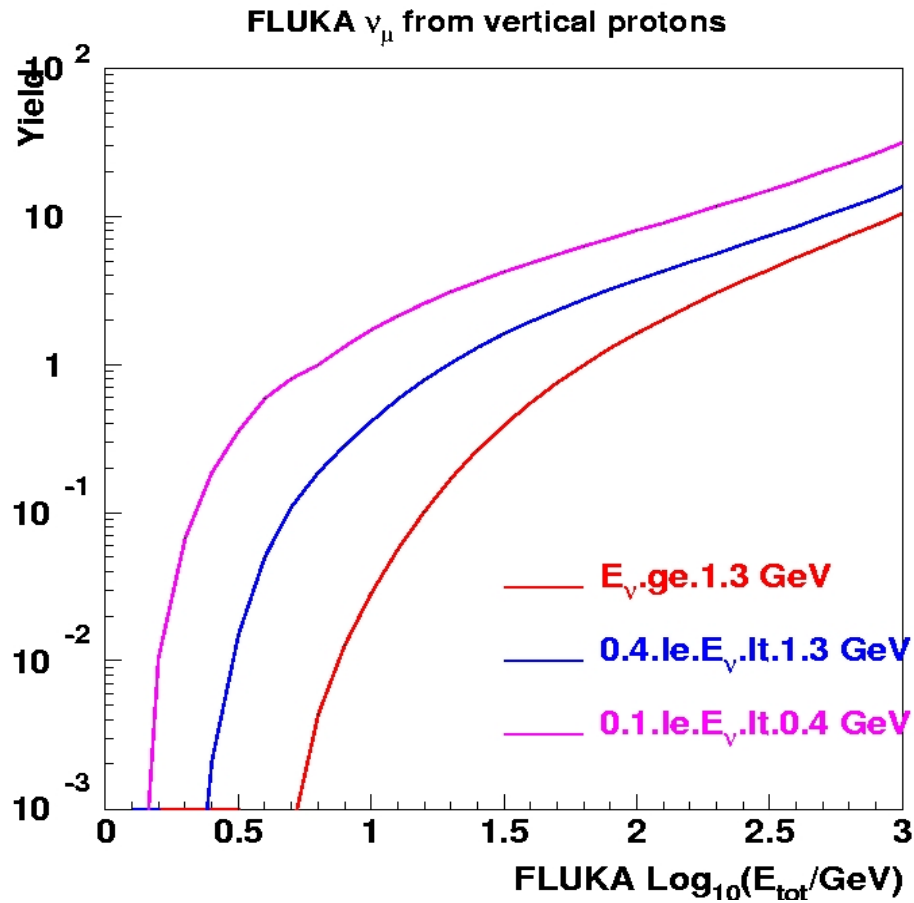
FLUKA: benchmarks



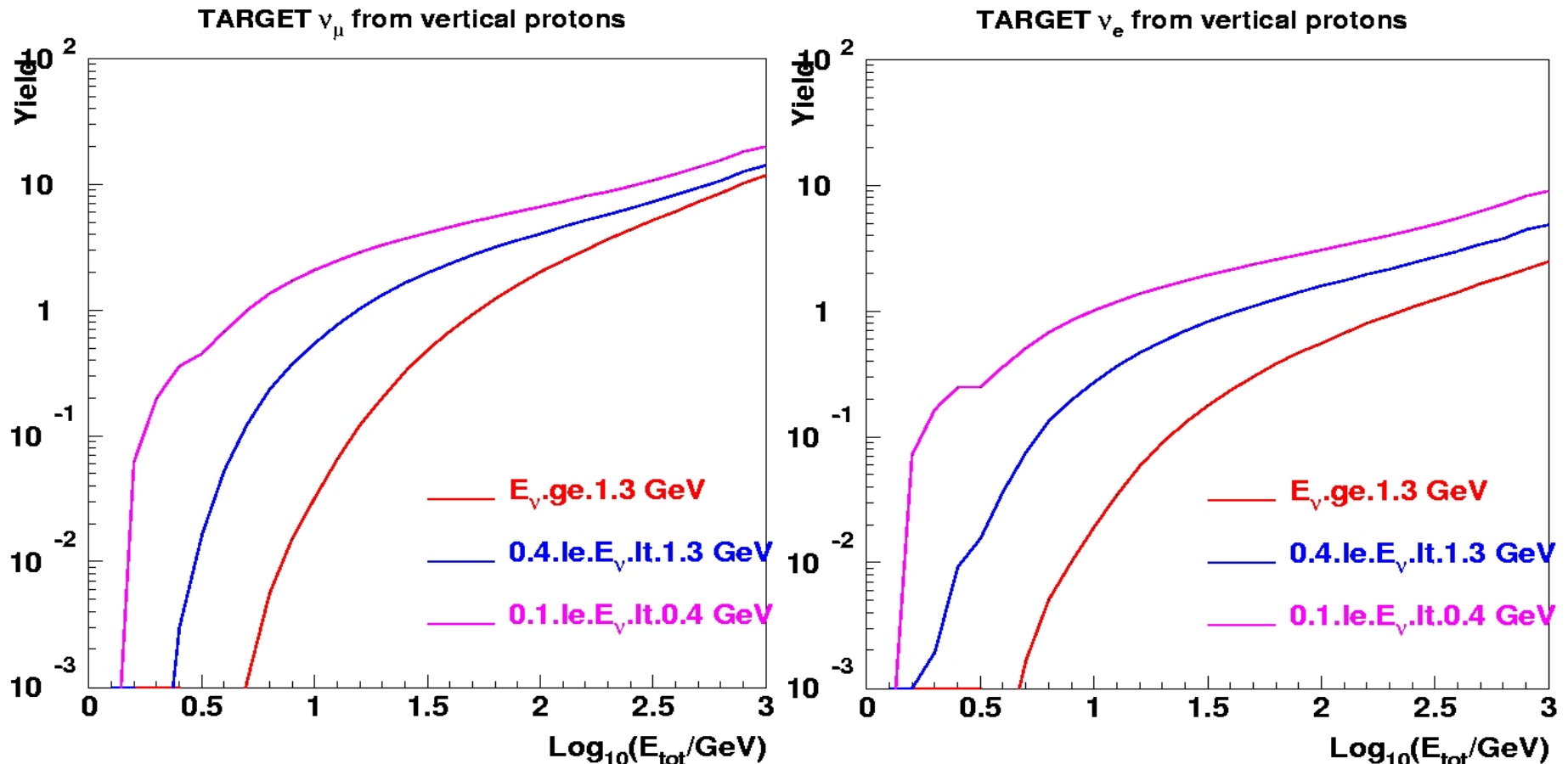
FLUKA compared to SPY
p(450 GeV/c)+Be with 3% precision on K/π for $p < 40 \text{ GeV}/c$ (Ambrosini et al., Eur Phys JC10(1999) and Atherton et al. (CERN rep80-07) p(400 GeV/c)+Be for $p > 67.5 \text{ GeV}$

K^\pm yields from 10 cm Be target in momentum ranges vs production angle

FLUKA/TARGET: ν yields



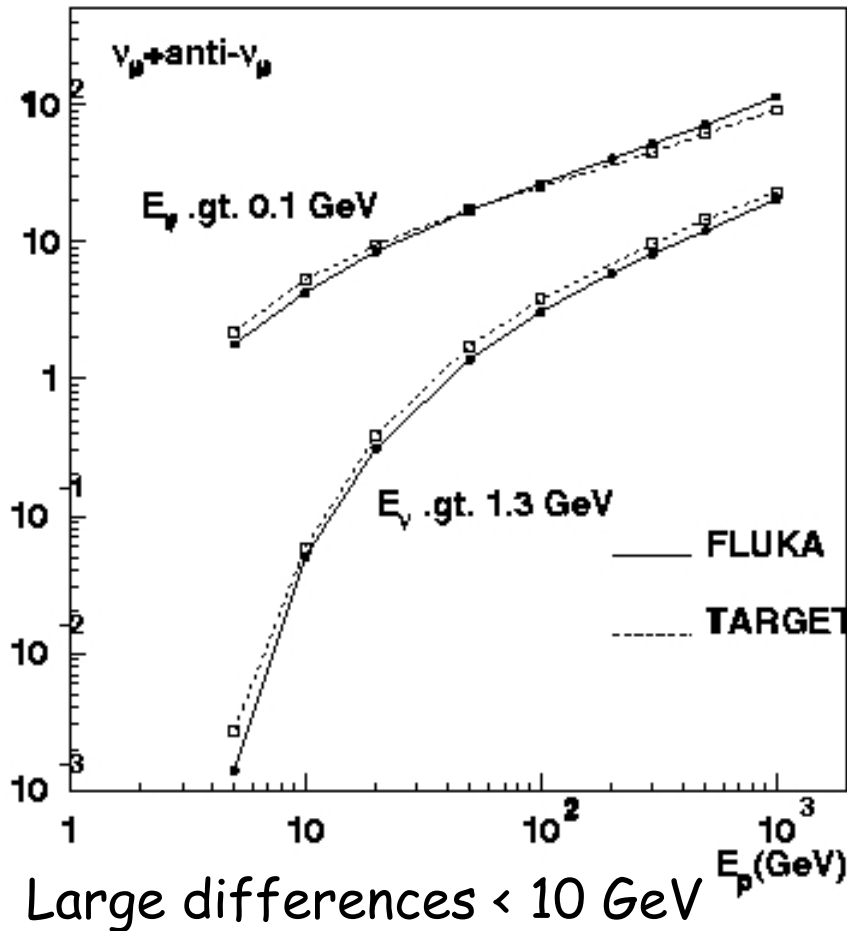
FLUKA/TARGET: ν yields



From extensive comparison we learnt: TARGET gives too high π multiplicity @ small $x = E/E_0$. Next future: **new 3D TARGET (ICRC)**
No model is perfect, all need continuous benchmark against data

FLUKA/TARGET

Vertical Proton Showers

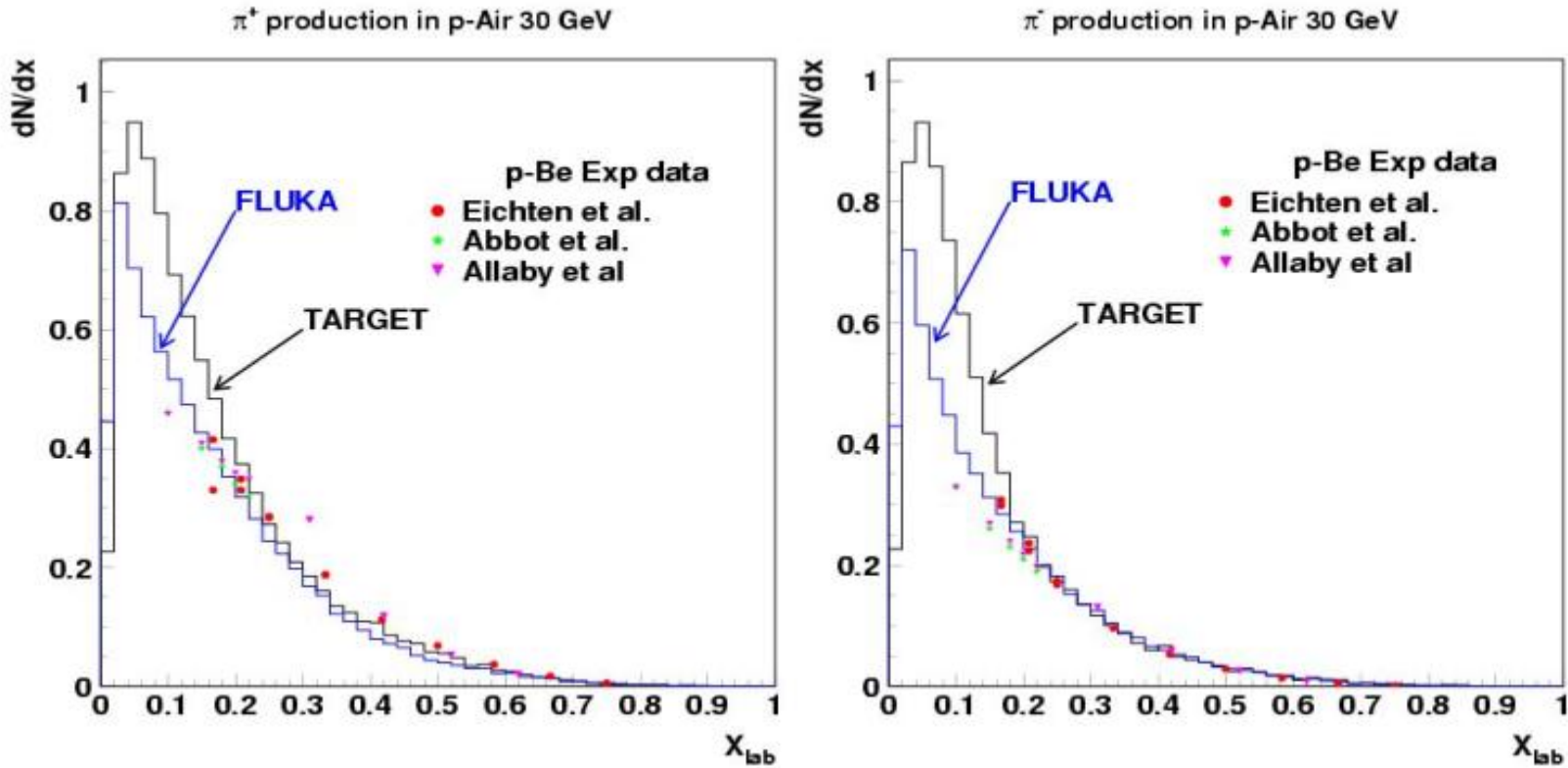


At HE FLUKA produces softer ν s

Warning: from ν fluxes to detected rates uncertainties on ν cross sections are relevant
Larger for $E_\nu \sim 0.1-10 \text{ GeV}$ (quasi-elastic interactions, resonance production, nuclear effects, transition in DIS regime)
Need of higher precision data (K2K, LBL near detectors)

Average n. of atm ν_μ produced by vertical protons

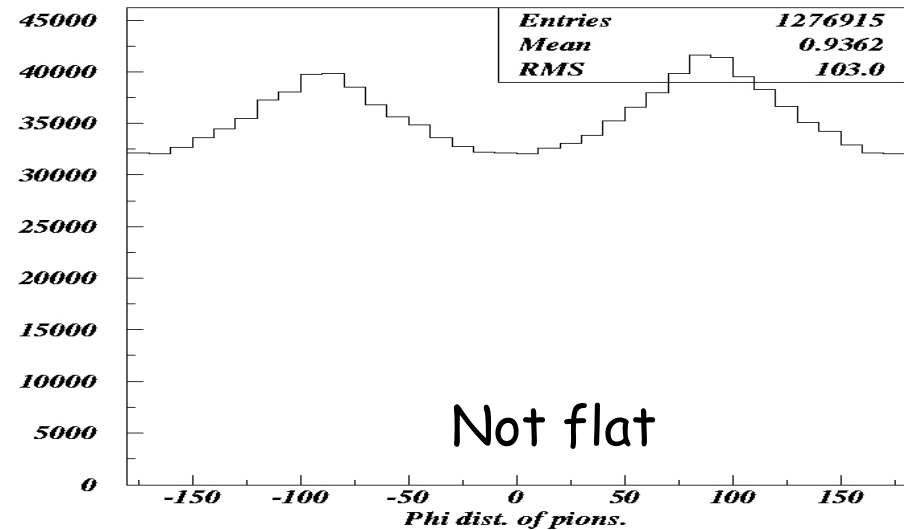
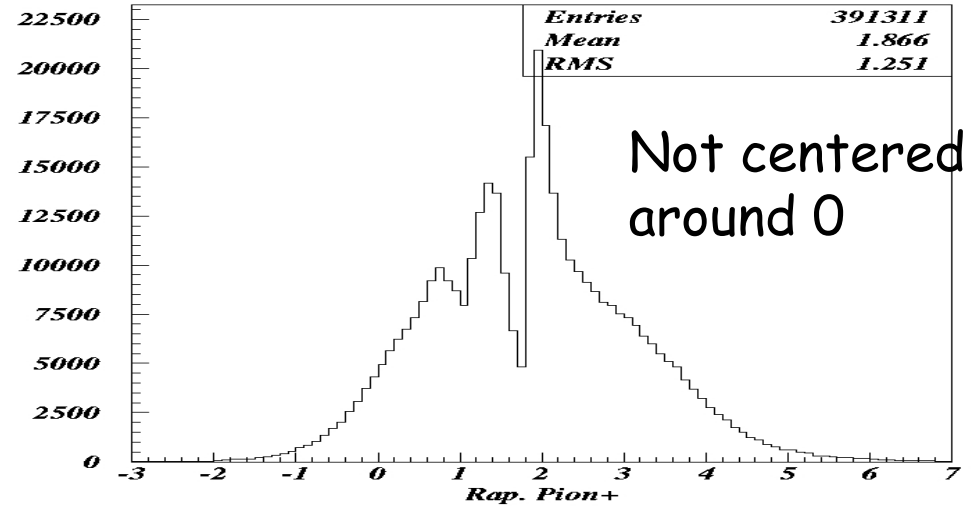
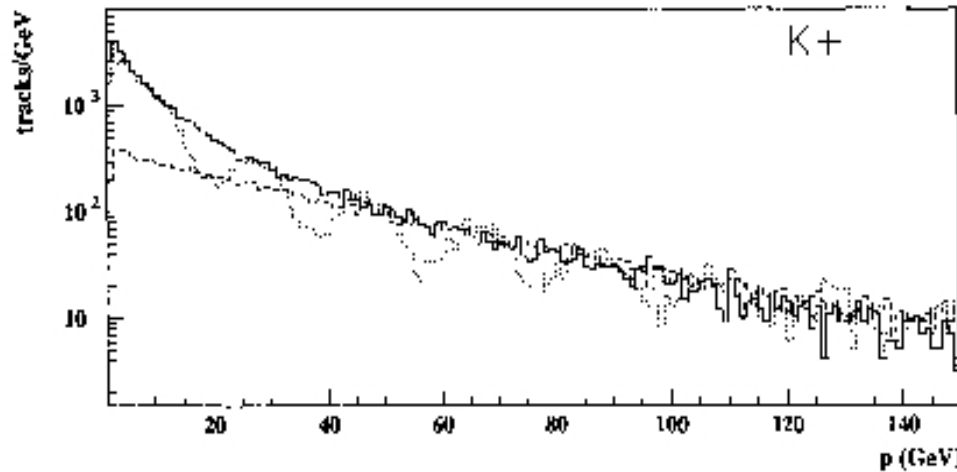
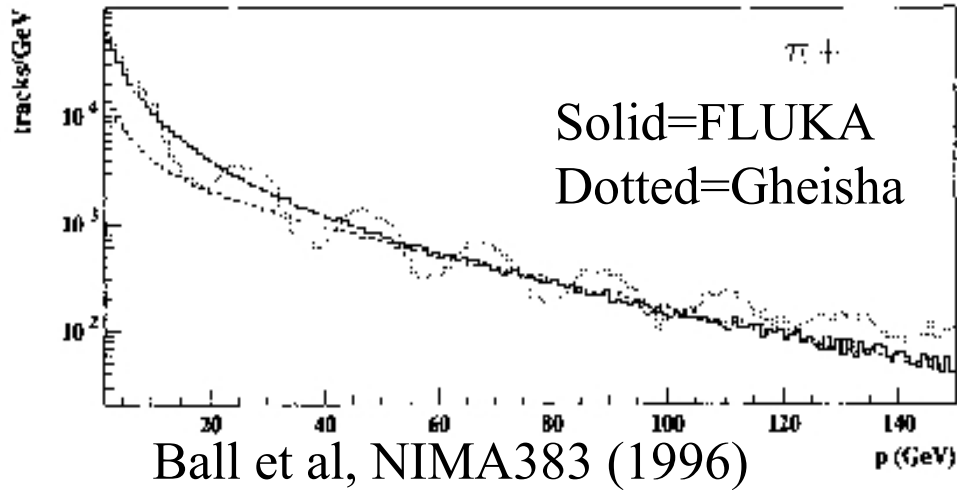
FLUKA/TARGET



Fluka predicts that a smaller fraction of primary energy goes into charged pions \Rightarrow smaller ν fluxes

Gheisha

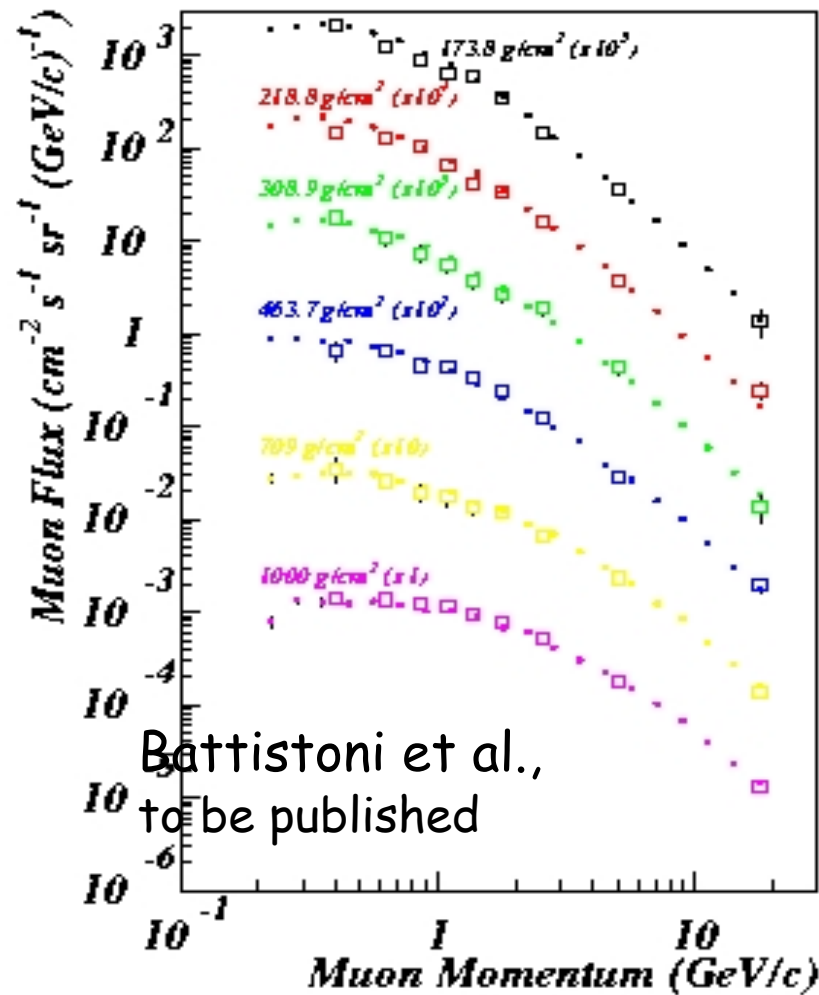
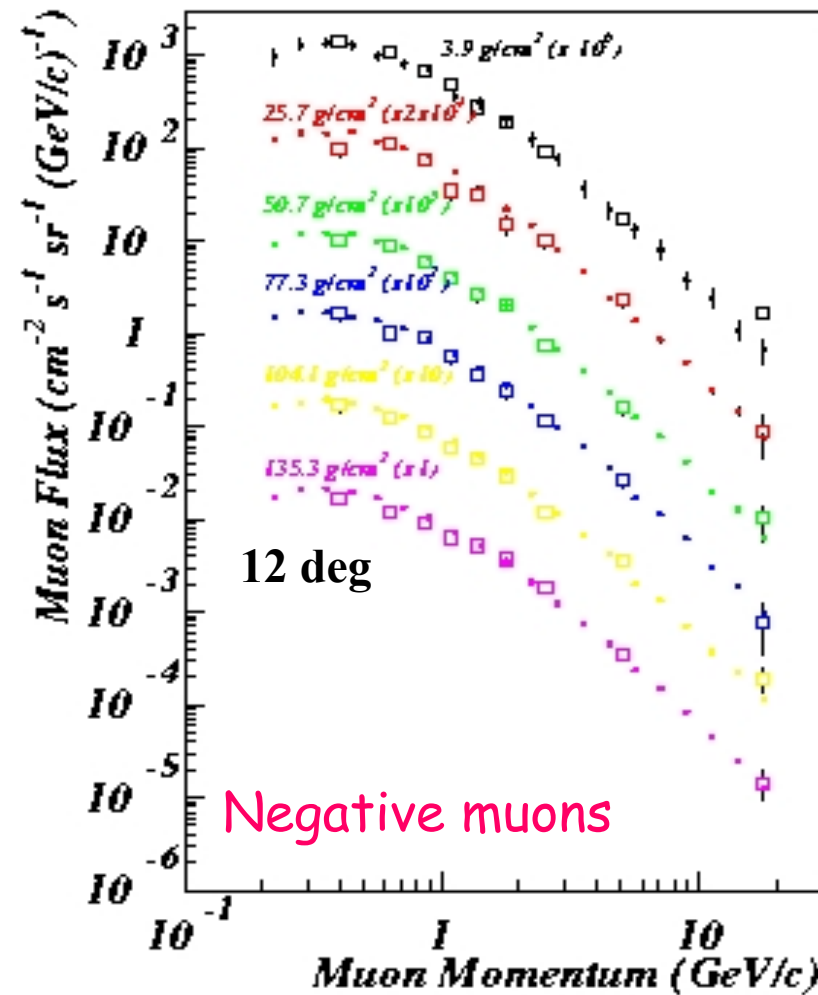
Production spectra of π^+ and K^+
for 400 GeV incident p
Used in Plyaskin, hep-ph/0103286



FLUKA floating muon benchmark

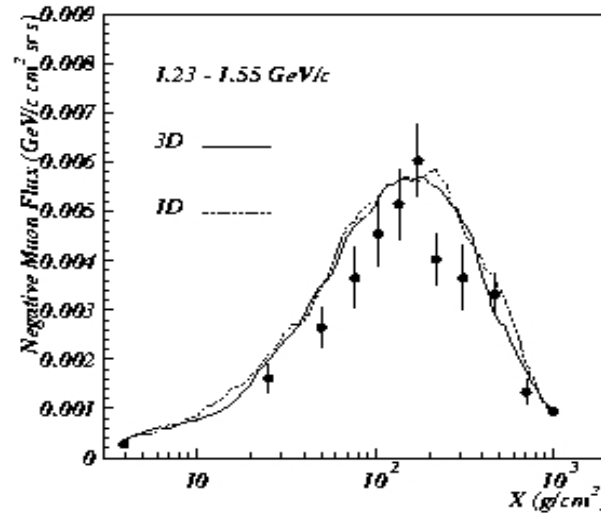
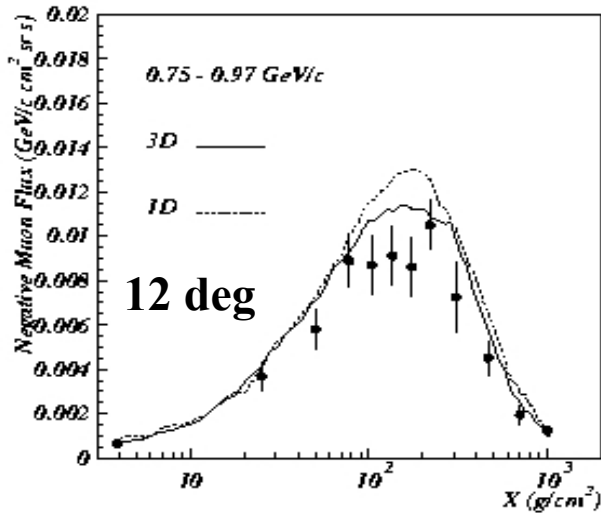
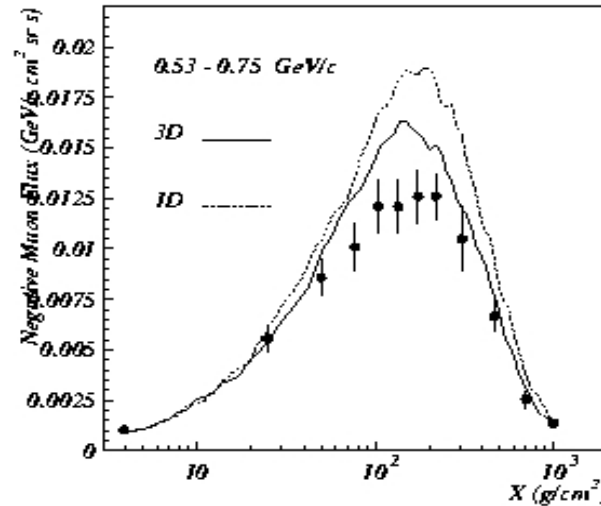
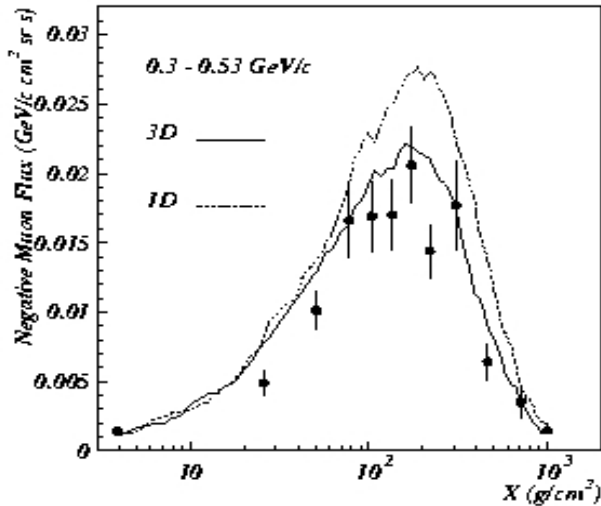
Important benchmark to validate V calculations (same parents, shower development check)

Differences TARGET/FLUKA: not due to FLUKA insufficient particle production



CAPRICE 94
(Lynn Lake)
FLUKA 3D,
100 standard
USA atm.
shells, Bartol
all-nucleon
spectrum
modulated
with Climax
n data,
geomagnetic
field in
shower
development

Floating muon benchmark: 3D/1D



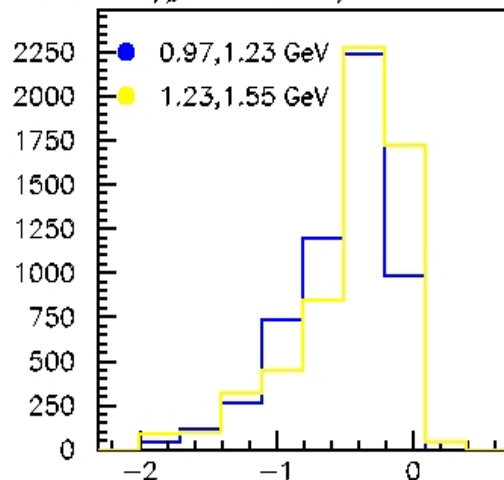
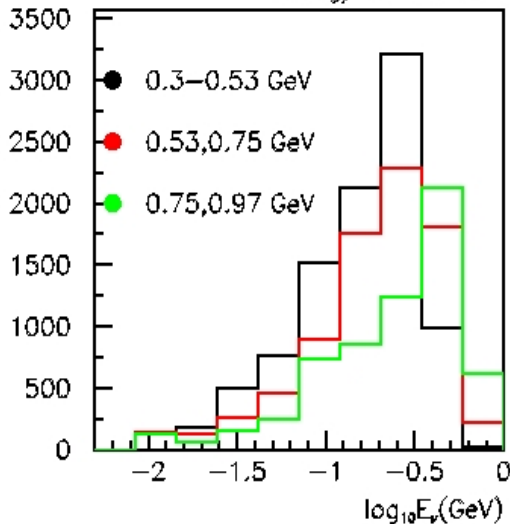
1D brings overestimate at low p_μ : kinematic angles + bending in geomagnetic field \Rightarrow increase of path-length and larger decay probability
Better agreement than 1D by Fiorentini et al.
(produces lower fluxes at low energies)

Warning: still Bartol CR flux

Negative muons

Correlation between muons and neutrinos

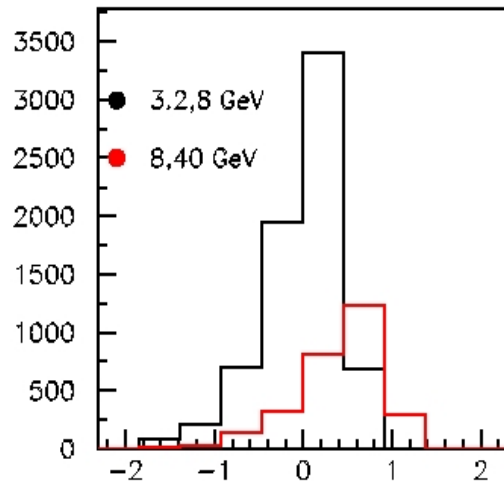
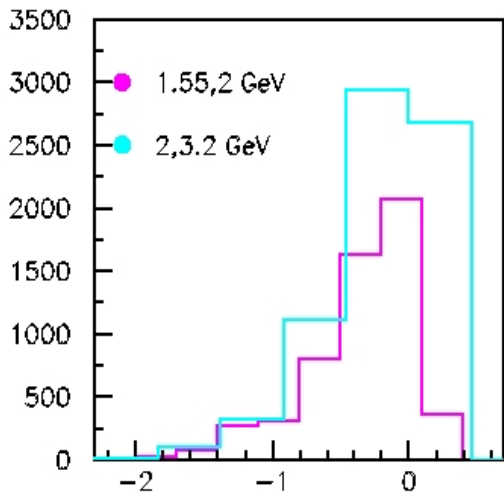
ν energy distribution in intervals of p_μ for π decay



Caprice 94 μ s constrain Sub-GeV events

Average ν energies in μ momentum intervals:

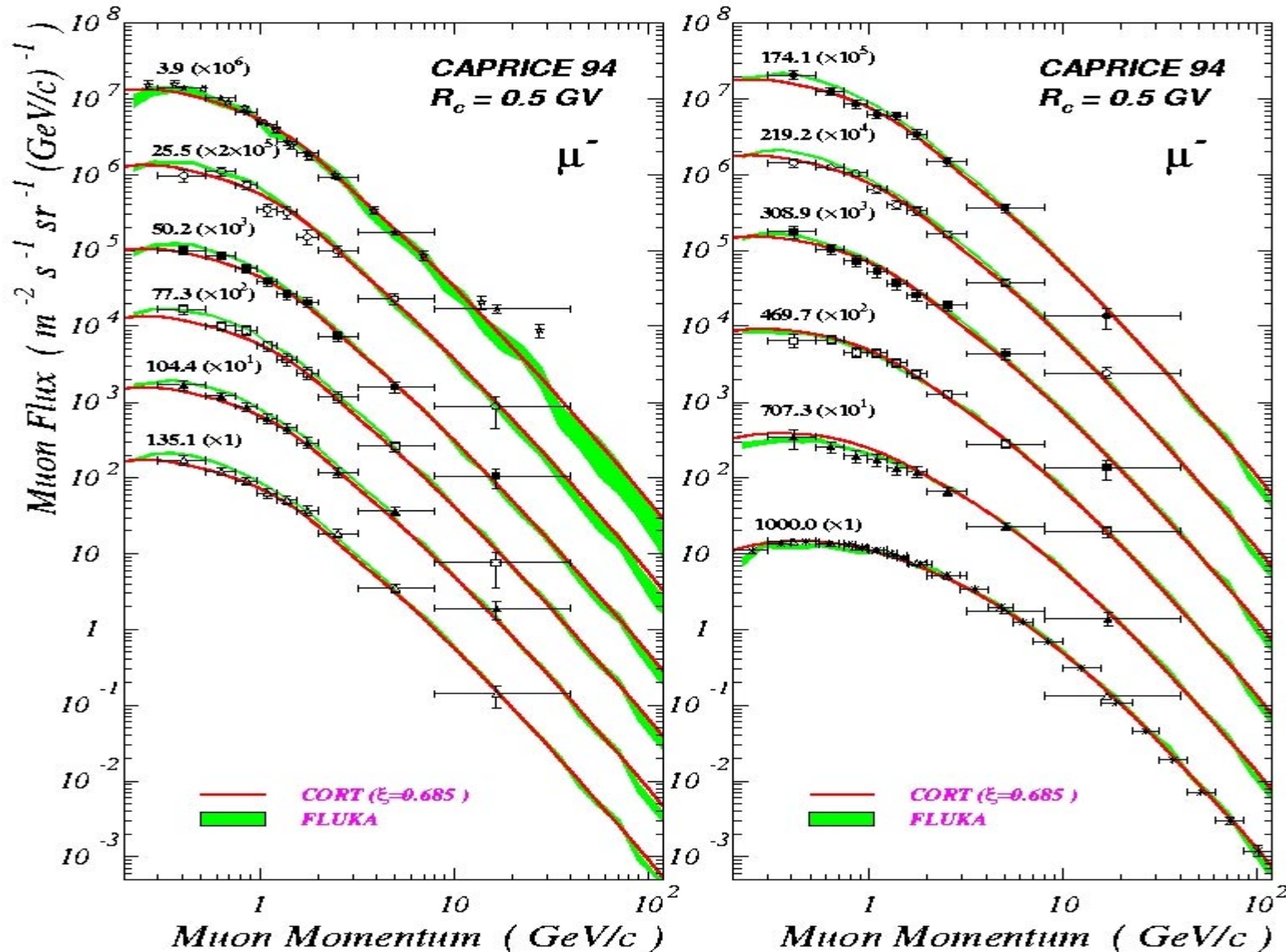
p_μ GeV/c $\langle E_\nu \rangle$ GeV Frac. of primaries with $E < 10$ GeV



0.3 - 0.53	0.19	42%
0.53 - 0.75	0.25	34%
0.75 - 0.97	0.32	28%
0.97 - 1.23	0.39	22%
1.23 - 1.55	0.48	18%
1.55 - 2	0.60	13%
2 - 3.2	0.89	5%
3.2 - 8	1.44	0.6%
8 - 40	3.28	0%

$\log_{10} E_\nu$

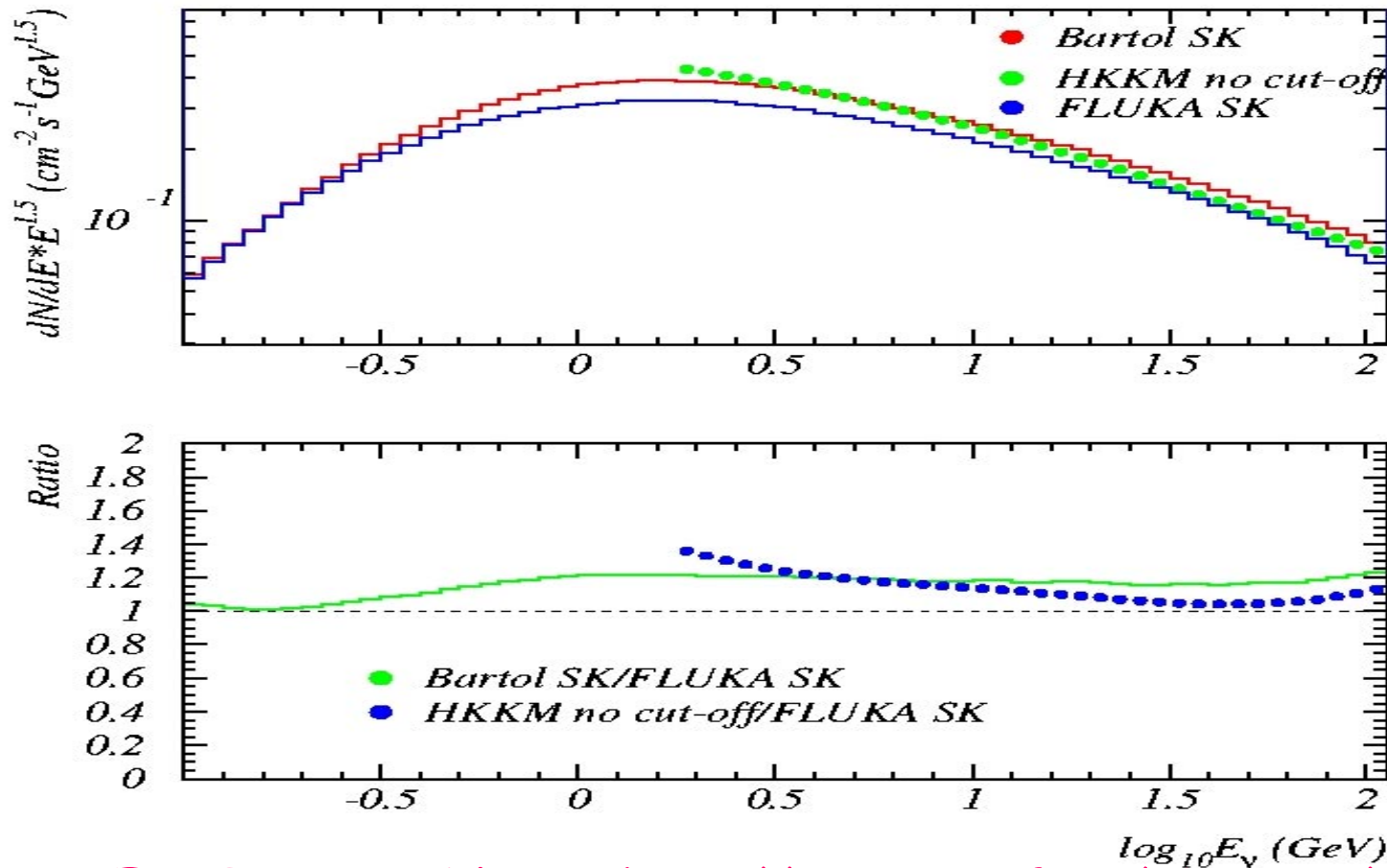
Correlation between muons and neutrinos



Thanks to
V.A. Naumov

Comparison of absolute $\nu_\mu + \text{anti-}\nu_\mu$ fluxes

Averaged over solid angle $\nu_\mu + \text{anti-}\nu_\mu$ fluxes Solar min SK



HKKM: no cut-off

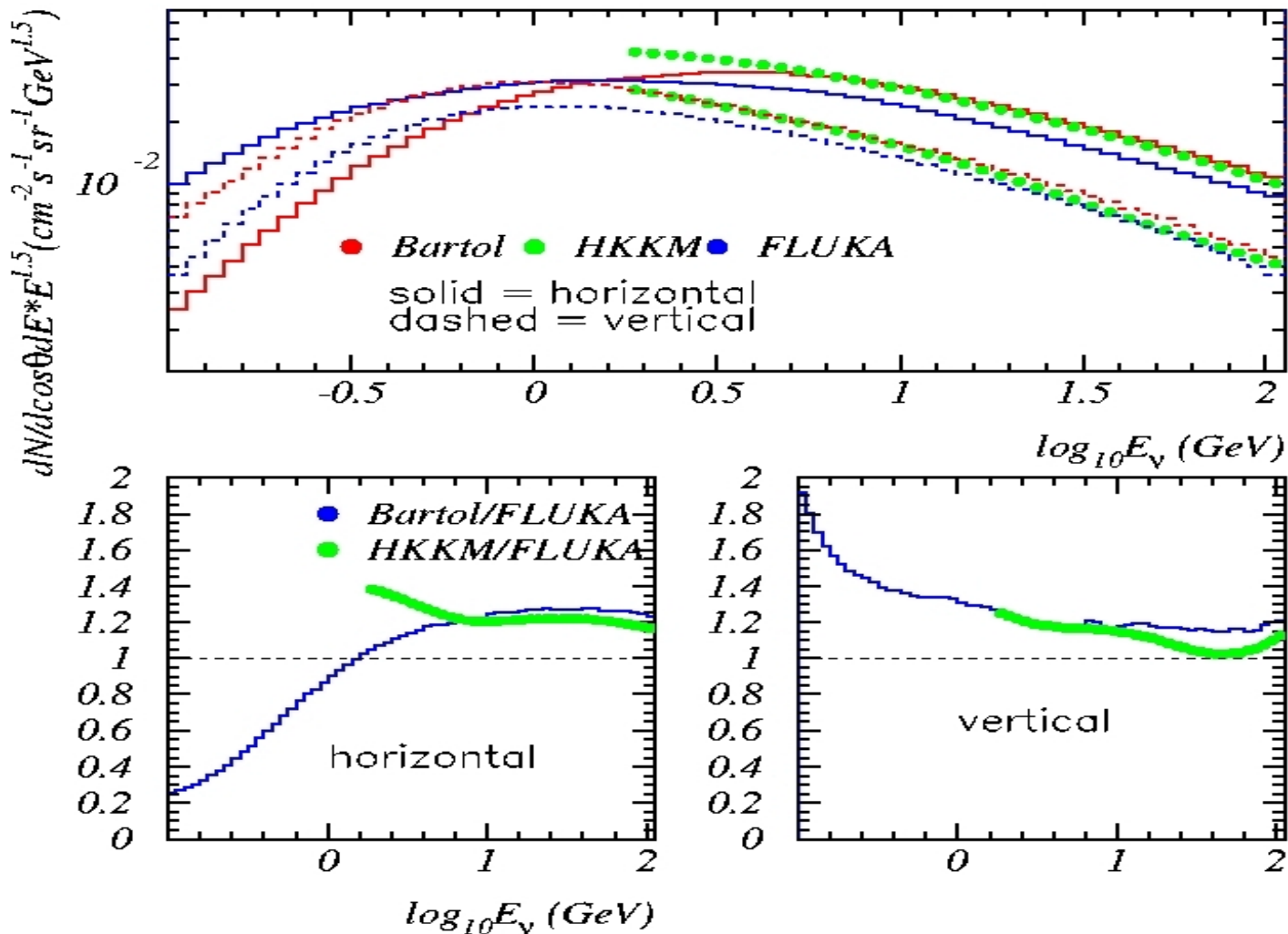
Average fluxes agree inside 20%

FLUKA predicts lower fluxes than TARGET due to lower π multiplicities

NEW FLUKA tables at <http://www.mi.infn.it/~battist/neutrino.html>:
introduced solar mod. (new CR flux will be introduced through weights)

Comparison of vertical and horizontal ν_μ +anti- ν_μ fluxes

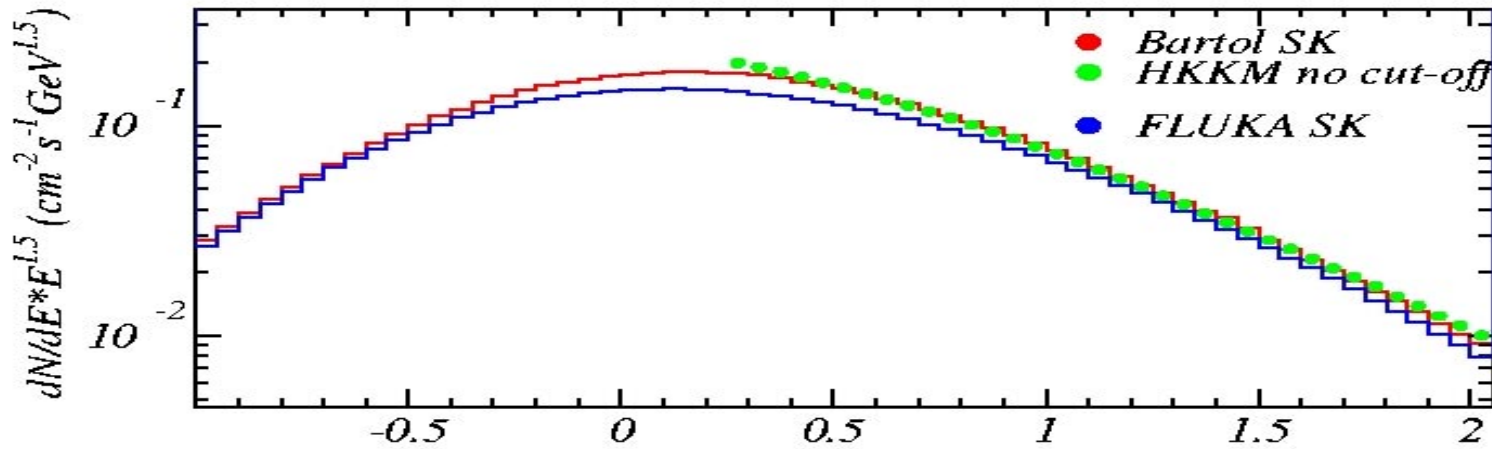
Vert. and Horiz. ν_μ +anti- ν_μ fluxes Solar min SK



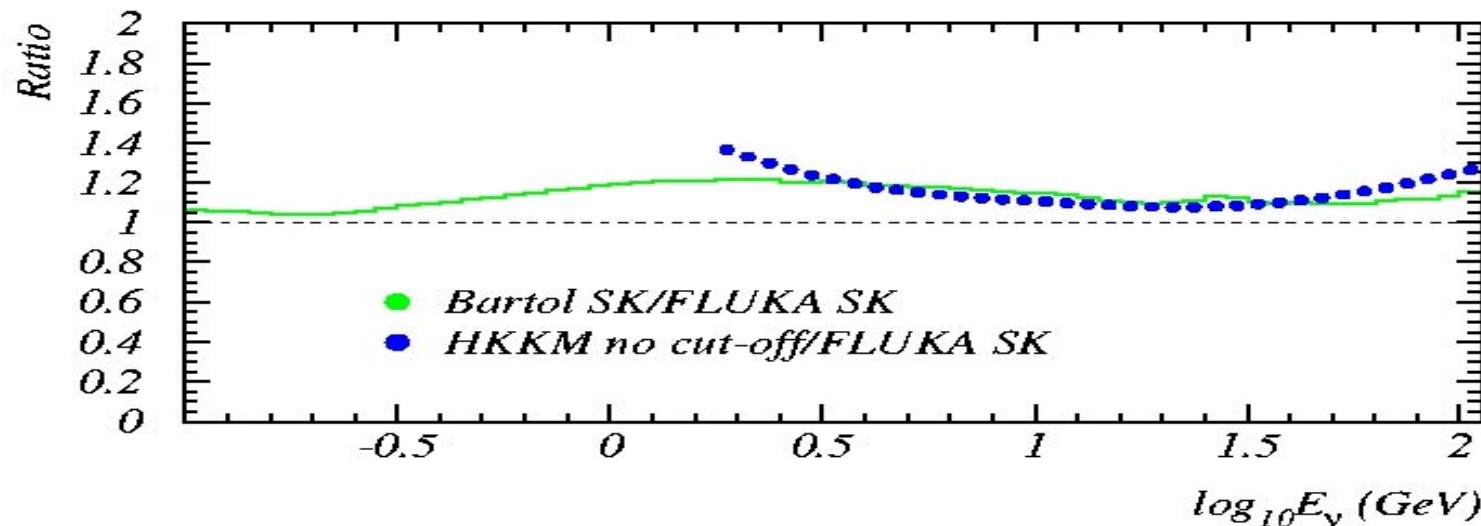
For $E_\nu < 600$ MeV
 FLUKA 3D
 produces larger
 fluxes than Bartol
 at the horizon,
 lower at the
 vertical

Comparison of absolute ν_e +anti- ν_e fluxes

Averaged over solid angle ν_e +anti- ν_e fluxes Solar min SK

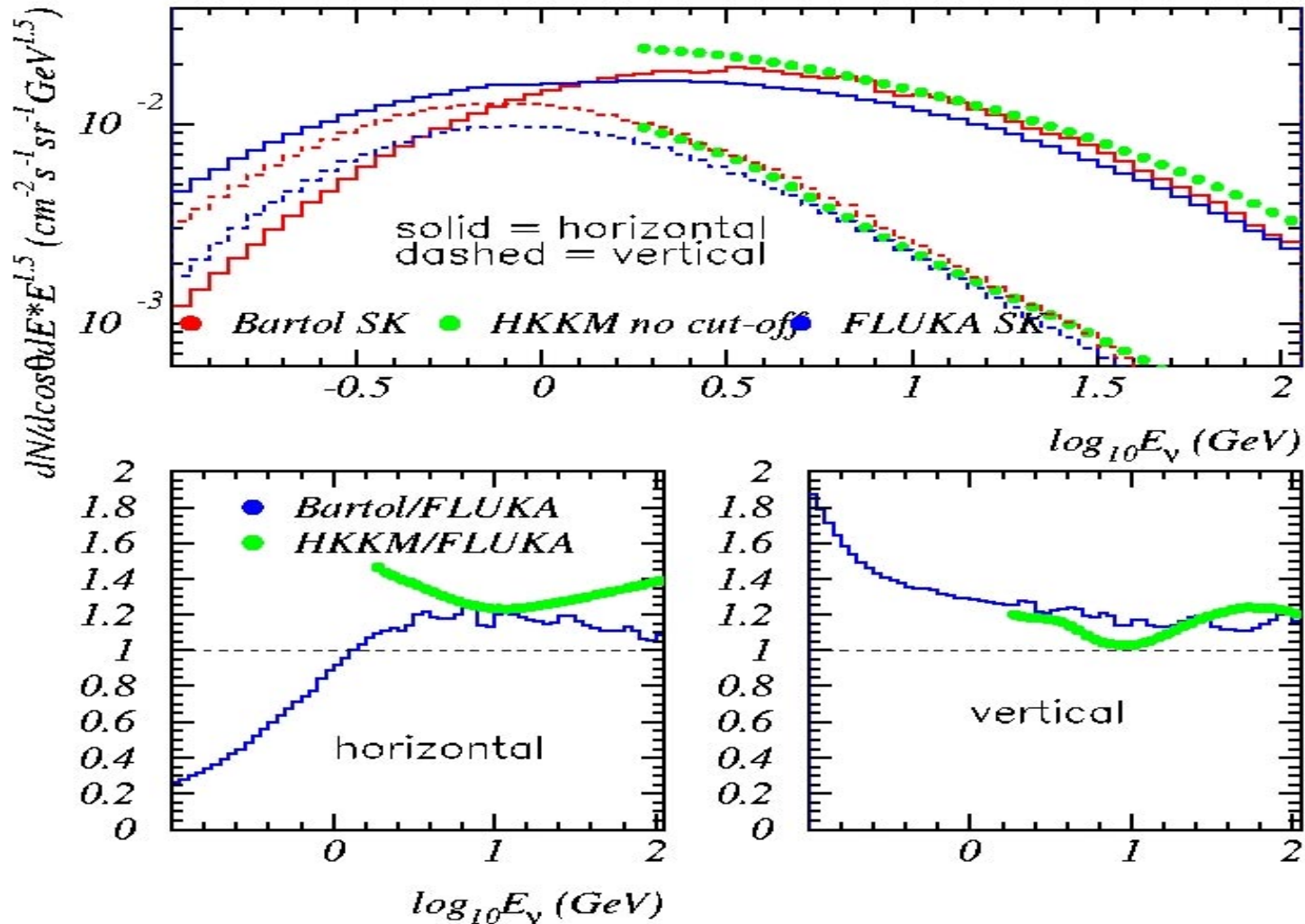


Average fluxes agree inside 10-20%



Comparison of vertical and horizontal ν_e +anti- ν_e fluxes

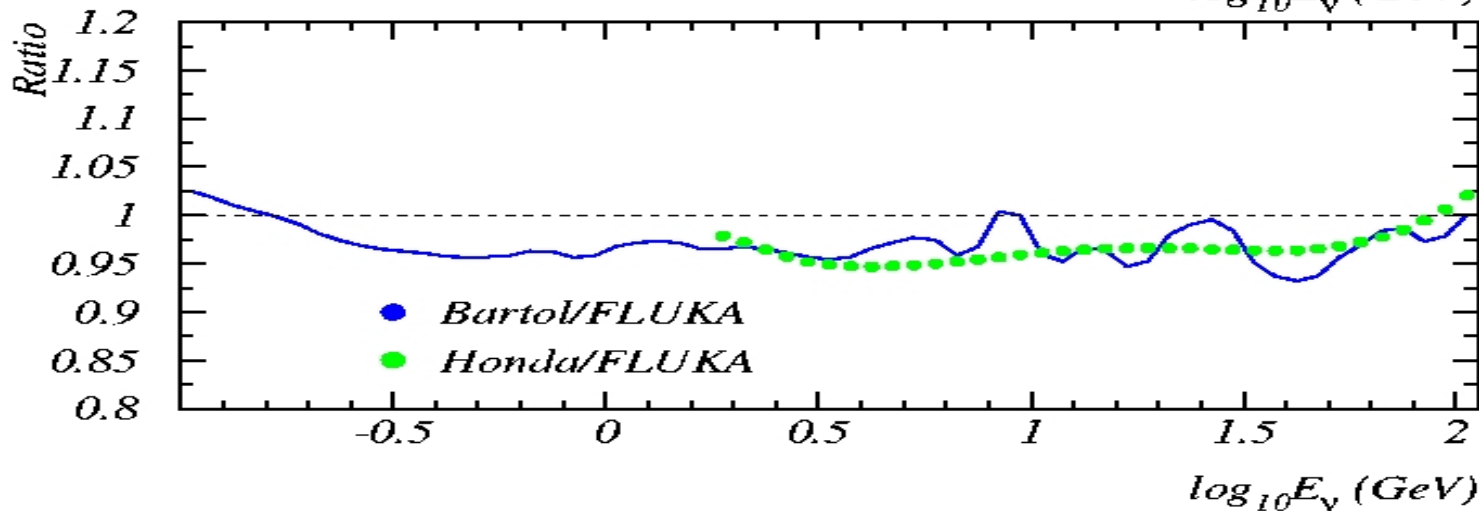
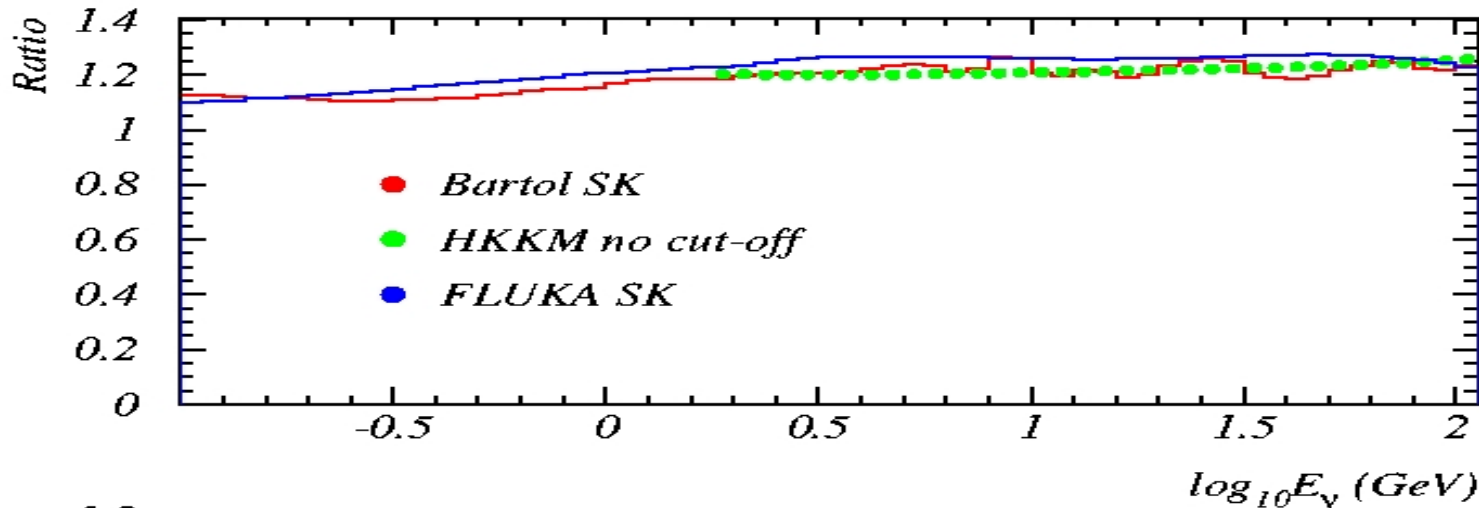
Vert. and Horiz. ν_e +anti- ν_e fluxes Solar min SK



For $E_\nu < 600$ MeV
 FLUKA 3D
 produces
 larger fluxes at
 the horizon,
 lower at the
 vertical

Charge ratio comparison: $\nu_e/\text{anti-}\nu_e$

ν_e/N_e Solar min SK



No experiment has measured charge ratio

Monolith:
magnetic field

At $E \lesssim 2$ GeV

$$\frac{\nu_e}{\bar{\nu}_e} \leq \frac{\mu^+}{\mu^-}$$

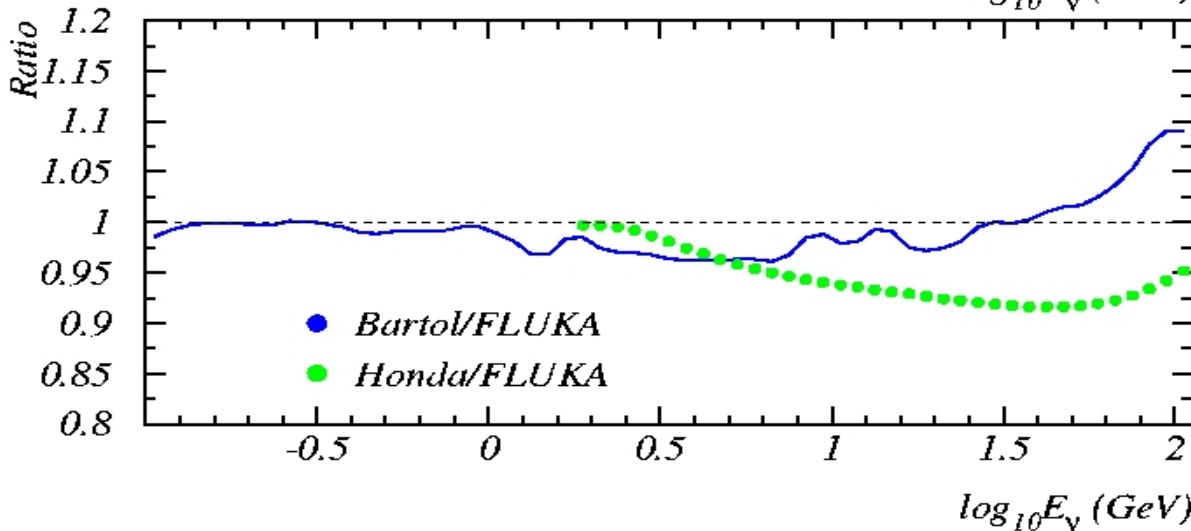
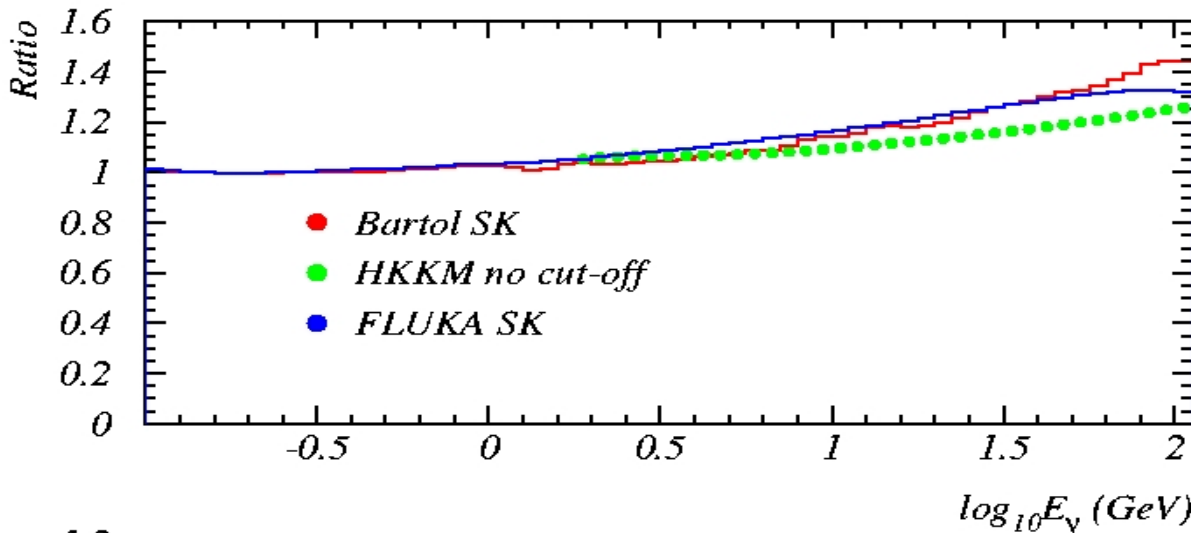
ν_e from μ decay + energy loss

Re reflects charge asymmetry in primary CRs proved by E-W asymmetry

At HE reflects K_L charge asymmetry

Charge ratio comparison: $\nu_\mu/\text{anti-}\nu_\mu$

$\nu_\mu/\bar{\nu}_\mu$ Solar min SK



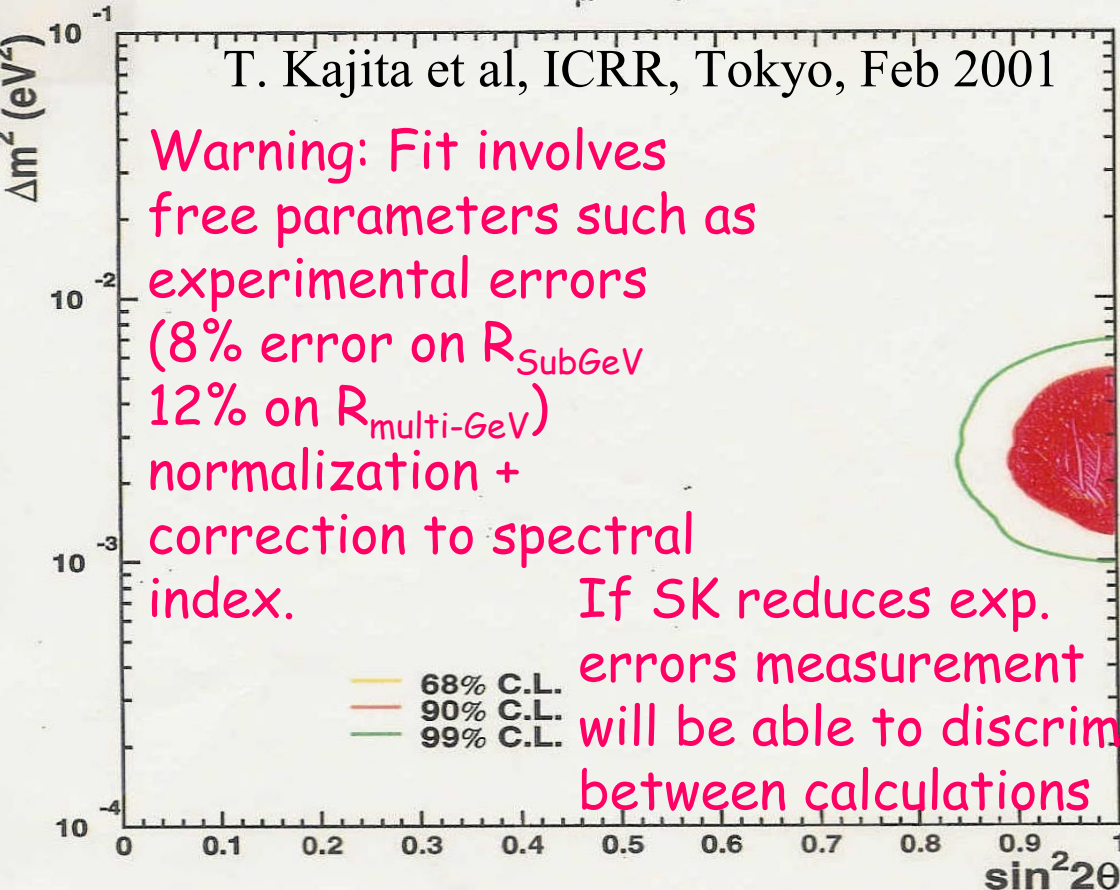
When μ do not decay increase due to meson charge asymmetry.

Check for interaction models but large differences in charge ratio at HE do not affect current measurable quantities

E.g.: upgoing μ rate changes of factor 3 if $\frac{\phi_\nu}{\phi_{\bar{\nu}}} = 0 \rightarrow \infty$

$$\begin{aligned} \text{Rate} &= \Phi_\nu \sigma_\nu + \Phi_{\bar{\nu}} \sigma_{\bar{\nu}} = \\ &= (\Phi_\nu + \Phi_{\bar{\nu}}) \sigma_{\bar{\nu}} (3r_\nu + (1-r_\nu)) \\ r_\nu &= \Phi_\nu / (\Phi_\nu + \Phi_{\bar{\nu}}) \text{ and } \sigma_{\bar{\nu}} \sim 3\sigma_\nu \\ \text{If } \Phi_\nu / \Phi_{\bar{\nu}} &\rightarrow 0 \Rightarrow r_\nu \rightarrow 0 \Rightarrow \\ \text{Rate} &\rightarrow (\Phi_\nu + \Phi_{\bar{\nu}}) \sigma_{\bar{\nu}} \\ \text{If } \Phi_\nu / \Phi_{\bar{\nu}} &\rightarrow \infty \Rightarrow r_\nu \rightarrow 1 \Rightarrow \\ \text{Rate} &\rightarrow 3(\Phi_\nu + \Phi_{\bar{\nu}}) \sigma_{\bar{\nu}} \end{aligned}$$

SK regions with FLUKA



Main differences: interaction model (Honda/Fluka) + CR spectrum

FC+PC 1290 days

Best fit $\nu\mu \rightarrow \nu\tau$: FLUKA Honda

Δm^2 (eV²) 2.4·10⁻³ 2.4·10⁻³

$\chi^2_{\text{min}}/\text{dof}$ 129.7/137 132.4/137

No oscillations

$\chi^2_{\text{min}}/\text{dof}$ 308.5/139 229.3/139

Effect on absolute normalization

Sub-GeV	e	μ
FLUKA/Honda	0.88	1.19
FLUKA/Bartol	0.89	0.87

Effect on μ/e double ratio Sub-GeV

FLUKA/Honda ~4%

FLUKA/Bartol ~3%

Multi-GeV

FLUKA/Honda ~0.7%

FLUKA/Bartol ~0.1%

Conclusions

A lot of comparison work is being done between models and data and between models themselves

Major changes for next future calculations are due to:

- Recent Precise measurements of primary CRs
- Accelerator data and atmospheric muon benchmarks (but ~10% error from experiments) which seem to favor FLUKA interaction model with respect to models producing higher π/K multiplicities

Effects at %level are investigated to reach a very good description of shower propagation, interactions, geomagnetic field, solar modulation

Normalization error will probably be decreased at 15% level but reliable measurement are flavor ratio, asymmetry, shape of HE angular distribution (all these changes produce negligible effects for Δm^2 evaluation)

If SK, Soudan2, MACRO will be able to reduce exp. errors measurements can be used to constrain calculations

Future experiments (HARP and hopefully others at higher energies) will provide necessary knowledge for future generation experiments towards an exact determination of Δm^2 and channel

Future experiments improving cross section knowledge are needed

Neutrinos from meson decay

$$\frac{dN}{dE dE_M dE_N dX} = \frac{S(E, E_M)}{(1-r_M)E_M} \times \frac{1}{d_M} \times \int_0^X \frac{dX'}{\lambda_N} P_M(E_M, X, X') \times \frac{1}{E_M} F_{NM}(E_M, E_N)$$

$M = \pi, K$
kinematic factor
 $r_M = \frac{m_{\mu, \nu}^2}{m_M^2}$
 $\times e^{X/\Lambda_N} \phi(E_N)$
CR spectrum with int. spectral index γ
nucleon spectrum @ depth X'
 $\Lambda_N, \lambda_N \equiv$ nucleon attenuation / interaction length $\sim 120 / 86 \text{ g/cm}^2$
 $\frac{1}{d_M} = \frac{\epsilon_M}{E_M X \cos \vartheta} \equiv$ decay probability ($\epsilon_\pi = 115 \text{ GeV}$ $\epsilon_K = 850 \text{ GeV}$)
 $P_M(E_M, X, X') \equiv$ survival probability (decay and interaction) of meson
 $Z_{N \rightarrow \pi} = \int_0^1 dx (x)^{\gamma-1} F_{N \rightarrow \pi}(x)$ **Z-factors** to compare interaction models in regions where γ is constant
scaling approximation ($x = E_{\text{sec}}/E_{\text{pr}}$)
inclusive cross section $p, N + \text{Air} \rightarrow \pi + X$